

CKM matrix and FCNC suppression in $SO(5) \times U(1) \times SU(3)$ gauge-Higgs unification

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Funatsu, Hatanaka, YH, Orikasa, Yamatsu

1909.00190

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Gauge-Higgs unification

125 GeV Higgs boson

||

AB phase in the 5th dim

$$P \exp \left\{ ig \oint dy A_y \right\} \sim e^{i\Theta_H(x)}$$

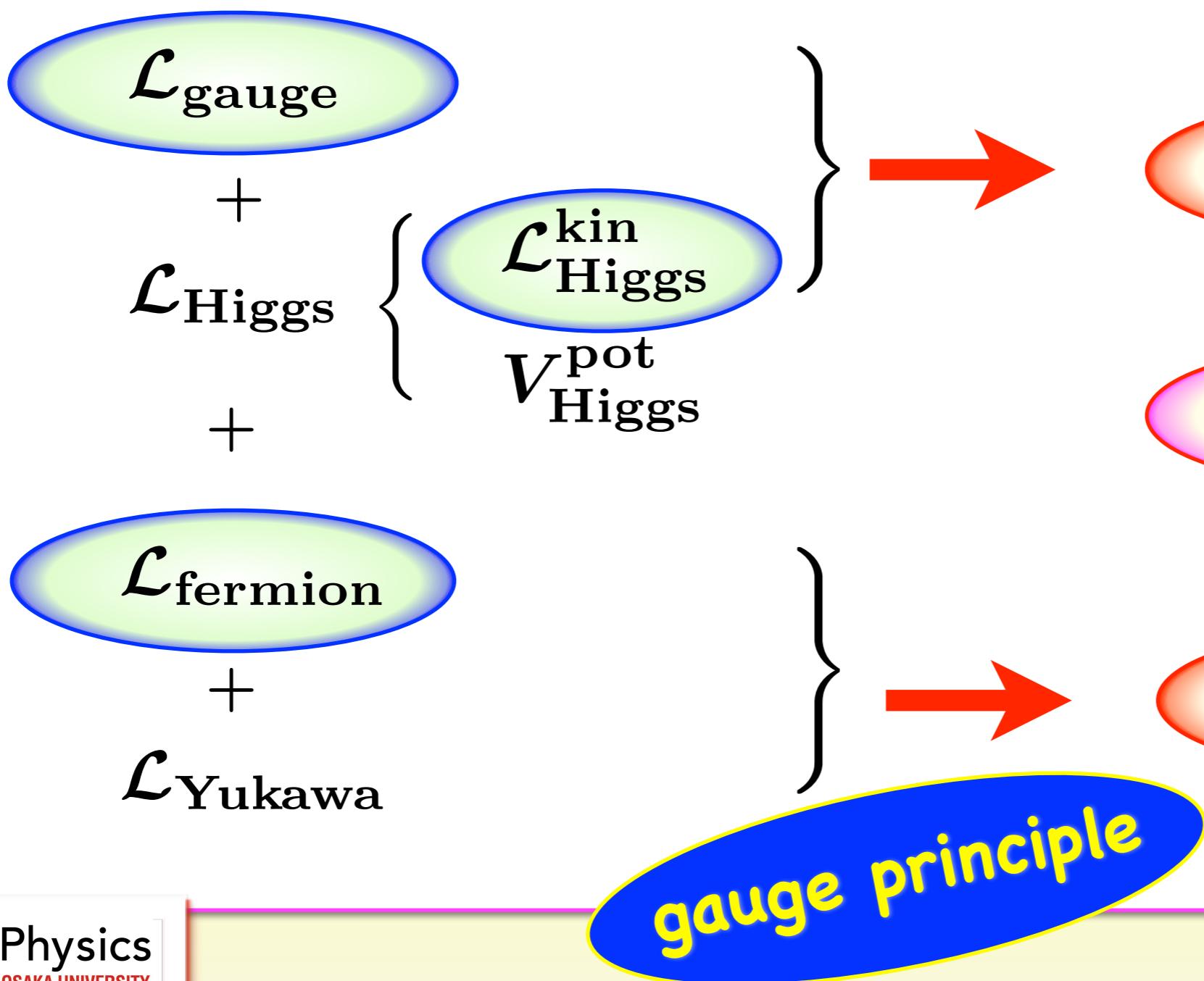
$$\Theta_H(x) = \theta_H + \frac{H(x)}{f_H}$$

$\theta_H \neq 0$

(Hosotani mechanism)

EW sym. breaking

Standard Model



Gauge-Higgs Unification

$SU(3) \times SO(5) \times U(1)$ gauge-Higgs on RS

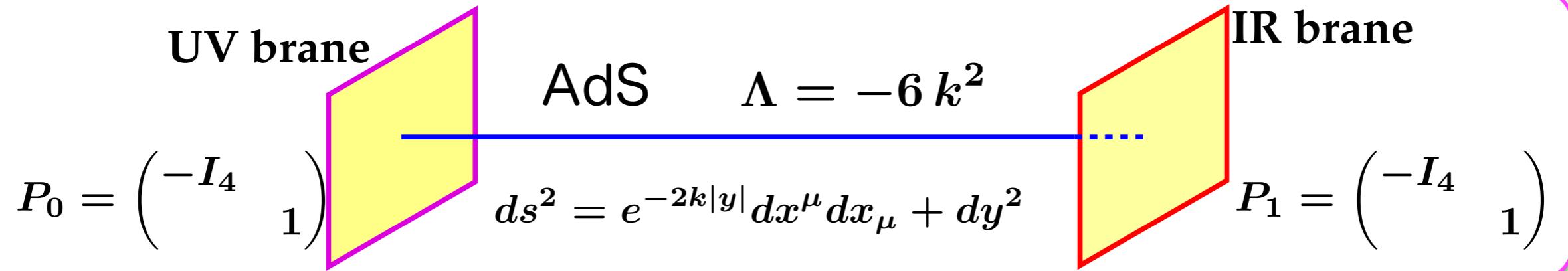
Agashe, Contino, Pomarol 2005

YH, Sakamura 2006

Medina, Shah, Wagner 2007

YH, Oda, Ohnuma, Sakamura 2008

Funatsu, Hatanaka, YH, Orikasa, Shimotani 2013



$$\rightarrow SU(3)_C \times SO(4) \times U(1)_X$$

brane scalar $\langle \hat{\Phi} \rangle$

$$\rightarrow SU(3)_C \times SU(2)_L \times U(1)_Y$$

Hosotani mechanism $\theta_H \neq 0$

$$\rightarrow SU(3)_C \times U(1)_{EM}$$

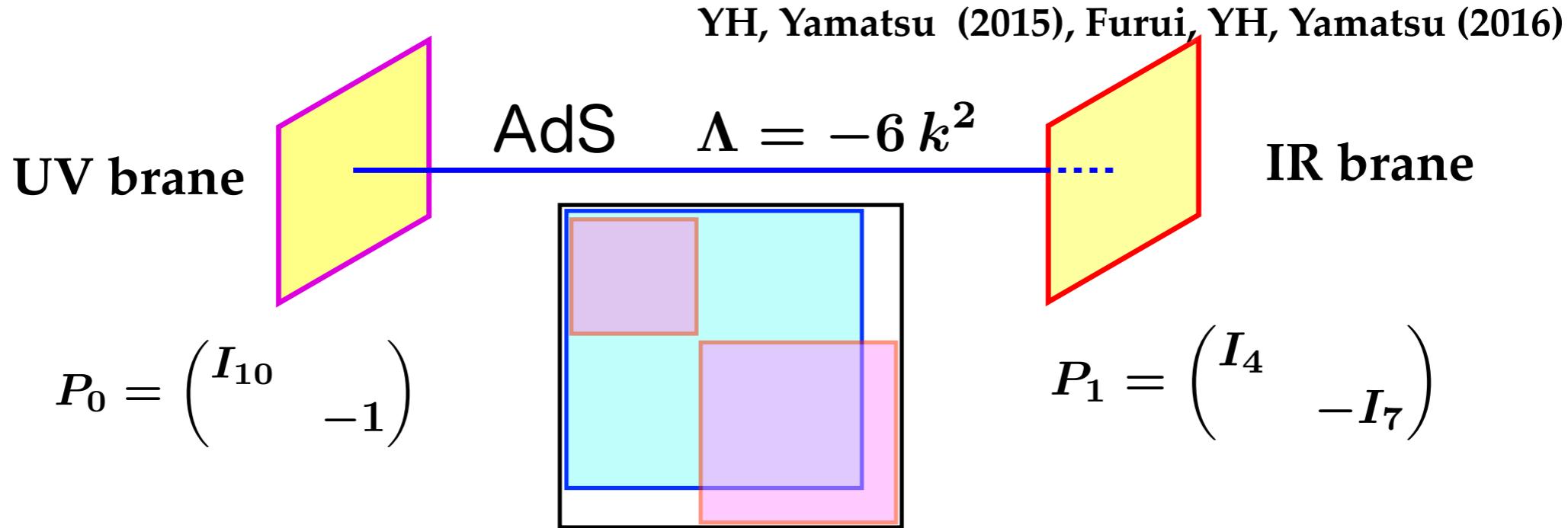
The diagram shows two components of the gauge field A_μ and A_y . The left component A_μ is associated with the W , Z , and γ bosons, represented by a blue oval inside a red rectangle. The right component A_y is associated with the Higgs field, represented by a blue oval inside a green rectangle. Below these, the expression $e^{i\hat{\theta}_H(x)} \sim P \exp \left\{ ig \int dy A_y \right\}$ is given, where P is the path integral measure.

Matter

$SU(3)_C \times SO(5) \times U(1)_X$ content

	B model GUT inspired	A model previous model
quark	$(3, 4)_{\frac{1}{6}}$ $(3, 1)^+_{-\frac{1}{3}}$ $(3, 1)^-_{-\frac{1}{3}}$	$(3, 5)_{\frac{2}{3}}$ $(3, 5)_{-\frac{1}{3}}$
lepton	$(1, 4)_{-\frac{1}{2}}$	$(1, 5)_0$ $(1, 5)_{-1}$
dark fermion	$(3, 4)_{\frac{1}{6}}$ $(1, 5)_0^+$ $(1, 5)_0^-$	$(1, 4)_{\frac{1}{2}}$
brane fermion	ν_χ $(1, 1)_0$	$(3, [2, 1])_{\frac{7}{6}, \frac{1}{6}, -\frac{5}{6}}$ $(1, [2, 1])_{\frac{1}{2}, -\frac{1}{2}, -\frac{3}{2}}$
brane scalar	$\hat{\Phi}$ $(1, 4)_{\frac{1}{2}}$	$(1, [1, 2])_{\frac{1}{2}}$
symmetry of brane interactions	$SU(3)_C \times SO(5) \times U(1)_X$	$SU(3)_C \times SO(4) \times U(1)_X$

SO(11) gauge-Higgs grand unification



$$SO(4) \times SO(6) \simeq SU(2)_L \times SU(2)_R \times SU(4)$$

$$\langle \hat{\Phi}_{32} \rangle \longrightarrow SU(2)_L \times U(1)_Y \times SU(3)_C$$

$$\Psi_{32} \begin{pmatrix} u & \nu \\ d & e \\ u' & \nu' \\ d' & e' \end{pmatrix} \begin{pmatrix} \hat{u} & \hat{\nu} \\ \hat{d} & \hat{e} \\ \hat{u}' & \hat{\nu}' \\ \hat{d}' & \hat{e}' \end{pmatrix} \quad \Psi_{11} \begin{pmatrix} N & \hat{E} \\ E & \hat{N} \\ D^+ & D^- \\ S \end{pmatrix}$$

Up-type quarks are only in “spinor 32”.

Quark sector in B model

field	\mathcal{G}	G_{22}	left-handed	right-handed	name
$\Psi_{(3,4)}^\alpha$	$(\mathbf{3}, \mathbf{4})_{\frac{1}{6}}$	[2, 1]	(+, +)	(-, -)	$u \ c \ t$ $d \ s \ b$
		[1, 2]	(-, -)	(+, +)	$u' \ c' \ t'$ $d' \ s' \ b'$
$\Psi_{(3,1)}^{\pm\alpha}$	$(\mathbf{3}, \mathbf{1})_{-\frac{1}{3}}$	[1, 1]	(\pm , \pm)	(\mp , \mp)	$D_d^\pm \ D_s^\pm \ D_b^\pm$
$\hat{\Phi}_{(1,4)}$	$(\mathbf{1}, \mathbf{4})_{\frac{1}{2}}$		brane scalar		$\hat{\Phi}$

Action in the bulk

$$\sum_{\alpha=1}^3 \left\{ \bar{\Psi}_{(3,4)}^\alpha \mathcal{D}(c_\alpha) \Psi_{(3,4)}^\alpha + \left(\bar{\Psi}_{(3,1)}^{+\alpha}, \bar{\Psi}_{(3,1)}^{-\alpha} \right) \begin{pmatrix} \mathcal{D}(c_{D_\alpha}) & -m_{D_\alpha} \\ -m_{D_\alpha} & \mathcal{D}(c_{D_\alpha}) \end{pmatrix} \begin{pmatrix} \Psi_{(3,1)}^{+\alpha} \\ \Psi_{(3,1)}^{-\alpha} \end{pmatrix} \right\}$$

$$\mathcal{D}(c) = \gamma^A e_A{}^M \left(D_M + \frac{1}{8} \omega_{MBC} [\gamma^B, \gamma^C] \right) - c \sigma'(y) ,$$

$$D_M = \partial_M - i g_S A_M^{SU(3)} - i g_A A_M^{SO(5)} - i g_B Q_X A_M^{U(1)}$$

Brane interactions

$$\begin{pmatrix} u \\ d \\ u' \\ d' \end{pmatrix}$$

$$\int d^5x \sqrt{-g} \delta(y) \left\{ y_B \bar{\Psi}_{(3,1)}_{-\frac{1}{3}} \hat{\Phi}_{(1,4)}^\dagger \frac{1}{2} \Psi_{(3,4)} \frac{1}{6} + \text{h.c.} \right\}$$

D



brane scalar

$$\langle \hat{\Phi}_{(1,4)} \rangle \neq 0$$

$$\rightarrow SO(4) \times U(1)_X \rightarrow SU(2)_L \times U(1)_Y$$

$$\rightarrow \mu D_L^\dagger d'_R$$

mass splitting

$$m_d \neq m_u$$

flavor mixing →

CKM

FCNC ?

Scale

$$m_W \simeq \sqrt{\frac{k}{L}} z_L^{-1} \sin \theta_H \simeq \frac{\sin \theta_H}{\pi \sqrt{kL}} m_{\text{KK}}$$

$$m_t \sim \pi^{-1} \sqrt{1 - 4c_t^2} \sin \frac{1}{2}\theta_H m_{\text{KK}}$$

$$m_{u,c} \sim \pi^{-1} \sqrt{4c_{u,c}^2 - 1} z_L^{-|c_{u,c}|+0.5} \sin \frac{1}{2}\theta_H m_{\text{KK}}$$

$$m_{\text{KK}} = \pi k z_L^{-1}, \quad z_L = e^{kL}$$

$$z_L = 10^{10}$$

θ_H	m_{KK} (TeV)	k (GeV)	c_u	c_c	c_t
0.10	12.08	3.84×10^{13}	-0.9169	-0.7545	-0.2274
0.15	8.07	2.57×10^{13}	-0.9170	-0.7546	-0.2294

CKM mixing

mass: up-type quarks

gauge interactions ($\theta_H \neq 0$) only

→ no mixing

mass: down-type quarks

gauge int. ($\theta_H \neq 0$) + brane int.

→ mass eigenstates \neq gauge eigenstates

→ CKM mixing

Effective mass matrix

$$\begin{aligned}
 (\vec{\bar{d}}_L, \vec{\bar{D}}_L) & \mathcal{M}_{\text{down}} \begin{pmatrix} \vec{d}'_R \\ \vec{D}_R \end{pmatrix} + h.c. & \vec{d} = \begin{pmatrix} d \\ s \\ b \end{pmatrix} \\
 & \parallel \\
 \begin{pmatrix} M_{\text{up}} & 0 \\ \mu & m_D \end{pmatrix} & = \Omega \begin{pmatrix} M_{\text{down}} & 0 \\ 0 & M_D \end{pmatrix} \tilde{\Omega}^\dagger
 \end{aligned}$$

Mass eigenstates

$$\begin{pmatrix} \vec{\hat{d}}_L \\ \vec{\hat{D}}_L \end{pmatrix} = \Omega^\dagger \begin{pmatrix} \vec{d}_L \\ \vec{D}_L \end{pmatrix} \quad \begin{pmatrix} \vec{\hat{d}}_R \\ \vec{\hat{D}}_R \end{pmatrix} = \tilde{\Omega}^\dagger \begin{pmatrix} \vec{d}'_R \\ \vec{D}_R \end{pmatrix}$$

$$\Omega \Omega^\dagger = \tilde{\Omega} \tilde{\Omega}^\dagger = 1 \quad \Omega = \begin{pmatrix} \Omega_q & \Omega_b \\ \Omega_a & \Omega_D \end{pmatrix} \quad \Omega_q \Omega_q^\dagger \neq 1$$

CKM

$$\mathcal{L}_W \simeq \frac{g_L^W}{\sqrt{2}} W_\mu \vec{u}_L \Gamma^\mu \vec{d}_L \simeq \frac{g_L^W}{\sqrt{2}} W_\mu \vec{\hat{u}}_L \Gamma^\mu \underline{\Omega_q} \vec{\hat{d}}_L$$



$$V^{\text{CKM}} \simeq \Omega_q$$

$$\begin{pmatrix} M_{\text{up}} & 0 \\ \mu & m_D \end{pmatrix} \begin{pmatrix} \tilde{\Omega}_q^\dagger & \tilde{\Omega}_a^\dagger \\ \tilde{\Omega}_b^\dagger & \tilde{\Omega}_D^\dagger \end{pmatrix} = \begin{pmatrix} \Omega_q & \Omega_b \\ \Omega_a & \Omega_D \end{pmatrix} \begin{pmatrix} M_{\text{down}} & 0 \\ 0 & M_D \end{pmatrix} \quad \rightarrow \quad \text{Red Arrow}$$

$$\Omega_b = -\Omega_q M_{\text{down}} \tilde{\Omega}_b \tilde{\Omega}_D^{-1} M_D^{-1} \rightarrow ||\Omega_b|| = O\left(\frac{m_{d,s,b}}{m_D}\right) ||\tilde{\Omega}_b|| < 10^{-3}$$

$$M_{\text{up}} \tilde{\Omega}_q^\dagger = \Omega_q M_{\text{down}} \rightarrow \frac{m_{dk}}{m_{uj}} |V_{jk}^{\text{CKM}}| \sim |(\tilde{\Omega}_q^\dagger)_{jk}| < 1$$

$\rightarrow m_u > m_d$ — need to be solved.

FCNC

$$\begin{aligned}\mathcal{L}_Z^{\text{down}} \sim & -\frac{g_w}{\cos \theta_W} Z_\mu \left\{ -\frac{1}{2} \vec{\hat{d}}_L \Gamma^\mu \underline{\Omega_q^\dagger \Omega_q} \vec{\hat{d}}_L + \frac{1}{3} \sin^2 \theta_W \left(\vec{\hat{d}}_L \Gamma^\mu \vec{\hat{d}}_L + \vec{\hat{d}}_R \Gamma^\mu \vec{\hat{d}}_R \right) \right\} \\ & = I - \Omega_a^\dagger \Omega_a\end{aligned}$$

$$\Omega_a^\dagger \Omega_a = \Omega_q^\dagger \Omega_b \Omega_b^\dagger (\Omega_q^\dagger)^{-1} = O\left(\frac{m_{d,s,b}^2}{m_D^2}\right) \lesssim 10^{-6}$$

FCNC : suppressed naturally

Rigorous evaluation of W, Z couplings

$$m_Z, z_L = 10^{10}$$

θ_H	m_{KK} (TeV)	c_u	c_c	c_t
0.10	12.08	-0.9169	-0.7545	-0.2274
0.15	8.07	-0.9170	-0.7546	-0.2294

$$\mathcal{L}_{\text{brane}} = \delta(y) \left\{ 2\mu_{\alpha\beta} \bar{d}'^\alpha_R D_L^{+\beta} + \text{h.c.} \right\}$$

$$\mu = \begin{pmatrix} 0.1 & & \\ & 0.1 & \\ & & 1 \end{pmatrix} U_{23}^\dagger(0.002) U_{12}^\dagger(0.106)$$

$$\frac{m_{D_\alpha}}{k} = 1 \quad (c_{D_d}, c_{D_s}, c_{D_b}) \leftarrow (m_d, m_s, m_b)$$

$$\int_1^{z_L} dz \sqrt{-\det G} \sum_{\alpha=1}^3 \left\{ \bar{\Psi}_{(3,4)}^\alpha \mathcal{D}(c_\alpha) \Psi_{(3,4)}^\alpha + \dots \right\}$$



W

$$\theta_H = 0.10$$

$$g_L^W = 0.9978 g_w , \quad \hat{V}_{\text{CKM}} = \begin{pmatrix} 0.9744 & 0.2245 & 0.0031 \\ -0.2245 & 0.9743 & 0.0134 \\ 9 \times 10^{-6} & -0.0138 & 1.0002 \end{pmatrix}$$

$$g_L^W / g_{L \text{ lepton}}^W = 1.00013$$

CKM

$$\theta_H = 0.15$$

$$g_L^W = 0.9950 g_w , \quad \hat{V}_{\text{CKM}} = \begin{pmatrix} 0.9737 & 0.2264 & 0.0043 \\ -0.2264 & 0.9736 & 0.0185 \\ 1 \times 10^{-5} & -0.0190 & 1.0004 \end{pmatrix}$$

$$g_L^W / g_{L \text{ lepton}}^W = 1.00028$$

Z

$$\theta_H = 0.15$$

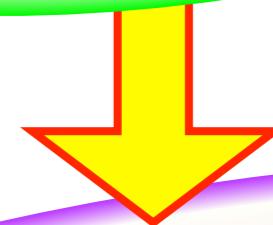
$$\begin{pmatrix} g_{Luu}^Z \\ g_{Lcc}^Z \\ g_{Ltt}^Z \end{pmatrix} = \begin{pmatrix} 0.3441 \\ 0.3441 \\ 0.3449 \end{pmatrix} g_w , \quad \begin{pmatrix} g_{Ruu}^Z \\ g_{Rcc}^Z \\ g_{Rtt}^Z \end{pmatrix} = \begin{pmatrix} -0.1533 \\ -0.1533 \\ -0.1524 \end{pmatrix} g_w$$

$$\hat{g}_{Ld}^Z = g_w \begin{pmatrix} -0.4208 & -7 \times 10^{-7} & -1 \times 10^{-8} \\ -7 \times 10^{-7} & -0.4208 & -4 \times 10^{-7} \\ -1 \times 10^{-8} & -4 \times 10^{-7} & -0.4207 \end{pmatrix}$$

$$\hat{g}_{Rd}^Z = g_w \begin{pmatrix} 0.0767 & -1 \times 10^{-6} & -1 \times 10^{-6} \\ -1 \times 10^{-6} & 0.0767 & -7 \times 10^{-6} \\ -1 \times 10^{-6} & -7 \times 10^{-6} & 0.0767 \end{pmatrix}$$

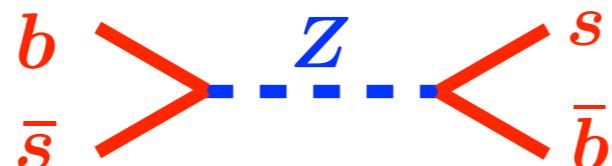
very close to SM at low energies !

$SO(5) \times U(1) \times SU(3)$
gauge invariance



FCNC : suppressed

$B_s^0 \bar{B}_s^0$ mixing



$$\Delta m_M \sim \frac{m_M f_M^2 (\hat{g}_d^Z|_M)^2}{3m_Z^2}$$

$$\begin{pmatrix} \Delta m_K \\ \Delta m_{B_d} \\ \Delta m_{B_s} \end{pmatrix} \sim \begin{pmatrix} 2 \times 10^{-19} \\ 3 \times 10^{-18} \\ 3 \times 10^{-16} \end{pmatrix} \text{GeV} \ll \begin{pmatrix} 3.48 \times 10^{-15} \\ 3.36 \times 10^{-13} \\ 1.17 \times 10^{-11} \end{pmatrix} \text{GeV}$$

(exp)

$$\frac{1}{g_{L \text{ lepton}}^W} \begin{pmatrix} g_{Luu}^Z \\ g_{Ruu}^Z \\ g_{Ldd}^Z \\ g_{Rdd}^Z \end{pmatrix} = \begin{pmatrix} \theta_H = 0.10 \\ 0.34588 \\ -0.15413 \\ -0.42295 \\ 0.07707 \end{pmatrix}, \begin{pmatrix} \theta_H = 0.15 \\ 0.34591 \\ -0.15411 \\ -0.42298 \\ 0.07706 \end{pmatrix} \Leftrightarrow \begin{pmatrix} SM \\ 0.3458 \\ -0.1541 \\ -0.4229 \\ 0.0771 \end{pmatrix}$$

CKM matrix in GHU
FCNC naturally suppressed

Higgs couplings

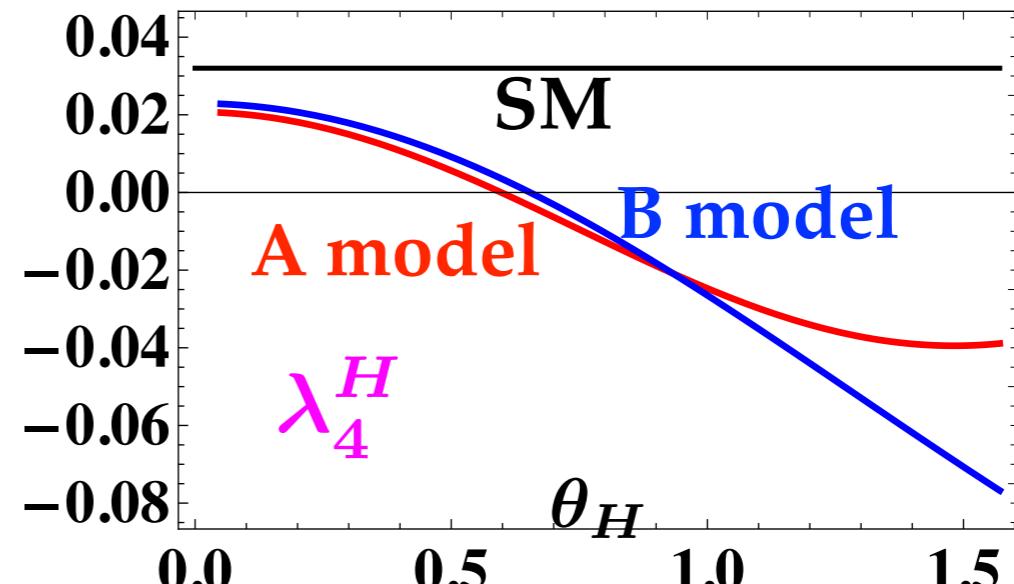
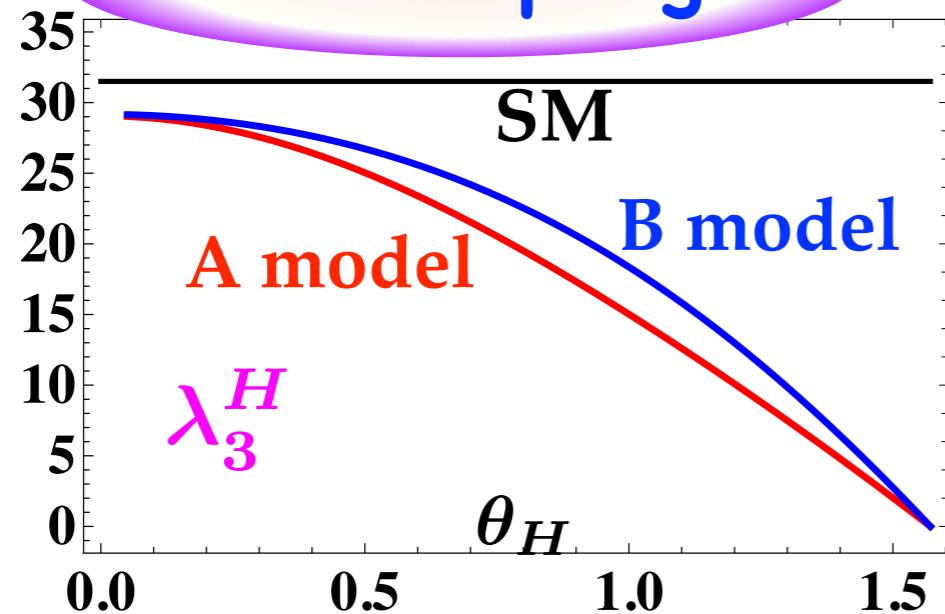
WWH, ZZH

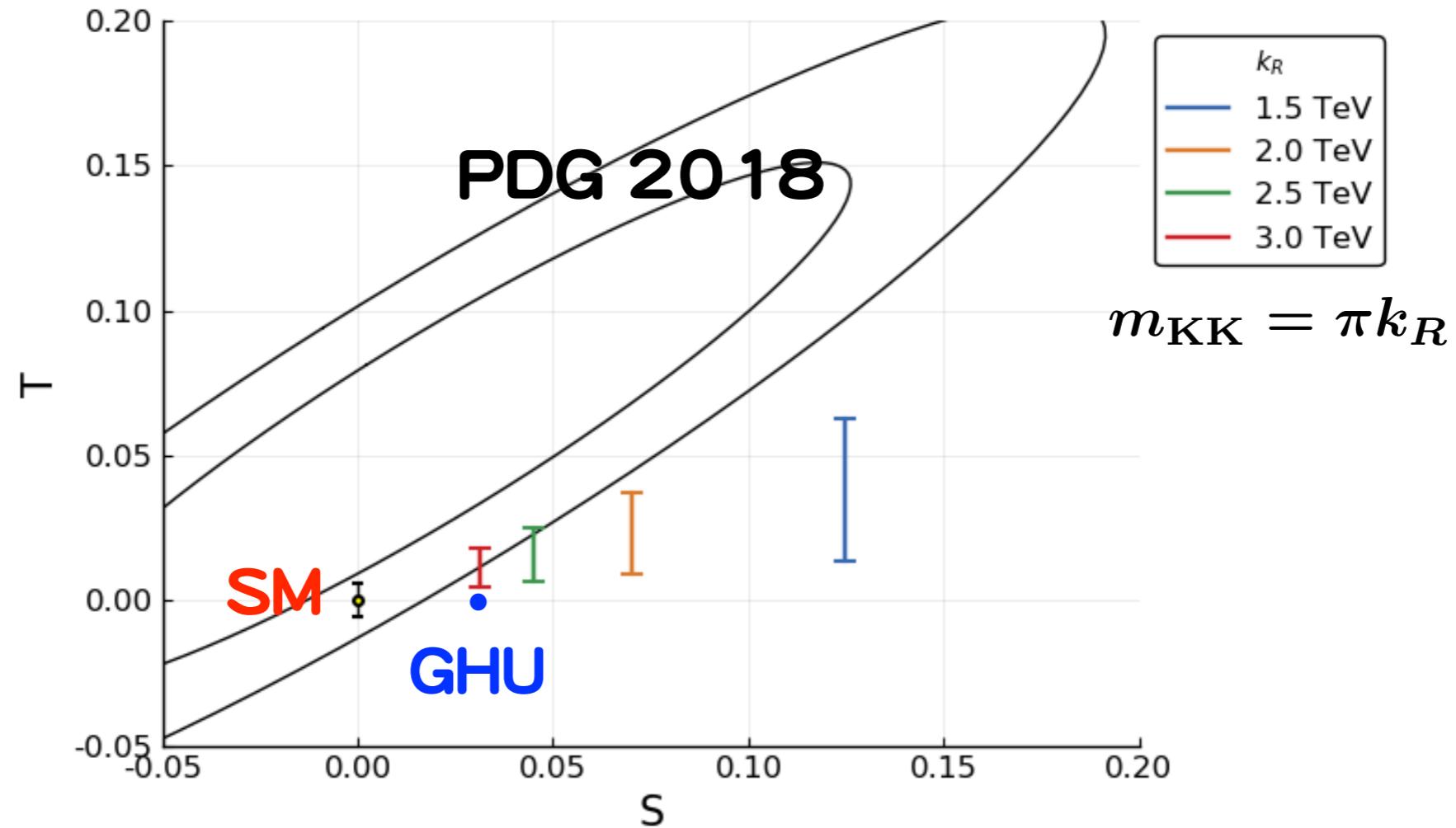
$$\sim (\text{SM}) \times \cos \theta_H$$

Yukawa couplings $\sim \begin{cases} (\text{SM}) \times \cos \theta_H & \text{A model} \\ (\text{SM}) \times \cos^2 \frac{1}{2}\theta_H & \text{B model} \end{cases}$

Deviation from SM is small for $\theta_H \sim 0.1$

self-couplings





Yoon-Peskin, PRD 100, 015001 (2019)

Z' couplings in RS

Z' : $Z^{(1)}$ $\gamma^{(1)}$ $Z_R^{(1)}$ $m \sim 0.8 m_{\text{KK}}$
localized near IR

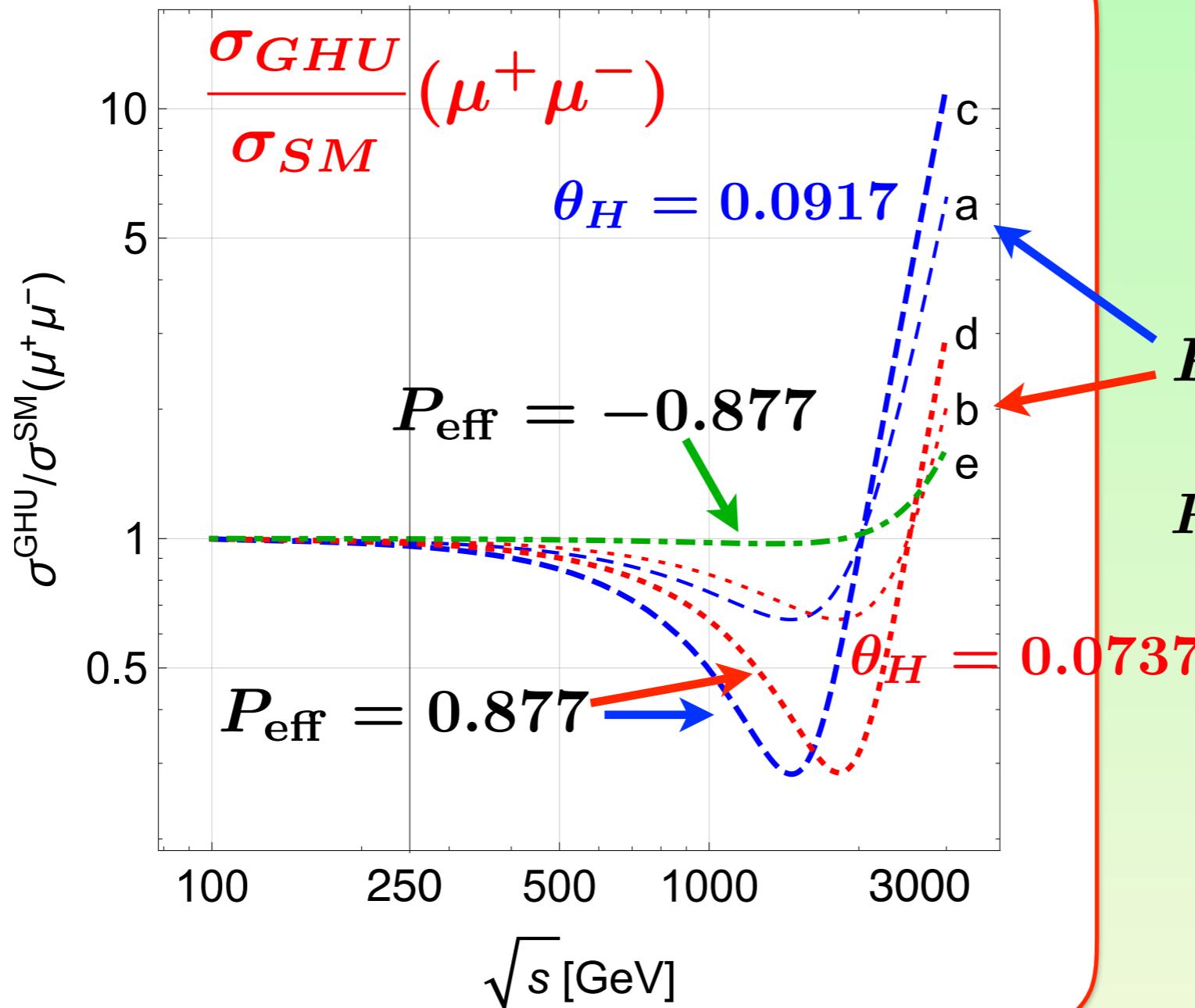
	c_ℓ, c_q	left-handed ℓ_L, q_L	right-handed ℓ_R, q_R
A model	> 0	near UV	near IR large Z' coupling
B model GUT inspired	< 0	near IR large Z' coupling	near UV

$$\mathcal{M} = \frac{e^-}{e^+} \text{---} \overset{Z, \gamma}{\text{---}} \text{---} \overset{\mu^-}{\mu^+} + \frac{e^-}{e^+} \text{---} \overset{Z_R^{(1)}, Z^{(1)}, \gamma^{(1)}}{\text{---}} \text{---} \overset{\mu^-}{\mu^+}$$

$$\mathcal{M}_0 \qquad \qquad \qquad \mathcal{M}_{Z'}$$

$$m_Z^2 \ll s \ll m_{Z'}^2$$

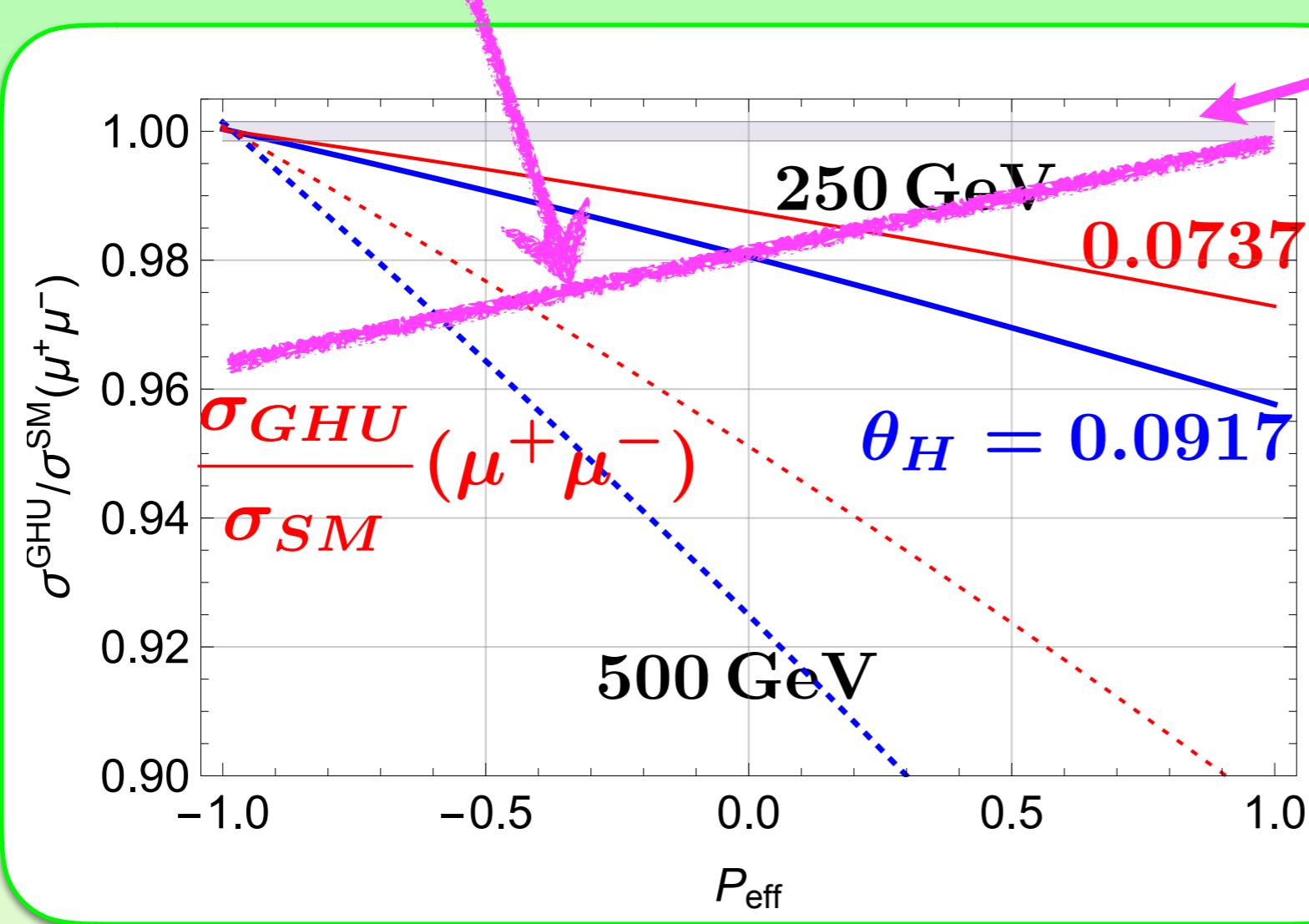
$e^+e^- \rightarrow \mu^+\mu^-$



A model

B model

(GUT inspired)



A model

$$P_{\text{eff}} = \frac{P_{e^-} - P_{e^+}}{1 - P_{e^-} P_{e^+}}$$

Distinguish

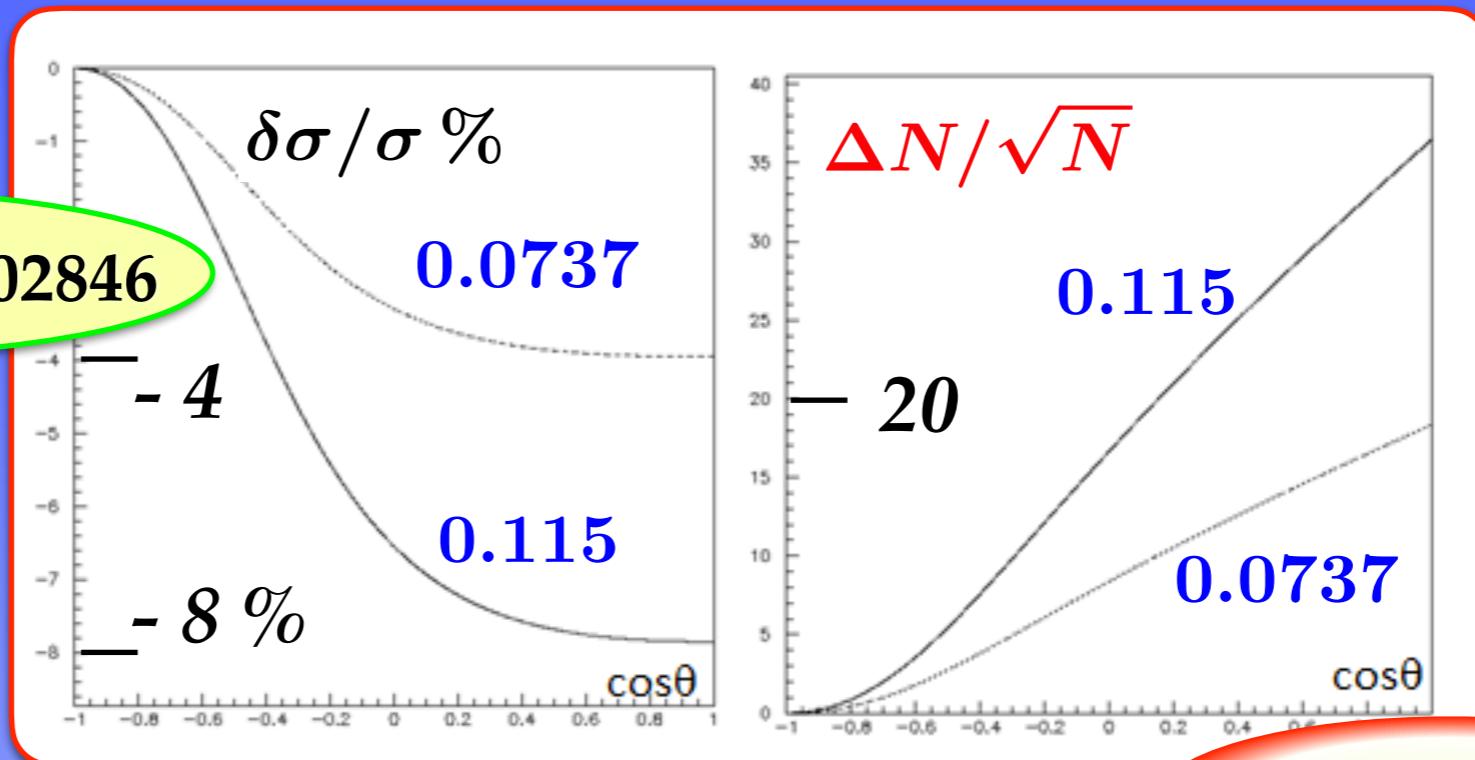
A model

B model

by polarization dependence

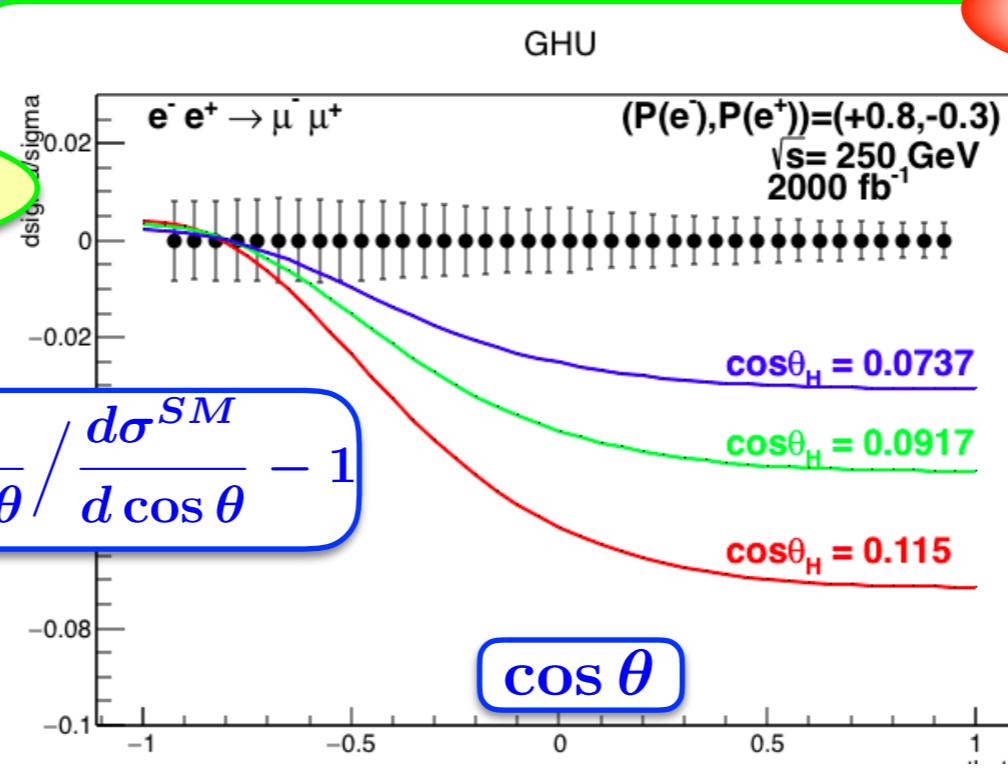
Angular distribution $e^+e^- \rightarrow \mu^+\mu^-$

F. Richard, 1804.02846



T. Suehara, ALCW2018

$$\Delta = \frac{d\sigma}{d\cos\theta} / \frac{d\sigma^{SM}}{d\cos\theta} - 1$$



A model

ILC 250
2000 fb^{-1}

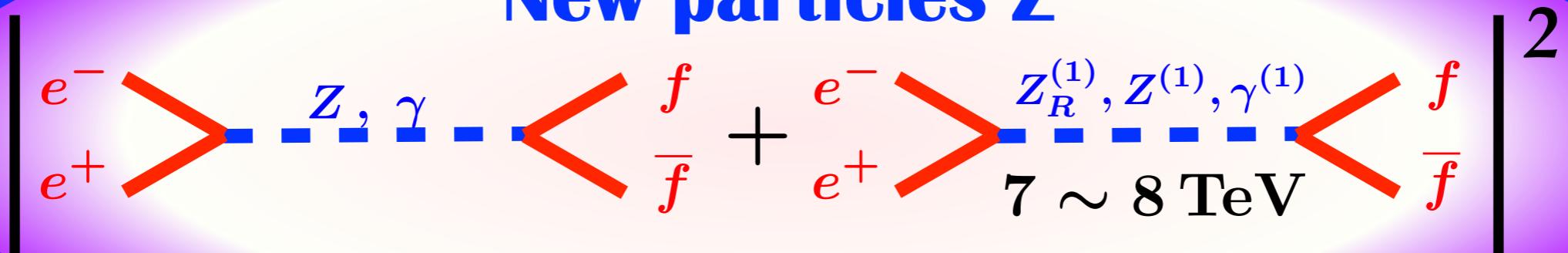
Summary

GUT inspired gauge-Higgs unification

Flavor mixing – CKM matrix

Natural suppression of FCNC

New particles Z'



in the early stage of ILC250