

Swampland Conjectures



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2022/11/01 Nagoya University

Kitahara-san's request:

Talk for master students
interested in particle phenomenology.

Standard Model of Elementary Particles

three generations of matter (fermions)				interactions / force carriers (bosons)		
	I	II	III			
QUARKS	mass charge spin	$\approx 2.2 \text{ MeV}/c^2$ $\frac{2}{3}$ $\frac{1}{2}$	$\approx 1.28 \text{ GeV}/c^2$ $\frac{2}{3}$ $\frac{1}{2}$	$\approx 173.1 \text{ GeV}/c^2$ $\frac{2}{3}$ $\frac{1}{2}$	0 0 1	$\approx 124.97 \text{ GeV}/c^2$ 0 0
	u up	c charm	t top	g gluon	H higgs	
	$\approx 4.7 \text{ MeV}/c^2$ $-\frac{1}{3}$ $\frac{1}{2}$	$\approx 96 \text{ MeV}/c^2$ $-\frac{1}{3}$ $\frac{1}{2}$	$\approx 4.18 \text{ GeV}/c^2$ $-\frac{1}{3}$ $\frac{1}{2}$	0 0 1	γ photon	
LEPTONS	$\approx 0.511 \text{ MeV}/c^2$ -1 $\frac{1}{2}$	$\approx 105.66 \text{ MeV}/c^2$ -1 $\frac{1}{2}$	$\approx 1.7768 \text{ GeV}/c^2$ -1 $\frac{1}{2}$	$\approx 91.19 \text{ GeV}/c^2$ 0 1	Z Z boson	
	e electron	μ muon	τ tau	W W boson		
	$< 1.0 \text{ eV}/c^2$ 0 $\frac{1}{2}$	$< 0.17 \text{ MeV}/c^2$ 0 $\frac{1}{2}$	$< 18.2 \text{ MeV}/c^2$ 0 $\frac{1}{2}$	$\approx 80.39 \text{ GeV}/c^2$ ± 1 1		
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino			

GAUGE BOSONS
VECTOR BOSONS

SCALAR BOSONS

Q_{color}
is m

GAUGE BOSONS
VECTOR BOSONS

SCALAR BOSONS

Quantum Gravity (QG)
Observed!
is missing.

Two Question

1: Do we have a framework of QG?

String Theory

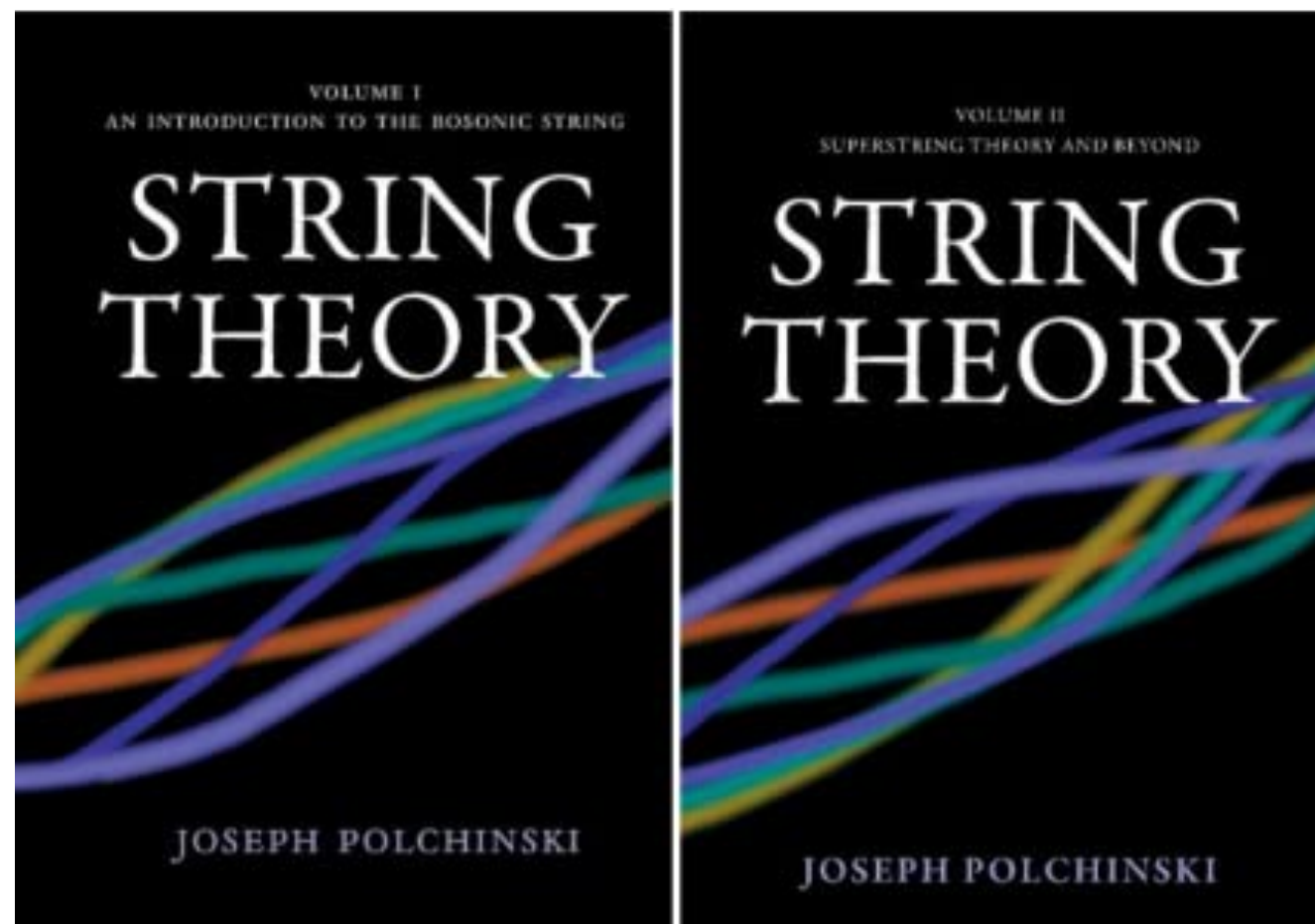
2: Is QG relevant at low-energy?

If not, QG is not useful for particle pheno at (low energy) $\ll M_P$
even though it is useful to study the scattering at M_P .

String Theory: A candidate of Quantum Gravity.

Advantage:

Around the flat background, the one-loop diagram of graviton is finitely computed!



String Theory: A candidate of Quantum Gravity.

Advantage:

The **entropy of BPS black hole** (stable black hole by supersymmetry) is reproduced!



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Physics Letters B 379 (1996) 99–104

Microscopic origin of the Bekenstein-Hawking entropy

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Abstract

The Bekenstein-Hawking area-entropy relation $S_{\text{BH}} = A/4$ is derived for a class of five-dimensional extremal black holes in string theory by counting the degeneracy of BPS soliton bound states.

Two Question

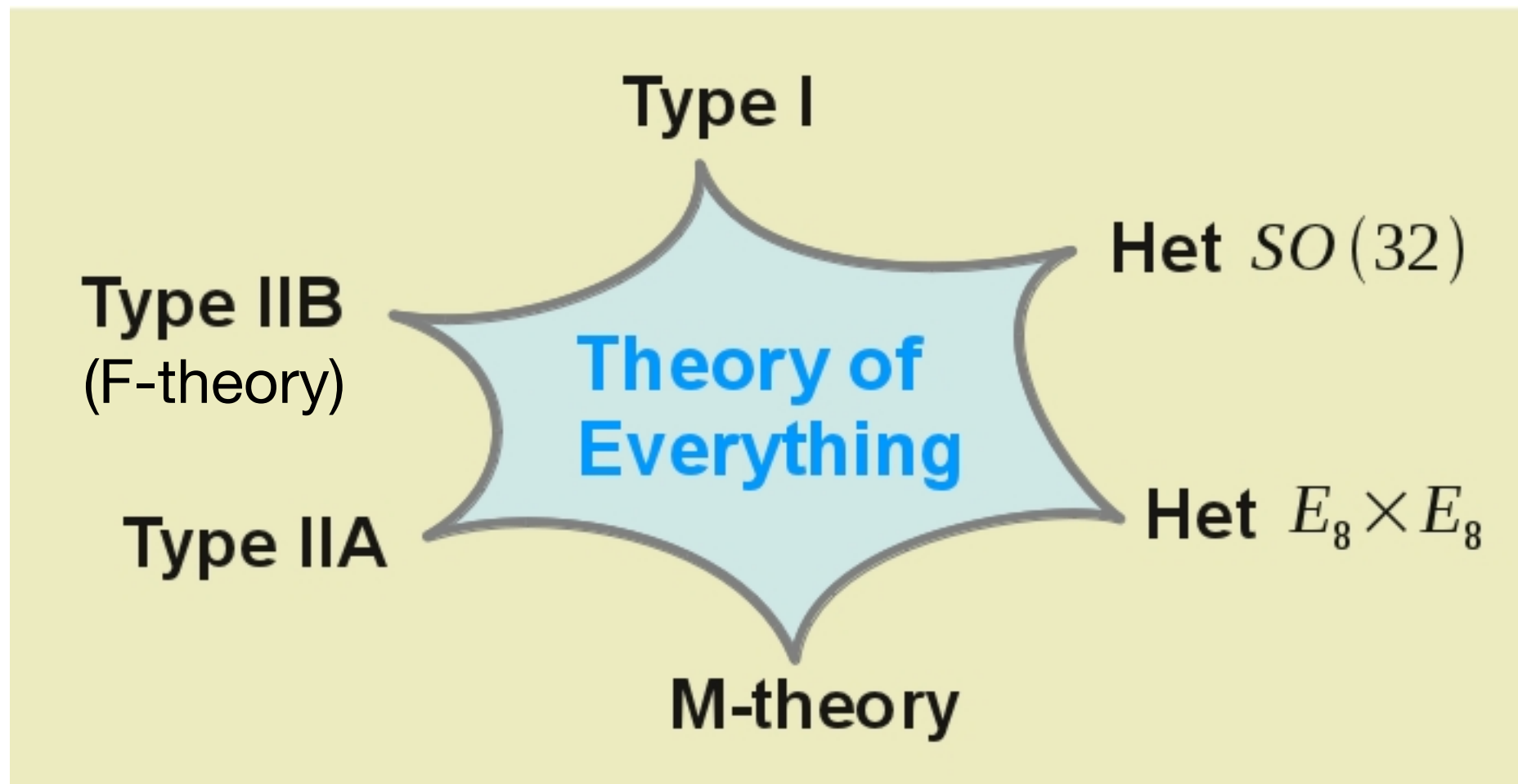
1: Do we have a framework of QG?

String Theory

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even though it is useful to study the scattering at M_P .

String Theory predicts 10 or 11 dimensions.



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Of course, our universe is 4 dimensional.

$$10 = \underset{\text{our universe}}{4} + \underset{\text{extra dimension (compact dimension)}}{6}$$

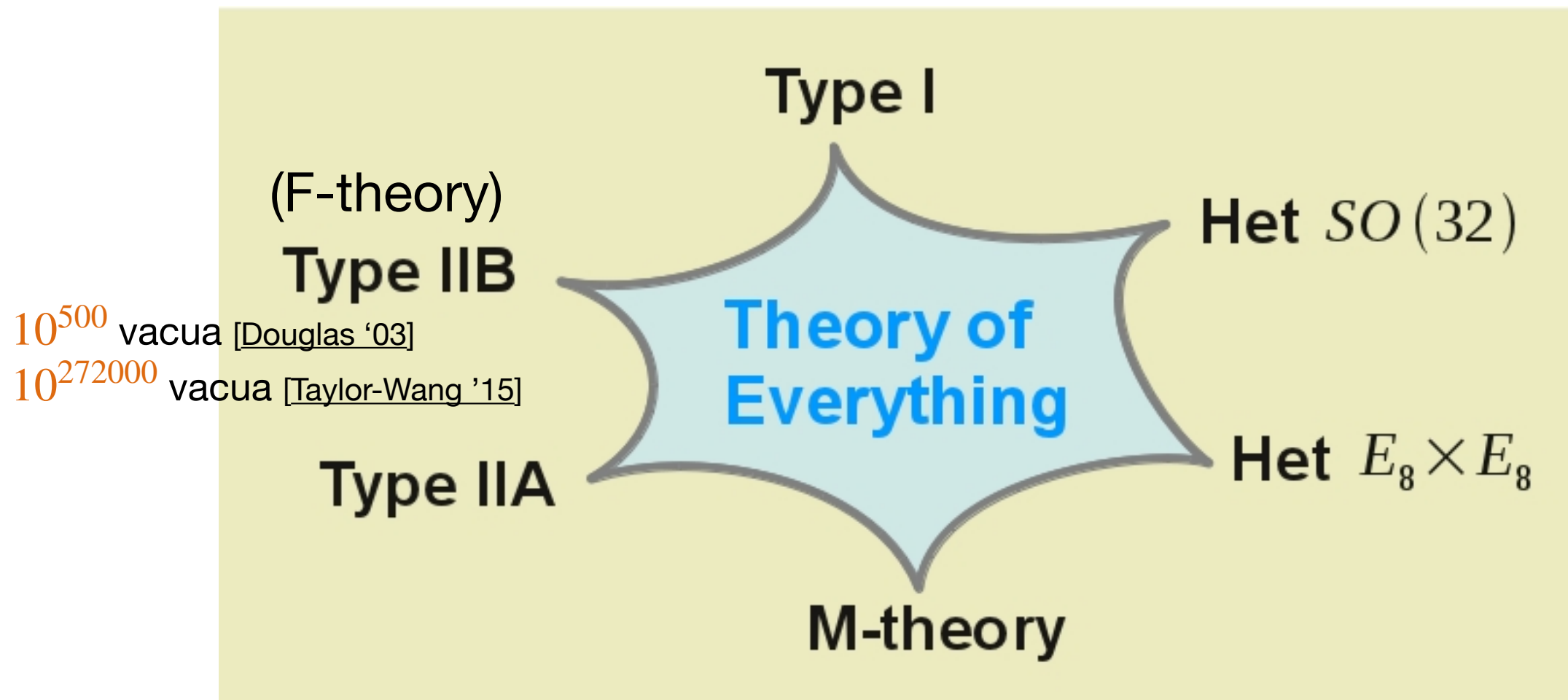
String theory predicts extra dimensions.

Choice of extra dimensions = Choice of EFT.

$$\forall \text{EFT}_A \exists \text{extra dim}_X, \text{s.t. (string theory on extra dim}_X) = \text{EFT}_A$$

If this is the case, string theory may not be useful for low-energy.

Number of vacua



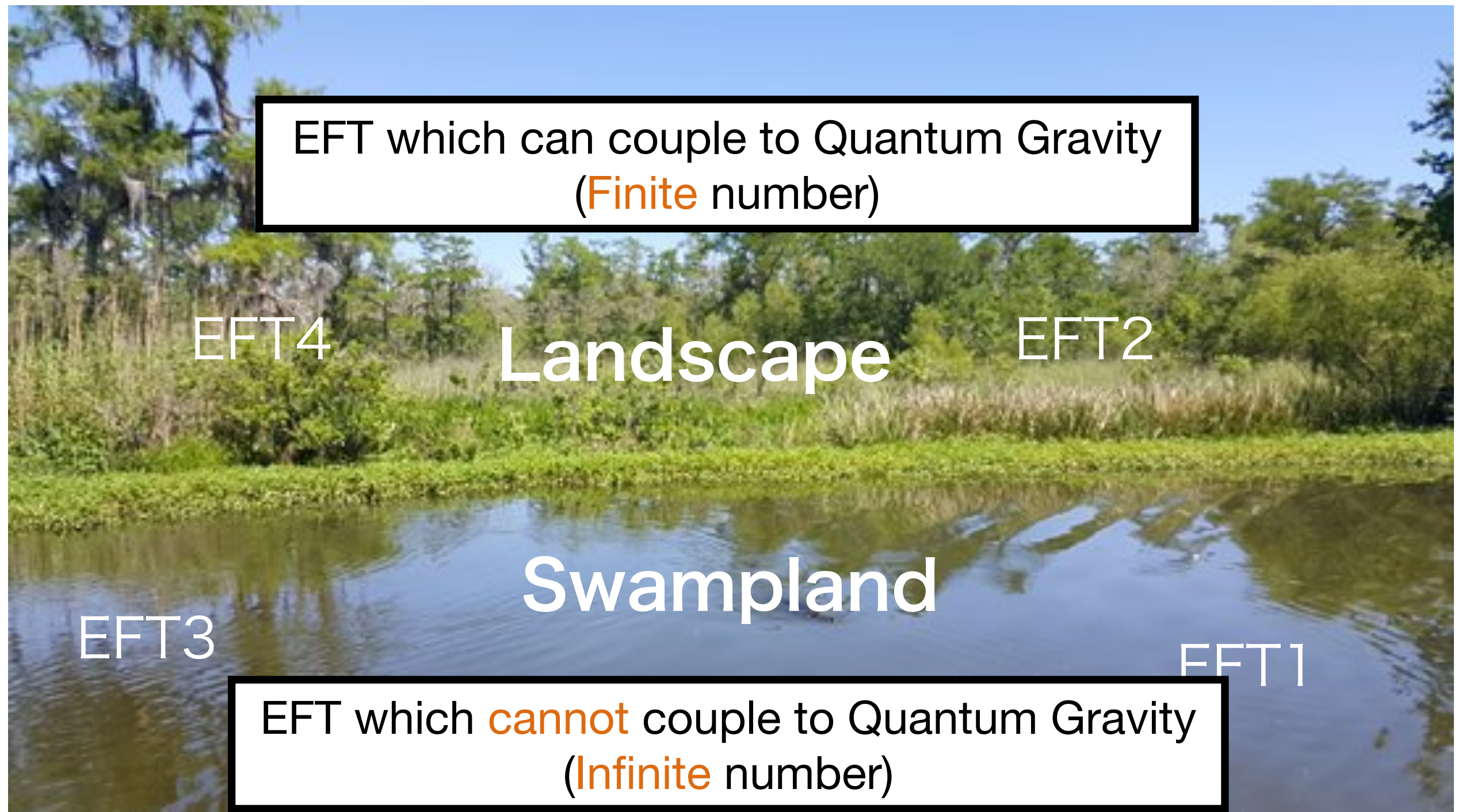
Even though the number of vacua is huge,
it is still **finite**!

This is remarkable since **the number of EFT is infinite**.

For example, There are infinite number of $SU(N)$
gauge theory parametrized by $N = 2, 3, 4, \dots$.

This leads to the notion of
the **Landscape** and the **Swampland**.

Landscape vs Swampland

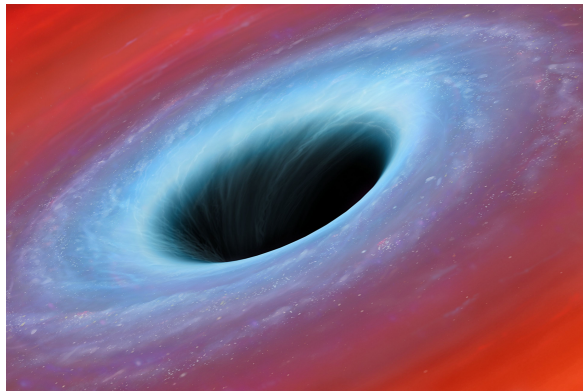


Q: What is the boundary between
the Landscape and the Swampland?

Swampland Conjectures

There are hidden conditions for healthy EFT.

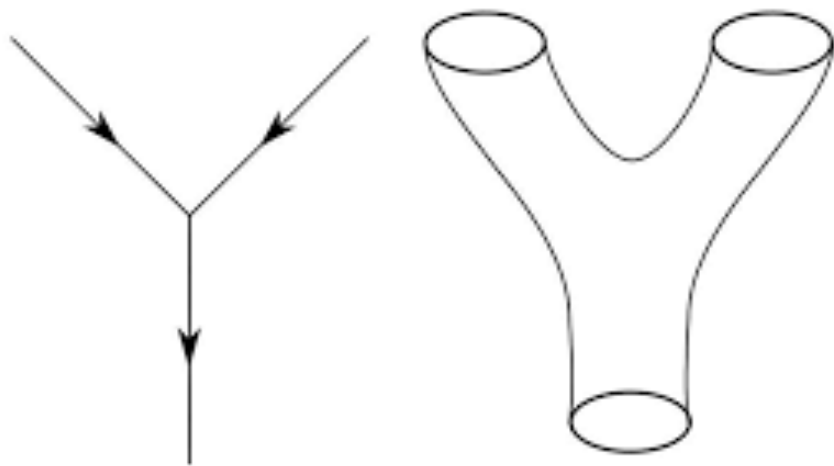
Talk Plan



Motivated from Black Hole (BH)

$$S_{BH} = A/4, \quad A: \text{BH area.}$$

No Global Symmetry Conjecture Generalization → Weak Gravity Conjecture



Motivated from String Theory

Distance Conjecture
de Sitter Conjecture

Talk Plan

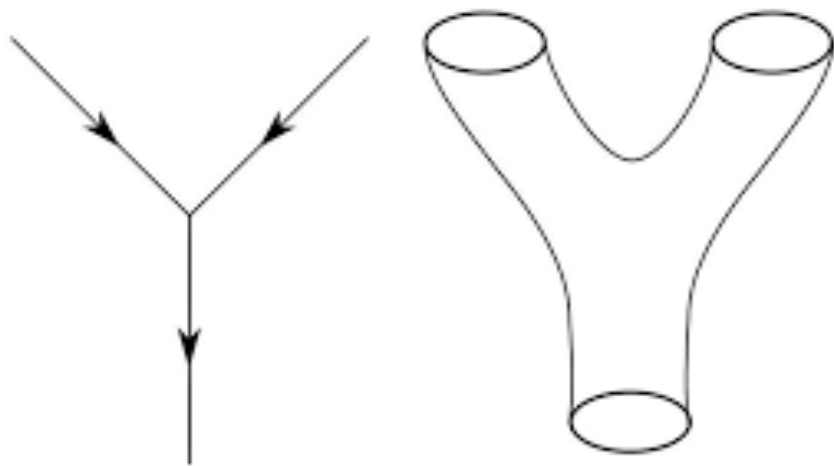


Motivated from Black Hole (BH)

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Generalization

No Global Symmetry Conjecture  Weak Gravity Conjecture



Motivated from String Theory
Distance Conjecture
de Sitter Conjecture

No Global Symmetry

Statement: No Global Symmetry in QG.

[..., [Banks-Dixon '88](#), ..., [Banks-Seiberg '10](#), ..., [Harlow-Ooguri '18](#), ...]

Perturbative string

BH

Holography

There are no discrete and continuous global symmetries.

For example, there are no \mathbb{Z}_N and $SU(2)$ global symmetries.

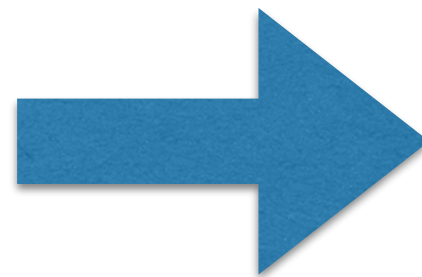
The Conjecture also applies to new notion of symmetry such as higher form symmetry and non-invertible symmetry.

The global symmetry at the boundary of the spacetime is OK.
(e.g. AdS/CFT)

Relation to Black Hole

Suppose there is $SU(2)$ global symmetry.

By throwing $\text{Spin } J$ matter into BH,
the BH with an arbitrarily $SU(2)$ charge is
constructed.



Hawking radiation

Distant observer cannot distinguish
 $SU(2)$ charge. The number of
indistinguishable state contributes to
entropy, but $e^{S_{BH}}$ is finite.



$$S_{BH} = A/4.$$

A : BH area.

Solutions

Solution(1) **Explicit braking.**

There are no global symmetries.

Solution(2) **Gauging**

The distance observer can see the black hole charge through the electric field.

$$B - L$$

The Standard Model possesses global $B - L$ symmetry.

(1) Explicitly broken

The left-handed neutrino Majorana mass term (after turning on)

$$\mathcal{L} = \frac{1}{\Lambda} L H L H + \dots$$

This breaks from $U(1)_{B-L}$ to \mathbb{Z}_2 .

(2) Gauging

The SM is extended in such a way that $U(1)_{B-L}^3$ anomaly is canceled.

Typically, we add 3 right-handed neutrinos.

Strong CP problem

QCD action is

$$S \sim \int d^4x \left(-F_{\mu\nu} F^{\mu\nu} + \theta F_{\mu\nu} \tilde{F}^{\mu\nu} \right)$$

Experimental constraint is $\theta \lesssim 10^{-10}$.

An explanation is given by QCD axion a .

Lagrangian is

$$S \sim \int d^4x \left((\partial_\mu a)^2 - F_{\mu\nu} F^{\mu\nu} + \frac{a}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu} \right)$$

EOM for axion requires

$$\frac{\delta}{\delta a} Z \sim \langle F_{\mu\nu} \tilde{F}^{\mu\nu} \rangle = 0 \quad \rightarrow \quad \theta = 0.$$

Axion quality problem

Axion is Nambu-Goldstone boson of chiral symmetry $U(1)_{PQ}$ associated with symmetry breaking by $\langle \Phi \rangle$. Φ : $U(1)_{PQ}$ charged scalar

$U(1)_{PQ}$ symmetry is broken only through $U(1)_{PQ}SU(3)_C^2$ anomaly.

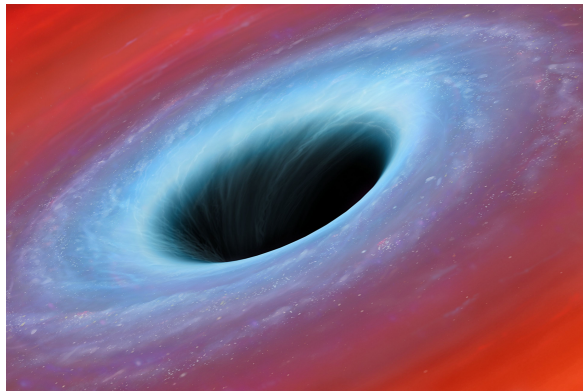
However, according to no global symmetry conjecture, one may expect $U(1)_{PQ}$ breaking term.

$$\mathcal{L} \sim \frac{\Phi^5}{M_P}$$

This spoils axion solution with $\langle \Phi \rangle \sim 10^{10}$ GeV (value preferred from cosmology).

$U(1)_{PQ}$ must be “good” symmetry even in the presence of the gravity.

Talk Plan

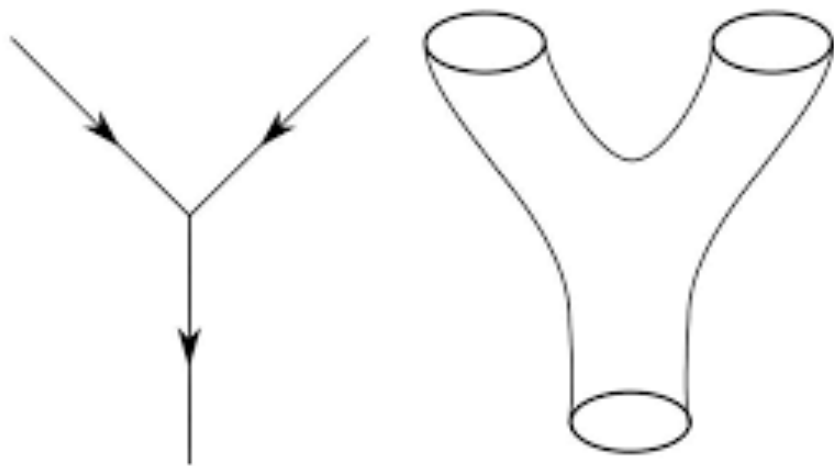


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Generalization

No Global Symmetry Conjecture  **Weak Gravity Conjecture**



Motivated from String Theory

Distance Conjecture
de Sitter Conjecture

Weak Gravity Conjecture (WGC)

Statement:

For $U(1)$ gauge group, there exists **at least** one **charged state** which satisfies (in $2M_{\text{Pl}}^2=1$ unit)

$$|Q| \geq M$$

(M, Q): mass and $U(1)$ charge of the state.

The magnetic version is $|Q_M| \geq m_M$.

(m_M, Q_M): monopole mass and $U(1)$ magnetic charge.

Why WGC is true?

Original motivation: Decay of Extremal BH. [[ArkaniHamed-Motl-Nicolis-Vafa '06](#)]

No counterexample in string theory.

Explanation from unitarity and causality in photon-photon scattering amplitude.

Extremal BH is a state satisfying WGC.

[[Hamada-Noumi-Shiu '18](#)]

Argument from Holography [[Montero '18](#)]

Non-SUSY AdS conjecture

- Conjecture1:

Except for BPS state, gravity is **strictly** weakest force. $|Q| > M$.



[Maldacena, Michelson, Strominger '98]

All non-SUSY AdS vacua supported by flux are unstable.

AdS vacuum

AdS with
less flux

- Conjecture2: All non-SUSY AdS vacua are unstable.

(as long as low energy action is Einstein gravity with finite number of fields)

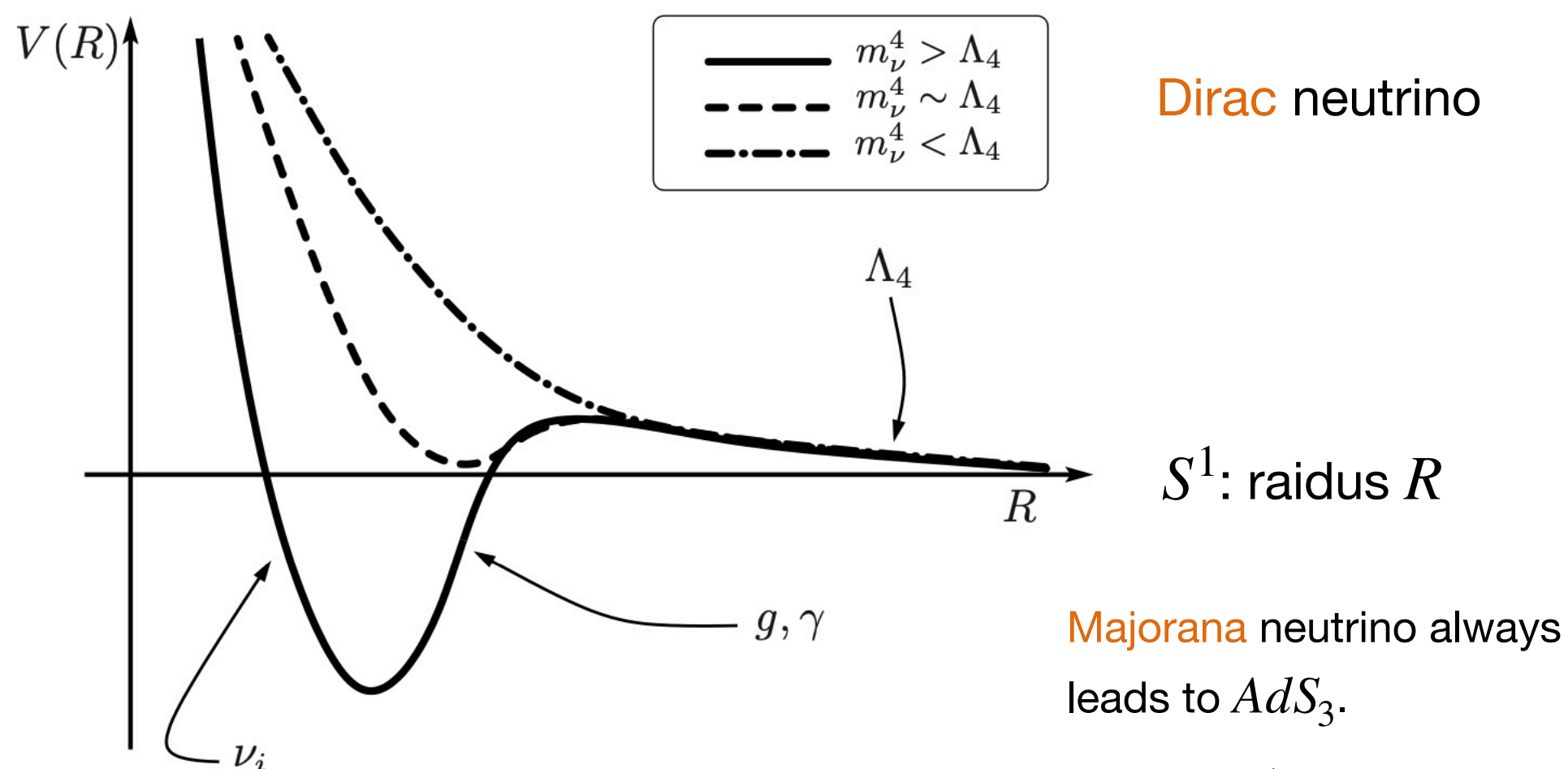
Motivation: All known construction from M/string theory,
AdS is supported by some flux.

AdS vacuum in SM

Idea: The conjecture applies all theories in Landscape.

Assumption: SM is in Landscape.

Then, it is likely that S^1 compactification of SM is in Landscape.

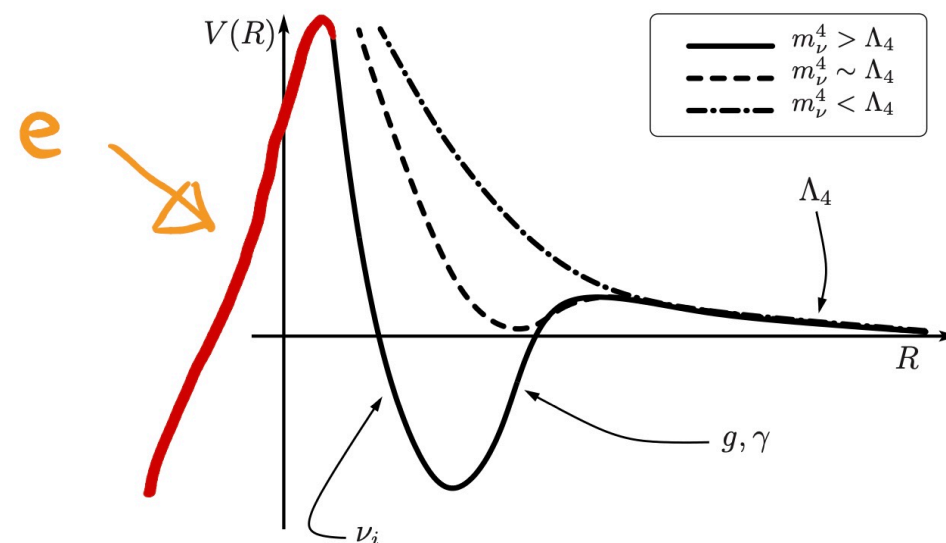


Depending on neutrino mass and type (Dirac/Majorana), $AdS_3 \times S^1$ appears.

Neutrino Mass

If this vacuum is stable, this is in the Swampland [[Ooguri, Vafa '16](#),
[Ibanez, Martin-Lozano, Valenzuela '17](#)]

$AdS_3 \times S^1$ vacuum is non-perturbatively unstable [[Hamada-Shiu '17](#)]



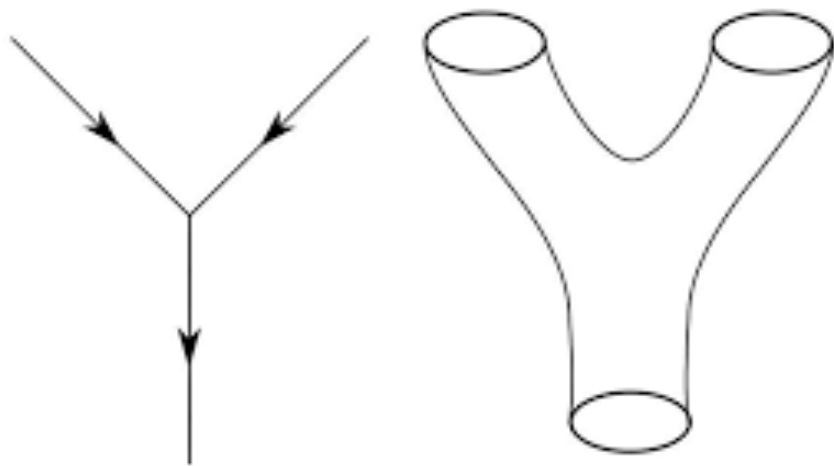
Attempts to constraint neutrino mass and type by using more complicated compactification and different conjectures. [[Gonzalo-Herraez-Ibanez '18](#), [Gonzalo-Ibanez-Valenzuela '21](#)]

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$$S_{BH} = A/4, \quad A: \text{BH area.}$$

No Global Symmetry Conjecture $\xrightarrow{\text{Generalization}}$ Weak Gravity Conjecture



Motivated from String Theory

Distance Conjecture

de Sitter Conjecture

Distance Conjecture

The Lagrangian of the massless scalar field is

$$\mathcal{L} = \frac{1}{2} \eta^{\mu\nu} g_{IJ} (\partial_\mu \phi^I) (\partial_\nu \phi^J)$$

g_{IJ} is called field space metric. The field space distance is defined

from g_{IJ} . (distance from ϕ_0 to ϕ_1 with path A) $= \int_{\phi_0}^{\phi_1} ds, \quad ds^2 = g_{IJ} d\phi^I d\phi^J$

Statement: At large geodesic distance $\Delta\phi \rightarrow \infty$, the exponentially light tower of state appears.

$$M_{\text{tower}} \sim M_P e^{-n\alpha\Delta\phi}, \quad \text{for } \Delta\phi \rightarrow \infty, \quad n = 1, 2, \dots$$

where α is $\mathcal{O}(1)$ positive number.

Two Towers

Limit 1: KK tower

$D = d + 1$ dimensional spacetime compactified on S^1 .

The radius R corresponds to the radion field ϕ .

$$2\pi R = e^{\sqrt{\frac{d-2}{2(d-1)}}\phi}, \quad M_{KK}^2 \sim e^{-\sqrt{\frac{2(d-1)}{d-2}}\phi}.$$

For $\phi \rightarrow \infty$, d -dimensional EFT breaks down.

Limit 2: String tower

The relation between dilaton field ϕ (string coupling e^ϕ) and string scale M_{st} is

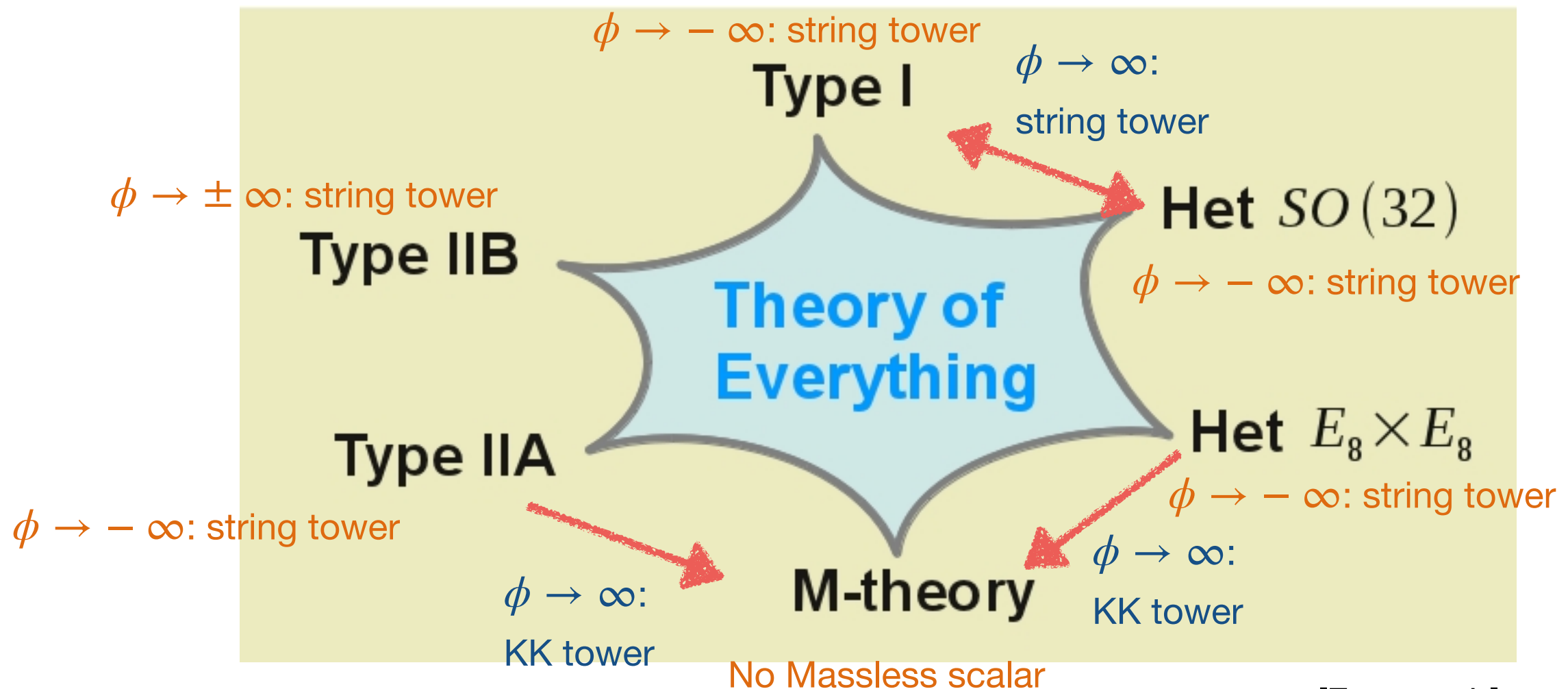
$$M_P^8 = M_{st}^8 e^{-2\phi} \text{ in 10d.}$$

In $\phi \rightarrow \infty$ limit with fixed M_P , the string excited states become light.

Emergent String Conjecture: These two are only possibilities. [[Lee-Lerche-Weigand '19](#)]

Examples in String Theory

Dilaton ϕ (String coupling e^ϕ)



[From [web](#)]

Inflation

The dynamics of inflaton may be modified if (cutoff scale) < (Hubble scale).

$$H \lesssim M_P e^{-\alpha \Delta\phi/M_P}, \quad \frac{\Delta\phi}{M_P} \lesssim \frac{1}{\alpha} \log \left(\frac{M_P}{H} \right)$$

$\Delta\phi$ is bounded from above for fixed H .

On the other hand, Lyth bound [Lyth '96] is lower bound on $\Delta\phi$ for fixed H .

$$10^5 \frac{H}{M_P} \lesssim \frac{\Delta\phi}{M_P}$$

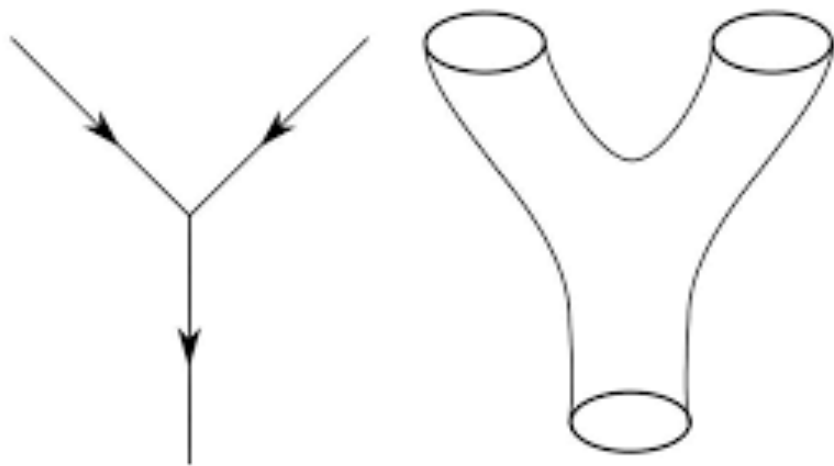
Therefore,
$$\frac{H}{M_P} \lesssim \frac{10^{-5}}{\alpha}.$$

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Motivated from String Theory

Distance Conjecture

de Sitter Conjecture

de Sitter Conjecture

Statement: Potential $V(\phi)$ must satisfy either

$$|\nabla V| \geq \frac{c}{M_P} V \quad \text{or} \quad \min(\nabla_i \nabla_j V) \leq -\frac{c'}{M_P^2} V,$$

where c and c' are $\mathcal{O}(1)$ positive numbers.

The conjecture excludes de Sitter vacua because

$|\nabla V| = 0$ and $\min(\nabla_i \nabla_j V) > 0$ are impossible.

$SO(16) \times SO(16)$ Heterotic String

$SO(16) \times SO(16)$ heterotic string: 10d theory without supersymmetry nor tachyon.

Tree level cosmological constant is zero. The one-loop cosmological constant is computed as

$$\Lambda_{10} \simeq 4 \times 10^{-6} (\alpha')^{-5} \quad (\alpha')^{-1}: \text{string tension.}$$

Positive cosmological constant (fermion/boson gives rise positive/negative contribution).

de Sitter solution in string theory?

Runaway Potential

This is **NOT** de Sitter solution.

String frame action is

$$S = (\alpha')^{-4} \int d^{10}x \sqrt{g} e^{-2\phi} \left(\frac{1}{2} R + 2(\nabla \phi)^2 - (\alpha')^4 \Lambda_{10} + \dots \right)$$

ϕ is dilaton ($g_s = e^\phi$ is string coupling). Einstein frame action is

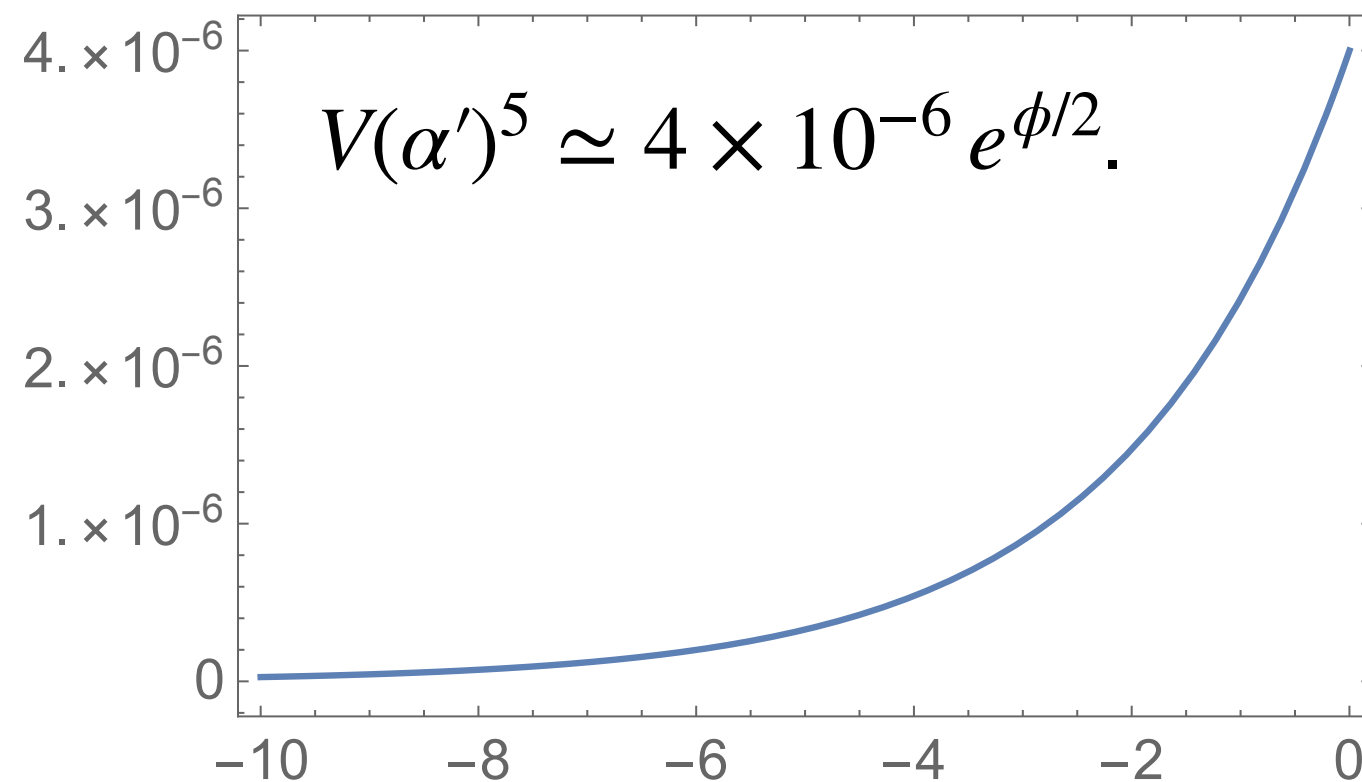
$$S = \int d^{10}x \sqrt{g} \left(R + \frac{1}{2}(\nabla \phi)^2 - \Lambda_{10} e^{\phi/2} + \dots \right)$$

The potential is $V = \Lambda_{10} e^{\phi/2}$.

$$V = \Lambda_{10} e^{\phi/2}$$

Einstein frameでのdilaton potential:

$$V = \Lambda_{10} e^{\phi/2} \simeq 4 \times 10^{-6} (\alpha')^{-5} e^{\phi/2}.$$



Weak coupling

ϕ

Strong coupling

Runaway potential to
 $g_s = e^{\phi} \rightarrow 0$.

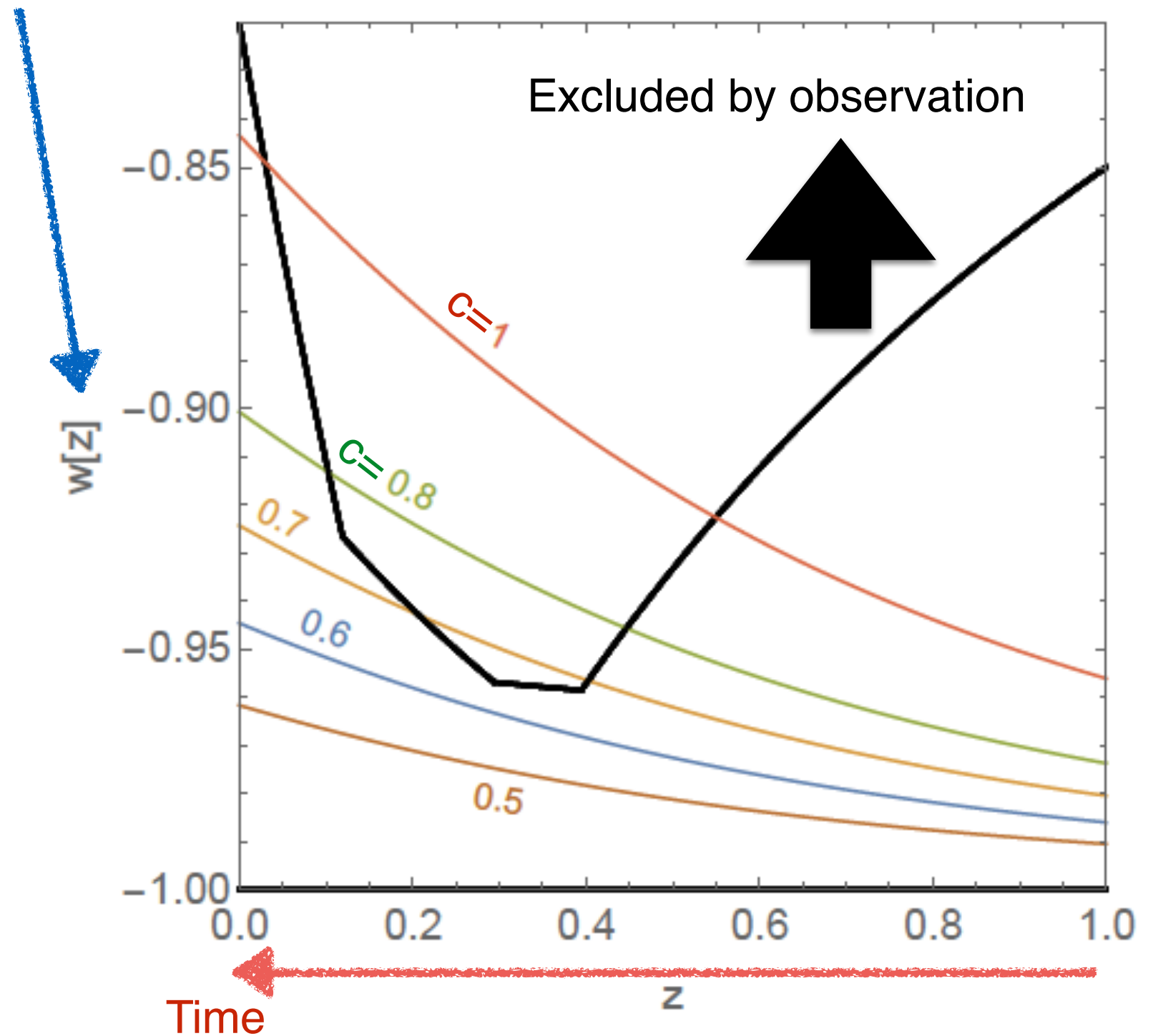
Constraint

Equation of state, $p=w\rho$

[Agrawal-Obied-Steinhardt-Vafa '18]

$$|\nabla V| \geq \frac{c}{M_P} V.$$

制限は $c < 0.6$.



Summary

The study of BH and string theory implies the number of Swampland Conjectures.

- No Global Symmetry Conjecture
- Weak Gravity Conjecture
- Distance Conjecture
- de Sitter Conjecture