

Based on 2012.11576
in collaboration with Fuminobu Takahashi

Kilobyte cosmic birefringence and ALP domain walls without strings

Birefringence (複屈折)



Tohoku University
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Online seminar at E-lab on 19th April 2021

<https://ja.wikipedia.org/wiki/複屈折>

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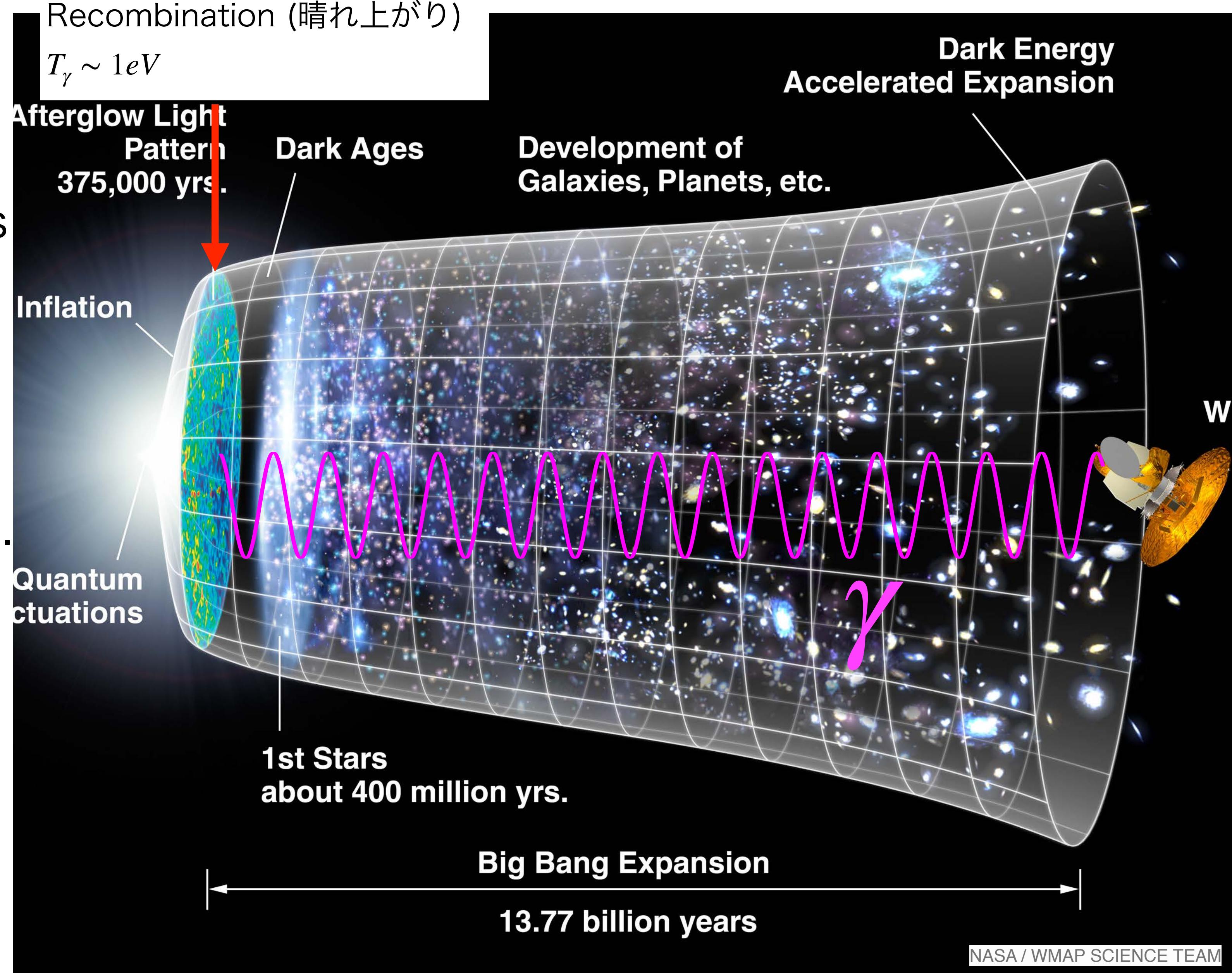
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- 2. ALP domain wall without a string
- 3. Kilobyte cosmic birefringence
- 4. Conclusions

- 1 Introduction

Cosmic Birefringence
(experimental side)

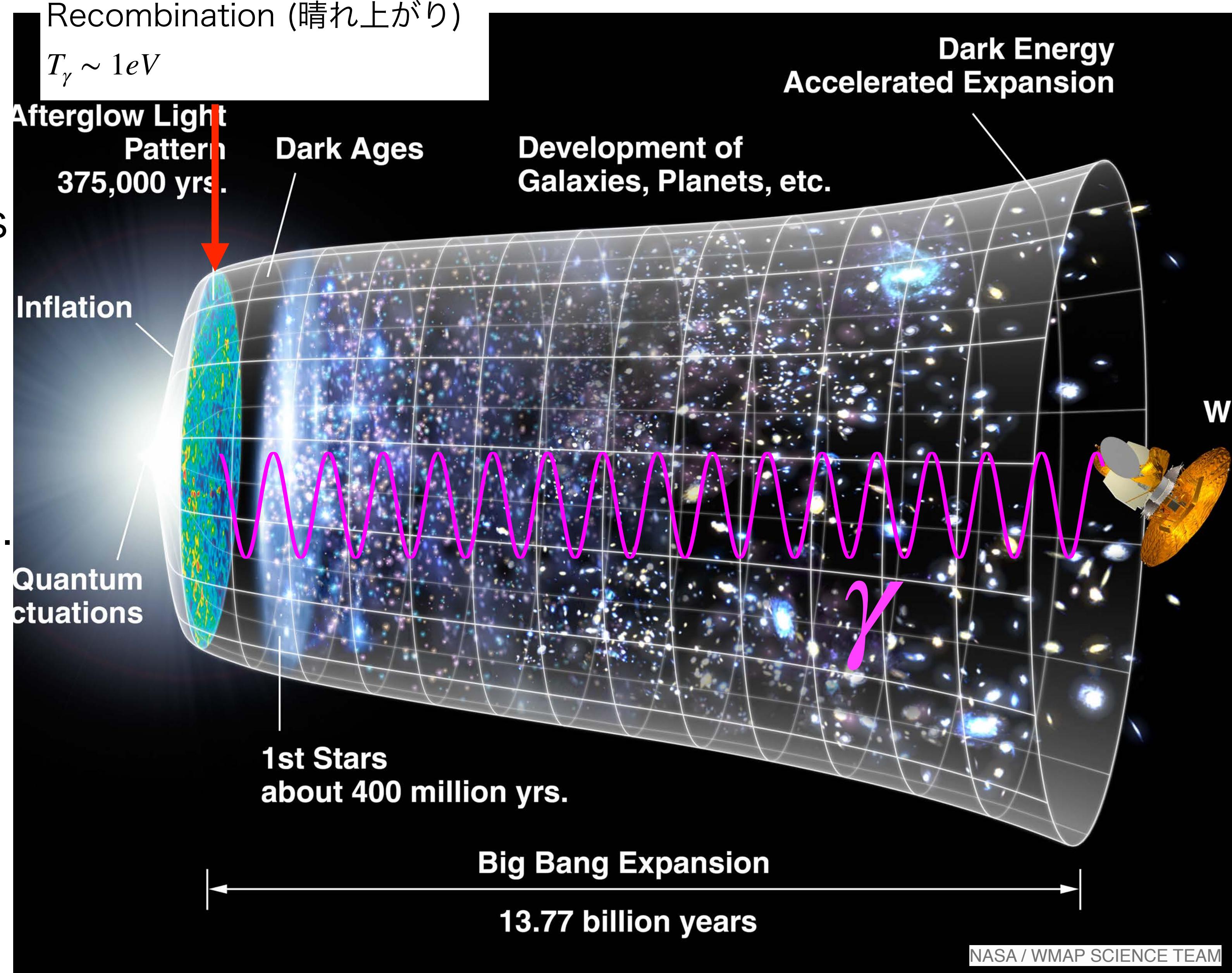
Cosmology and photons from recombination.

- Before recombination, photons are in thermal equilibrium.
- CMB photons ($E_\gamma \lesssim 1\text{eV}$) freely propagate after recombination.
- Last scattered photons are messengers of early Universe with $T \leq 1 \text{ eV}$.

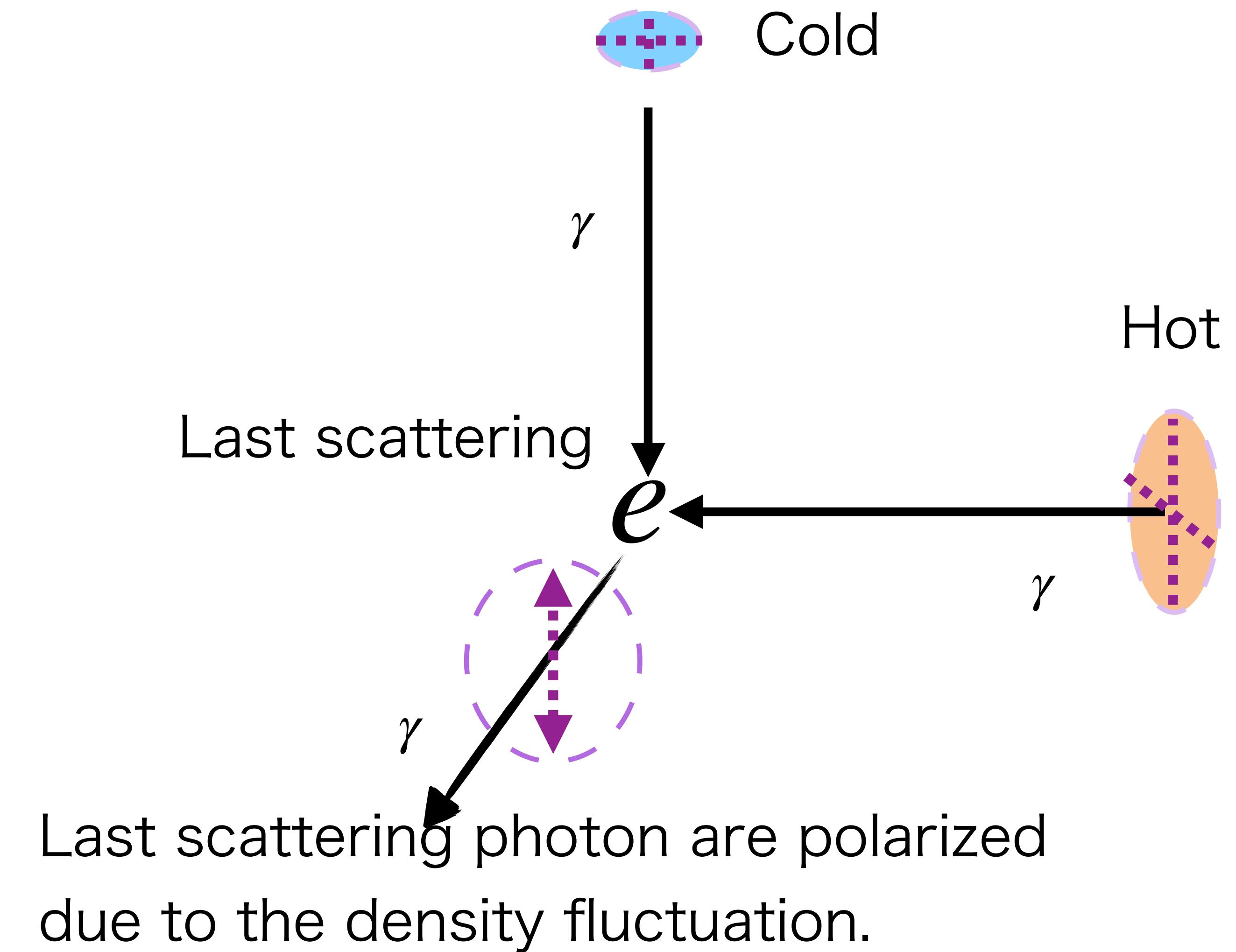
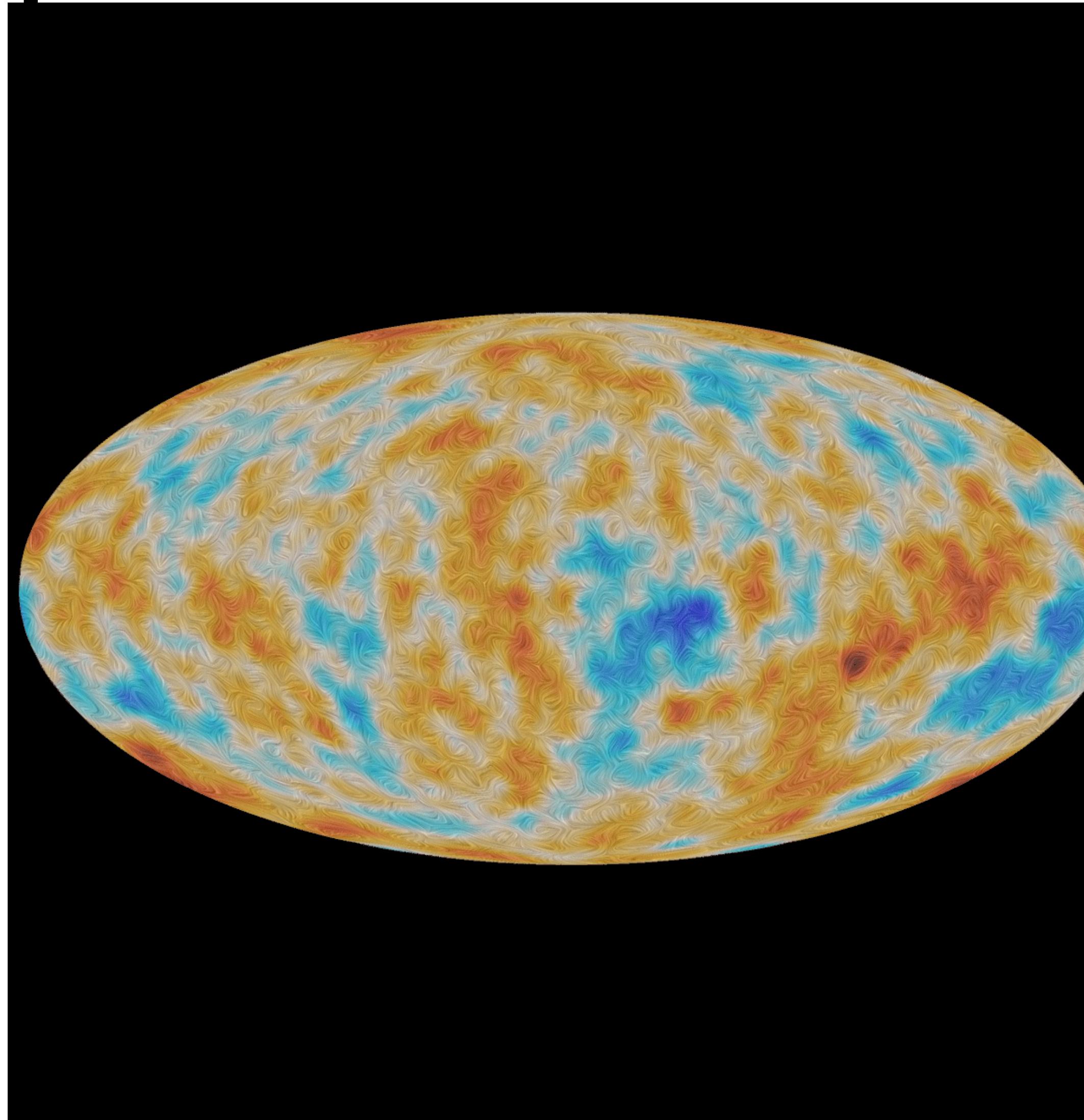


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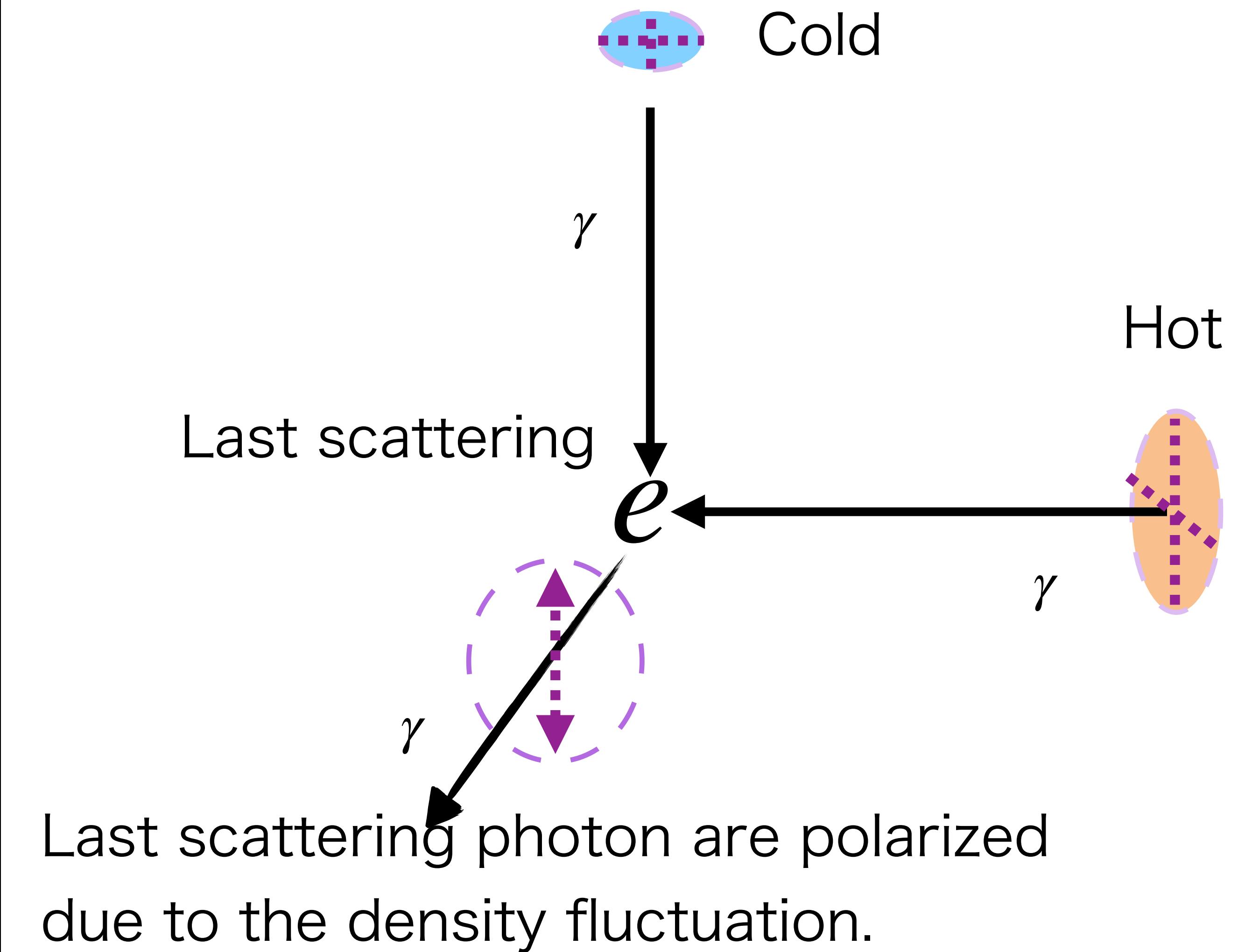
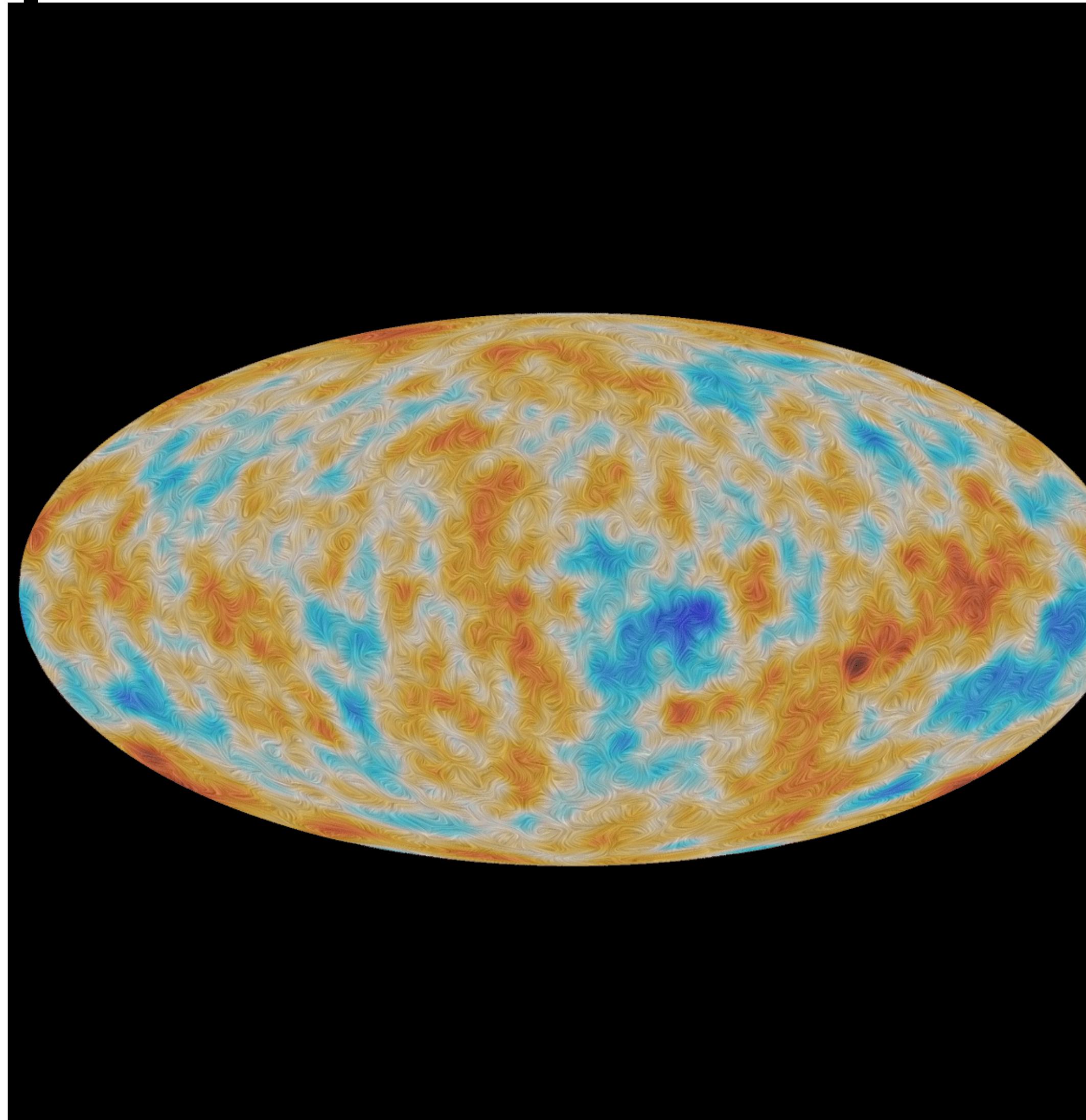
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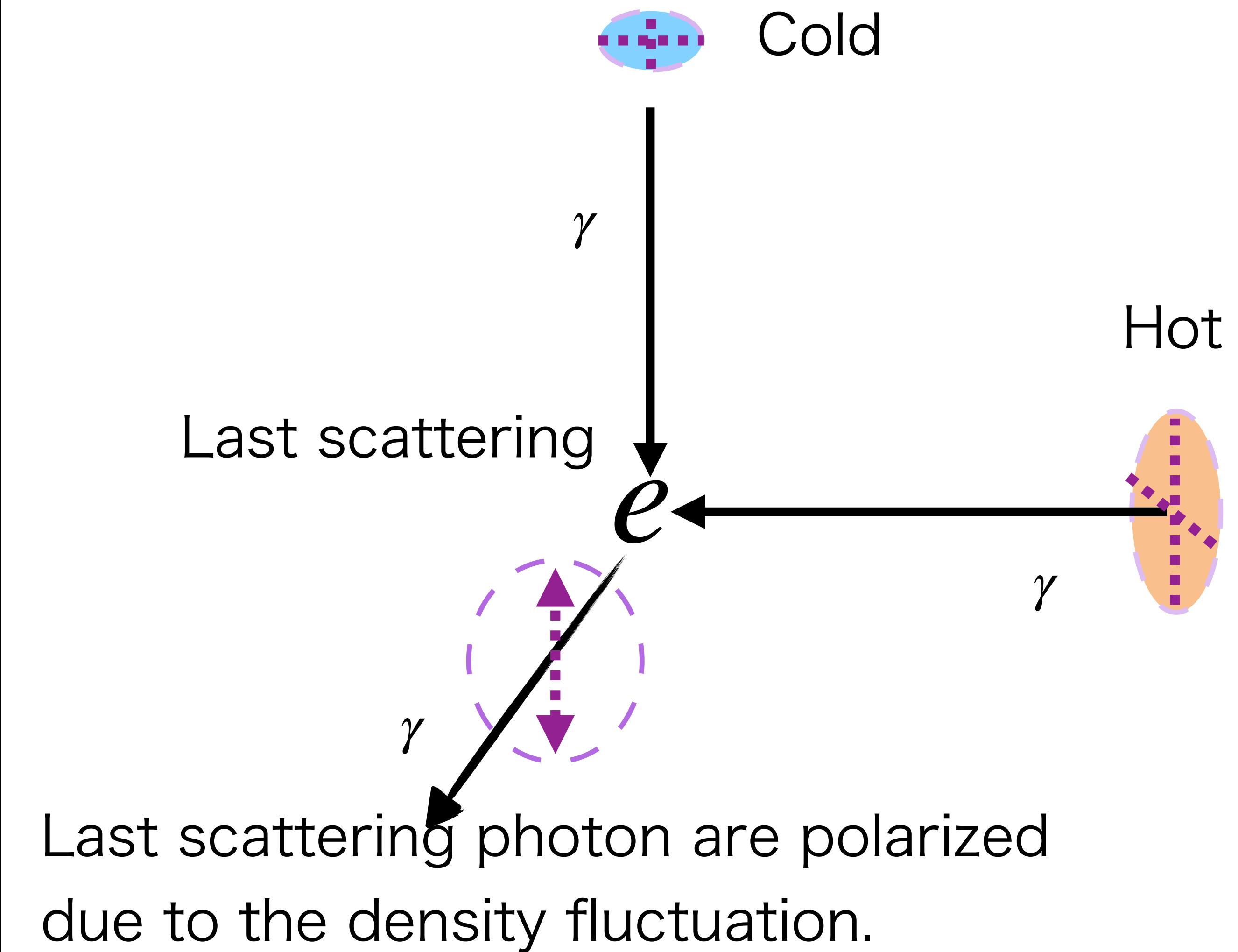
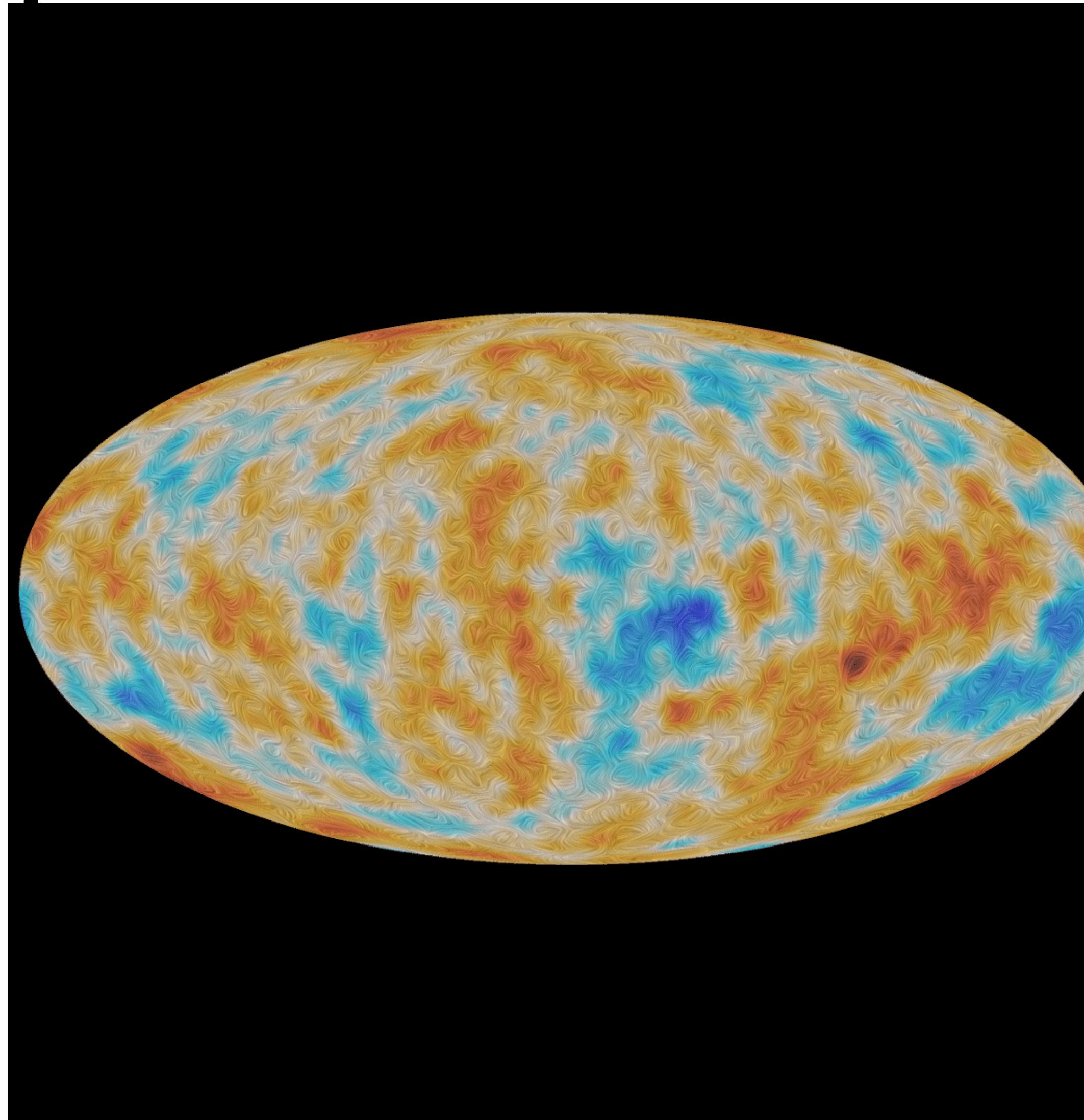
Temperature fluctuation and polarization of photon.



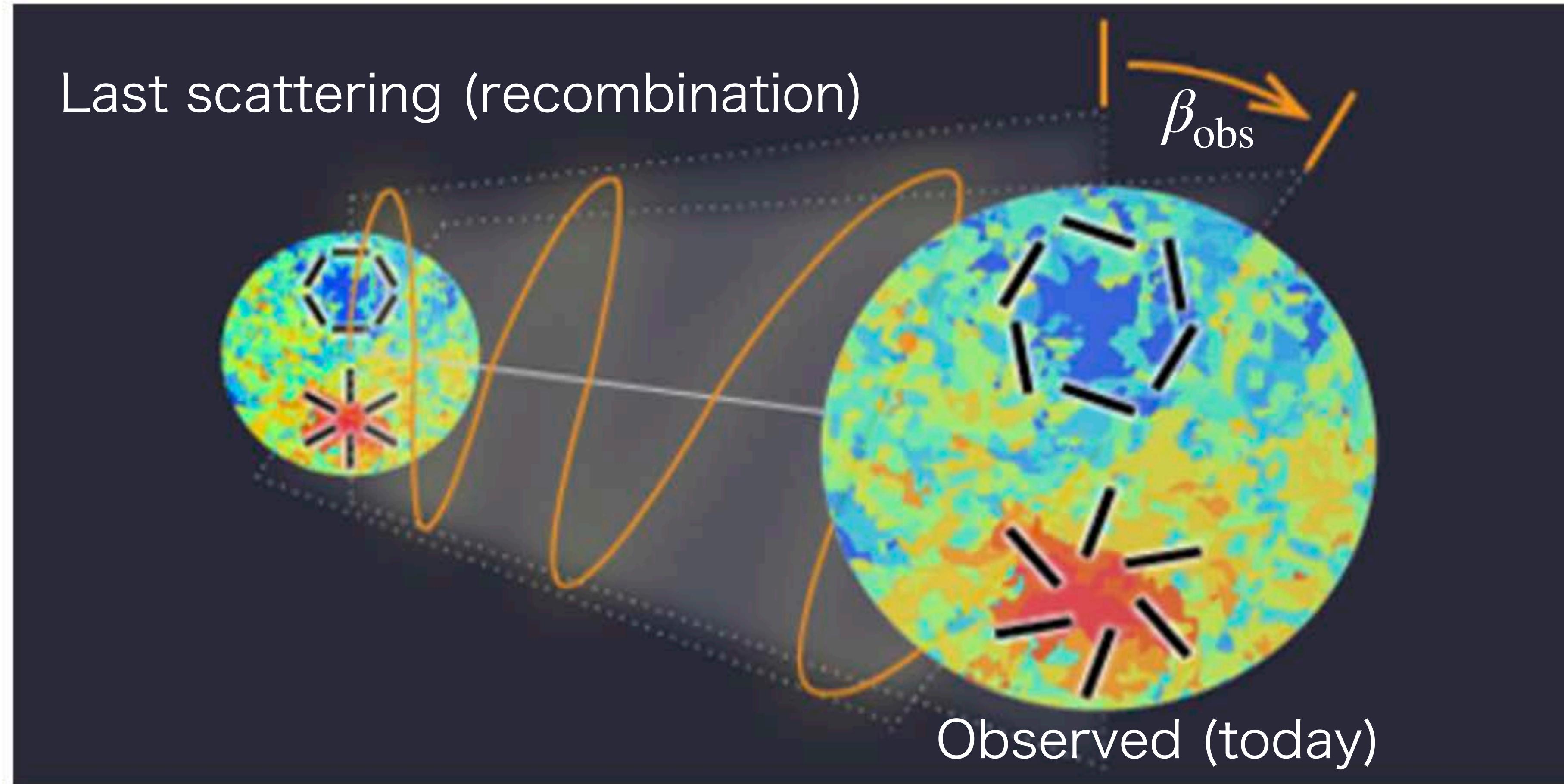
Temperature fluctuation and polarization of photon.



Temperature fluctuation and polarization of photon.



A new analysis is recently performed to get a parity-violating isotropic cosmic birefringence (CB) from Planck2018 data.



$$\beta_{\text{obs}} = 0.35 \pm 0.14 \text{ deg}, \quad (2.4 \sigma)$$

Minami and Komatsu, 2011.11254

See also for the development of the analysis [Minami et al,1904.12440](#), [2002.03572](#), [2006.15982](#).

Y. Minami/KEK

(If the isotropic CB is true,)

What is the “crystal” in the Universe
causing the birefringence?

- It couples to photon.
- It violates the parity.

- 1 Introduction

Cosmic Birefringence
(Theory side)

How to violate parity in electromagnetic theory?

$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} - c_\gamma \frac{\alpha}{4\pi}\theta[x, t]F_{\mu\nu}\tilde{F}^{\mu\nu}$$

How to violate parity in electromagnetic theory?

$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} - c_\gamma \frac{\alpha}{4\pi} \frac{\phi}{f_\phi} F_{\mu\nu} \tilde{F}^{\mu\nu}$$

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A simple model has an axion-Like Particle (ALP)

Cosmic Birefringence by Axion-Like Particle (ALP)

Carroll, Field, Jackiw, 1990; Harari, Sikivie, 1992; Carroll, 1998;

$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} - c_\gamma \frac{\alpha}{4\pi} \frac{\phi}{f_\phi} F_{\mu\nu}\tilde{F}^{\mu\nu}$$

$$= \frac{1}{2}(\vec{E}^2 - \vec{B}^2) - \frac{1}{4}g_{\phi\gamma\gamma}\phi(\vec{E} \cdot \vec{B})$$

$$\approx \frac{1}{2} \left[(\vec{E} + \frac{1}{2}g_{\phi\gamma\gamma}\phi\vec{B})^2 - (\vec{B} - \frac{1}{2}g_{\phi\gamma\gamma}\phi\vec{E})^2 \right]$$

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$$\boxed{\approx \frac{1}{2} \left[\underbrace{(\vec{E} + \frac{1}{2}g_{\phi\gamma\gamma}\phi\vec{B})^2}_{''D''} - \underbrace{(\vec{B} - \frac{1}{2}g_{\phi\gamma\gamma}\phi\vec{E})^2}_{''H''} \right]}$$

Cosmic Birefringence by Axion-Like Particle (ALP)

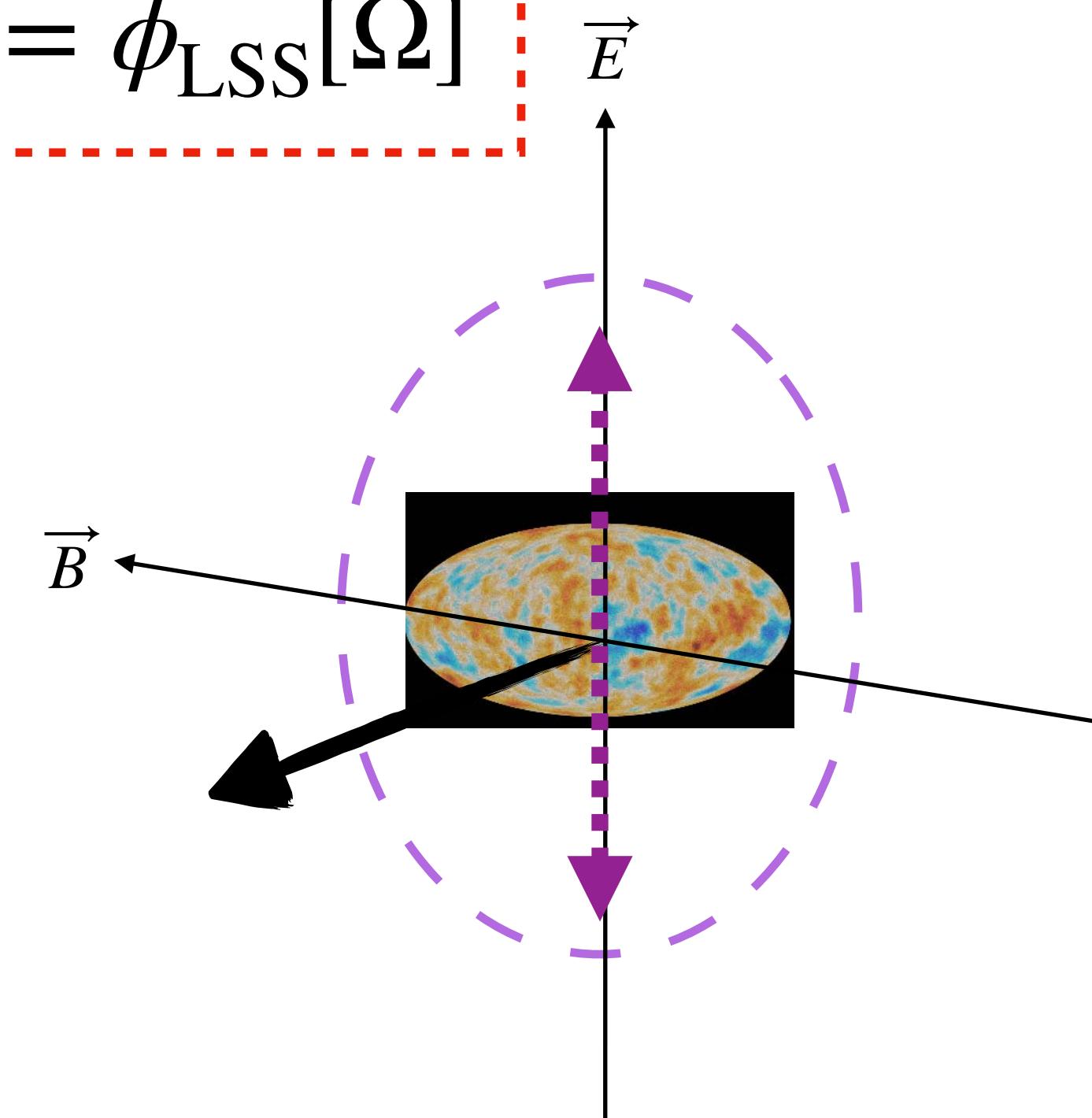
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$$\phi[\vec{x}_\gamma[t_{\text{rec}}], t_{\text{rec}}] = \phi_{\text{LSS}}[\Omega]$$



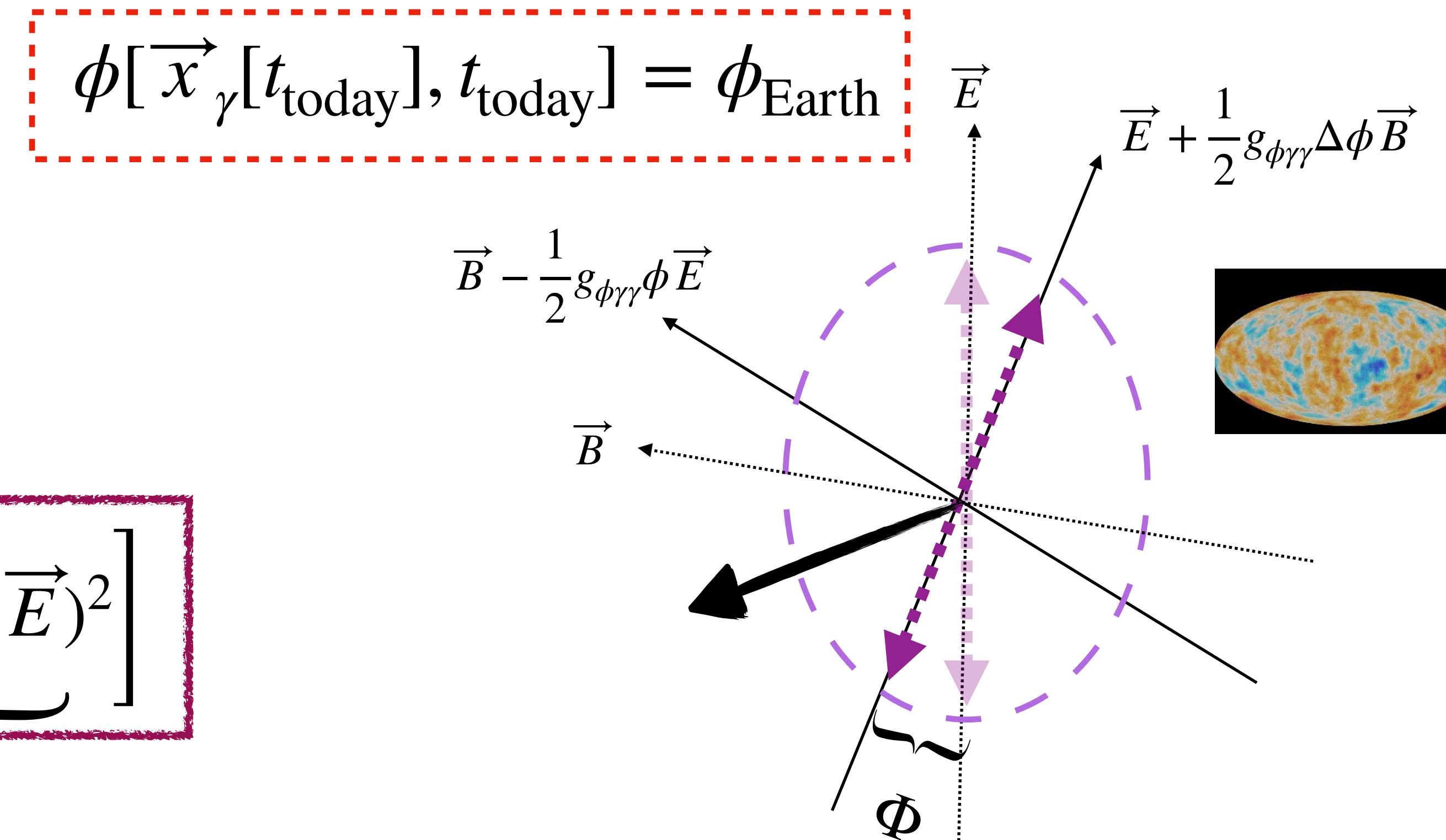
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(if ALP background changes adiabatically.)

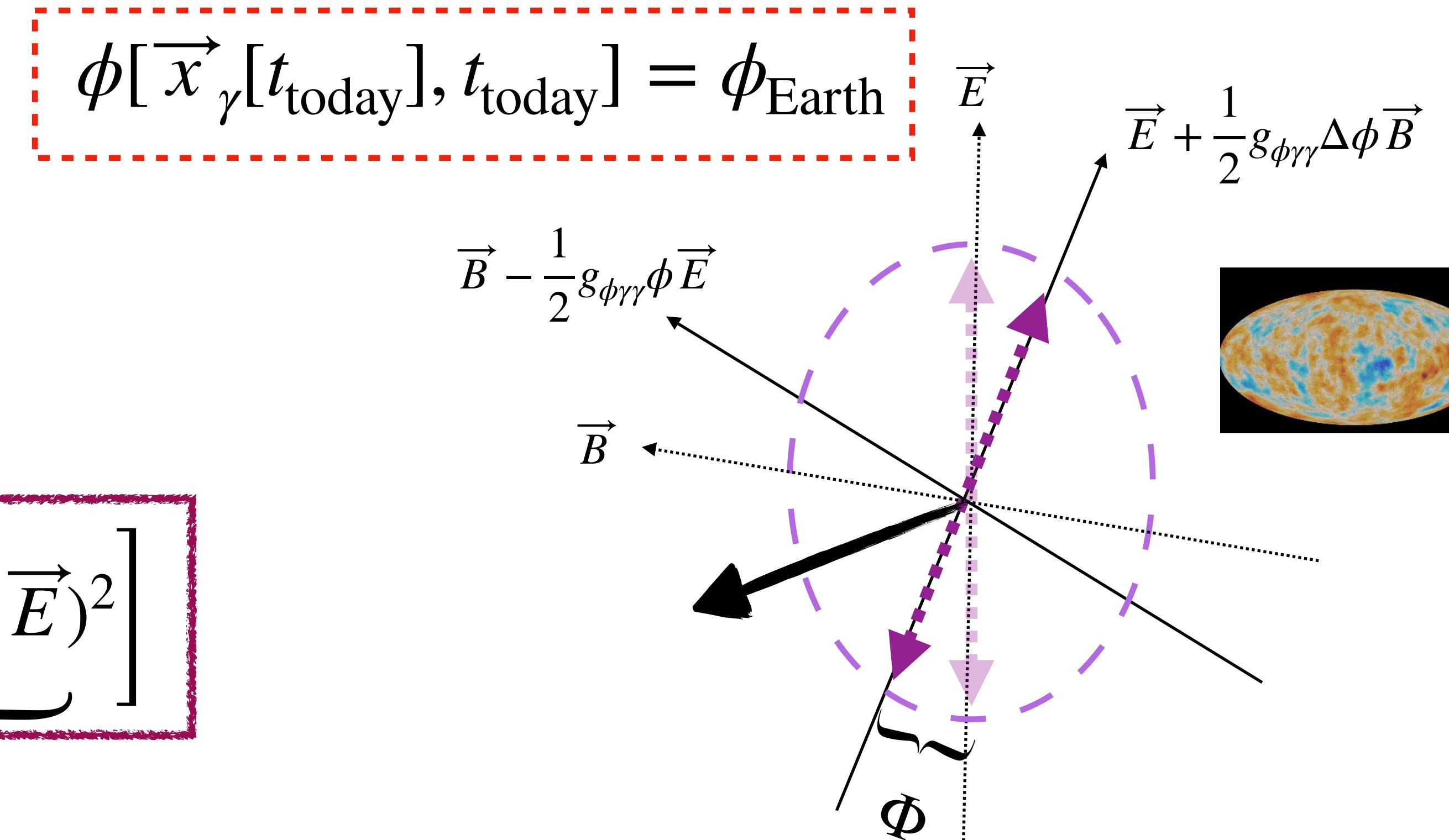
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(if ALP background changes adiabatically.)

$$\Phi(\Omega) = \frac{1}{2}g_{\phi\gamma\gamma} \int_{\text{LSS}}^{\text{today}} d\phi = 0.42 \text{ deg} \times c_\gamma \left(\frac{\phi_{\text{Earth}} - \phi_{\text{LSS}}(\Omega)}{2\pi f_\phi} \right),$$

$$\text{c.f. } \beta = \frac{1}{4\pi} \int d\Omega \Phi[\Omega]$$

Isotropic Cosmic Birefringence by ALP models

- Isotropic CB by $\dot{\phi} \neq 0$: Slow-rolling ALP

Minami and Komatsu, 2006.15982,

Fujita et al, 2011.11894, (CB and H_0 tension)

Mehta et al, 2103.06812, (Many ALPs)

Nakagawa et al, 2103.08153, (Very light ALP)

- Isotropic CB by $|\partial_{\vec{x}}\phi| \neq 0$: Domain walls

Takahashi, WY, 2012.11576, (CB by Domain wall)

This talk

Isotropic Cosmic Birefringence by ALP models

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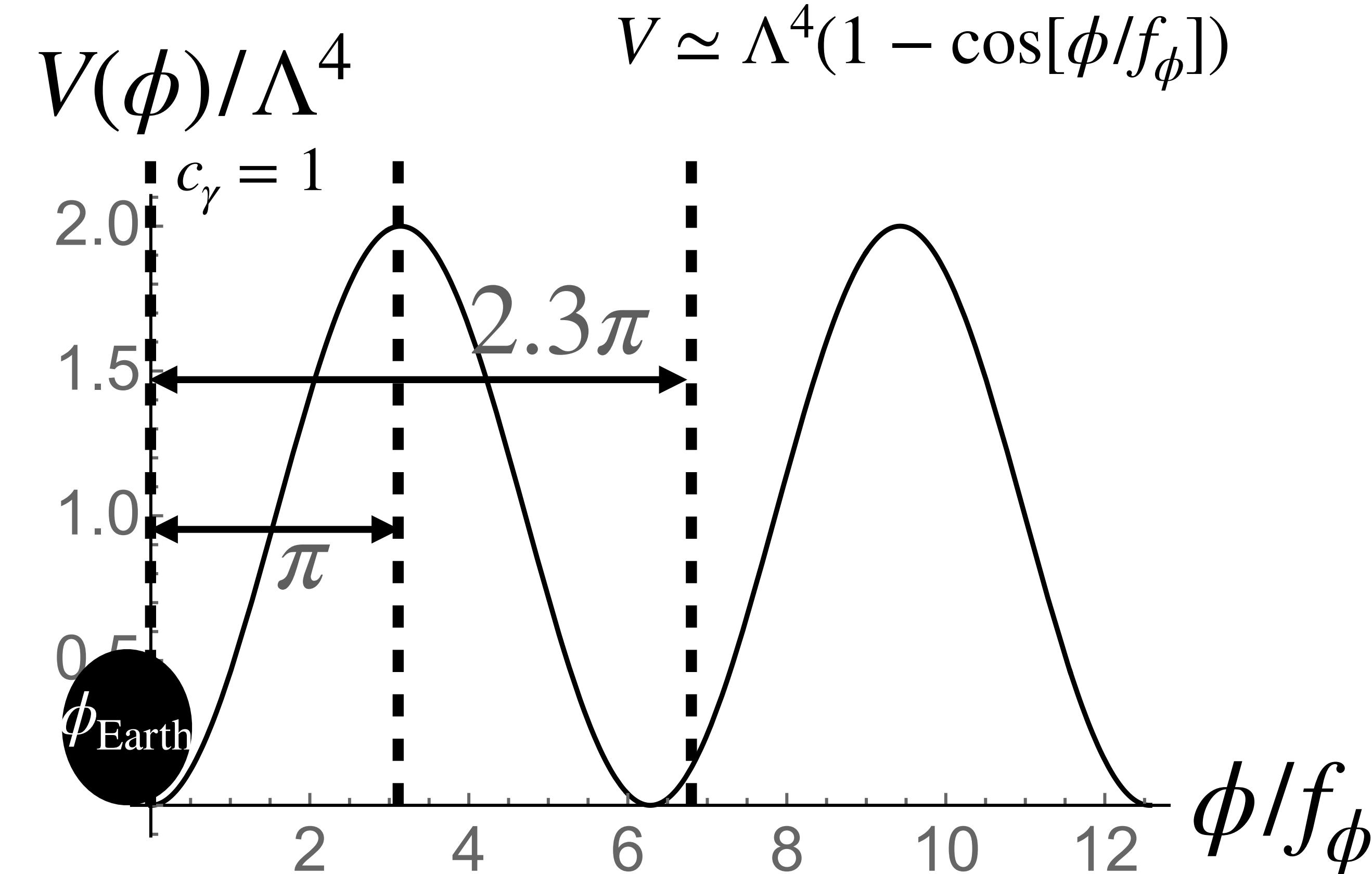
This talk

Why Cosmic Birefringence (CB) from Domain Wall?

$$\begin{aligned}\Phi(\Omega) &= \int_{\text{LSS}[\Omega]}^{\text{Today}} g_{\phi\gamma\gamma} d\phi/2 \\ &= 0.42 \text{ deg} \times c_\gamma \left(\frac{\phi_{\text{Earth}} - \phi_{\text{LSS}}(\Omega)}{2\pi f_\phi} \right), \\ \beta &= \frac{1}{4\pi} \int d\Omega \Phi[\Omega] \\ \beta_{\text{obs}} &= 0.35 \pm 0.14 \text{ deg},\end{aligned}$$

Minami and Komatsu, 2006.15982,

→ $c_\gamma \left(\frac{\phi_{\text{Earth}} - \bar{\phi}_{\text{LSS}}}{f_\phi} \right) \sim (\pi - 2.3\pi)$

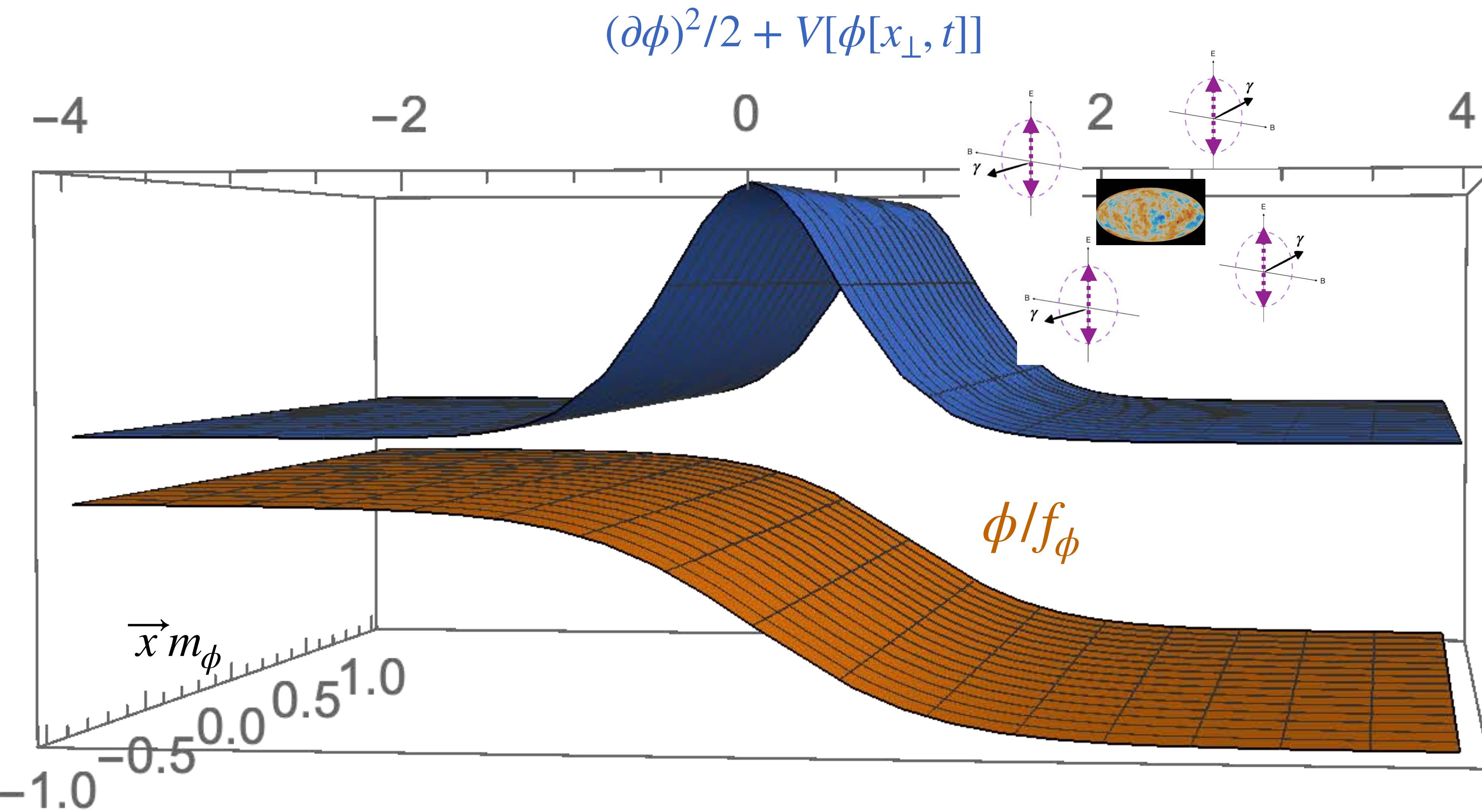


Photon emitted at recombination is likely to go through an ALP potential barrier.

→ The measured CB (and $c_\gamma \lesssim O(1)$) suggests a domain wall.

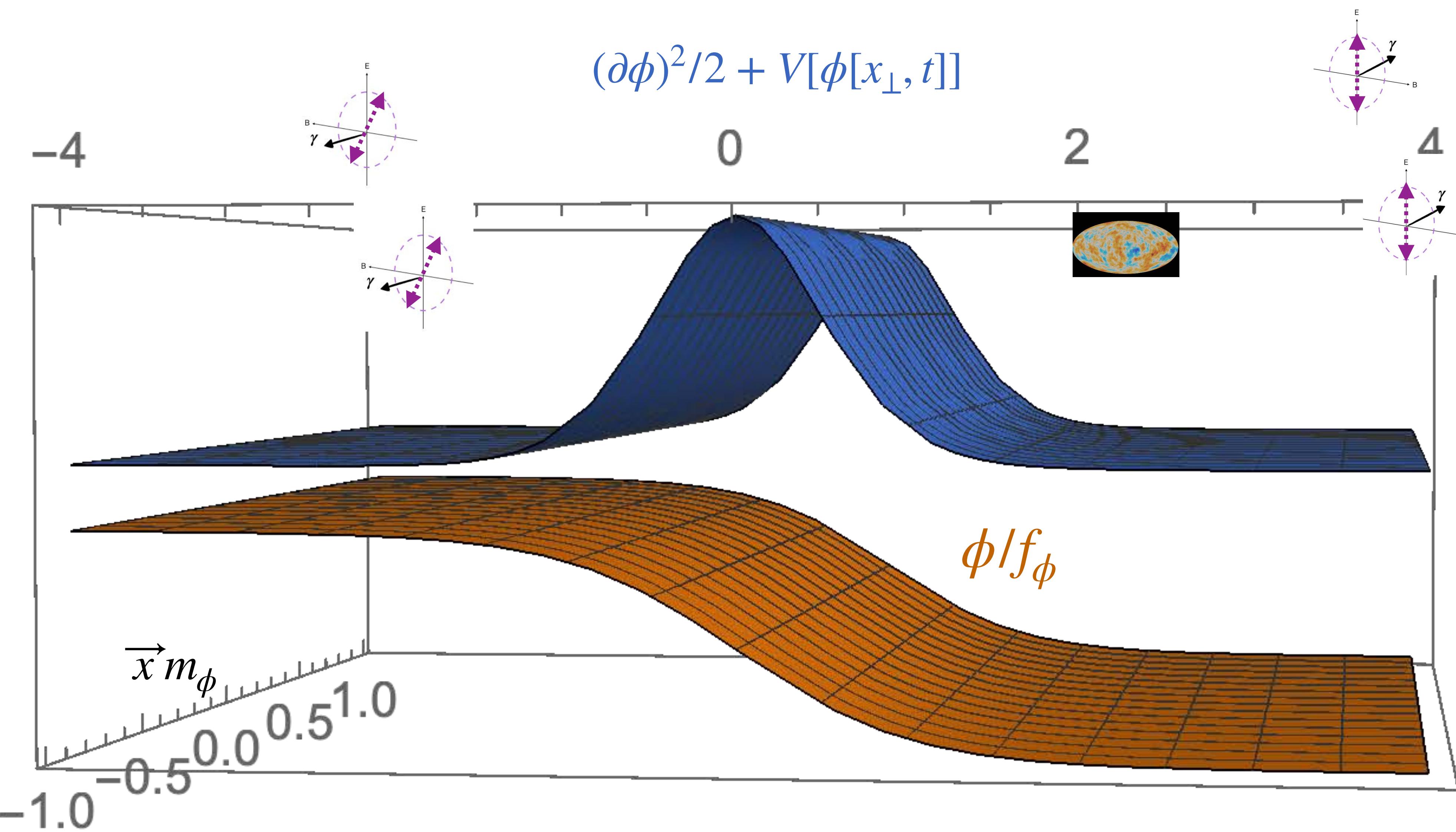
- CB by ALP domain walls

$$V \simeq \Lambda^4(1 + \cos[\phi/f_\phi])$$



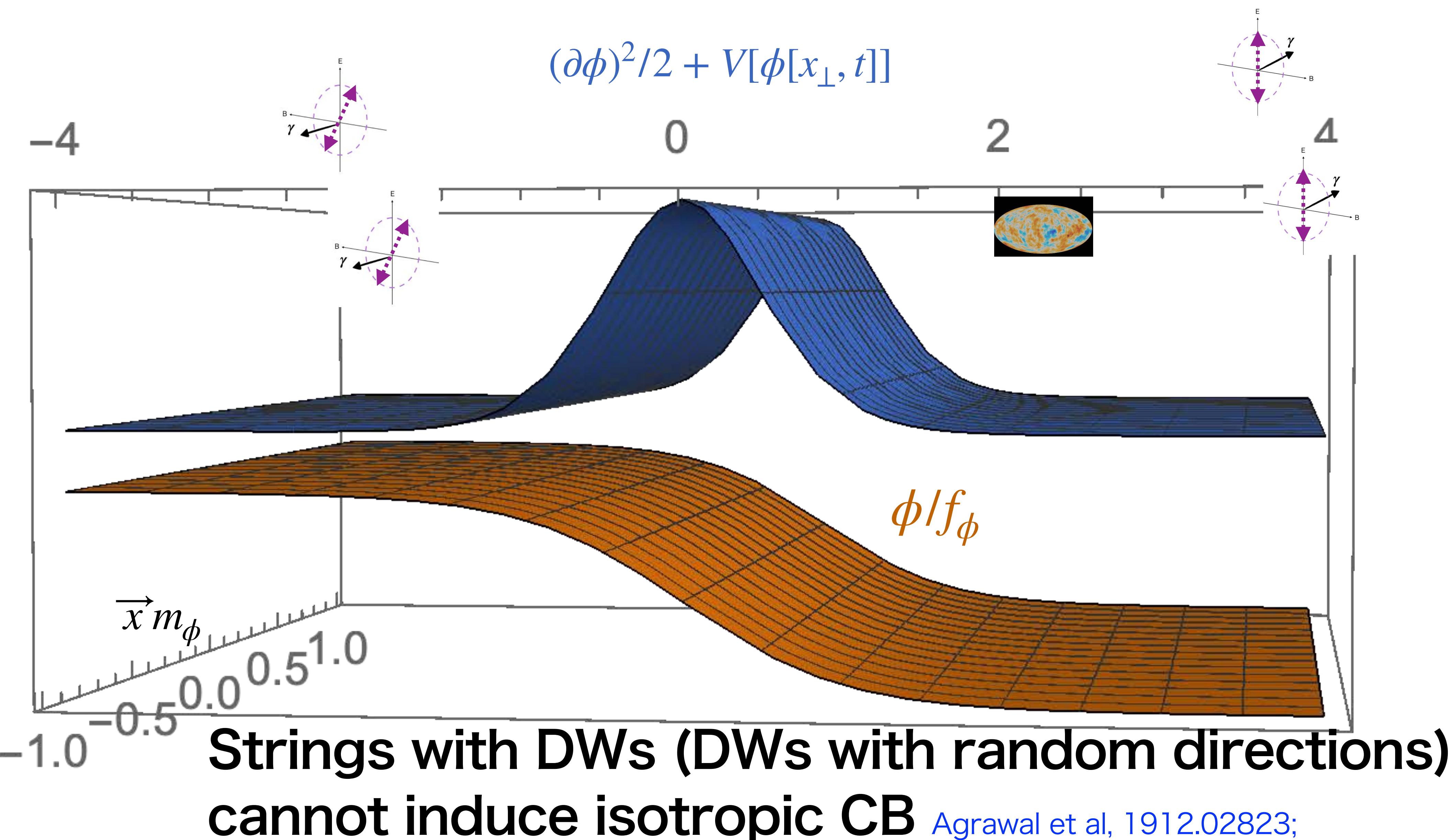
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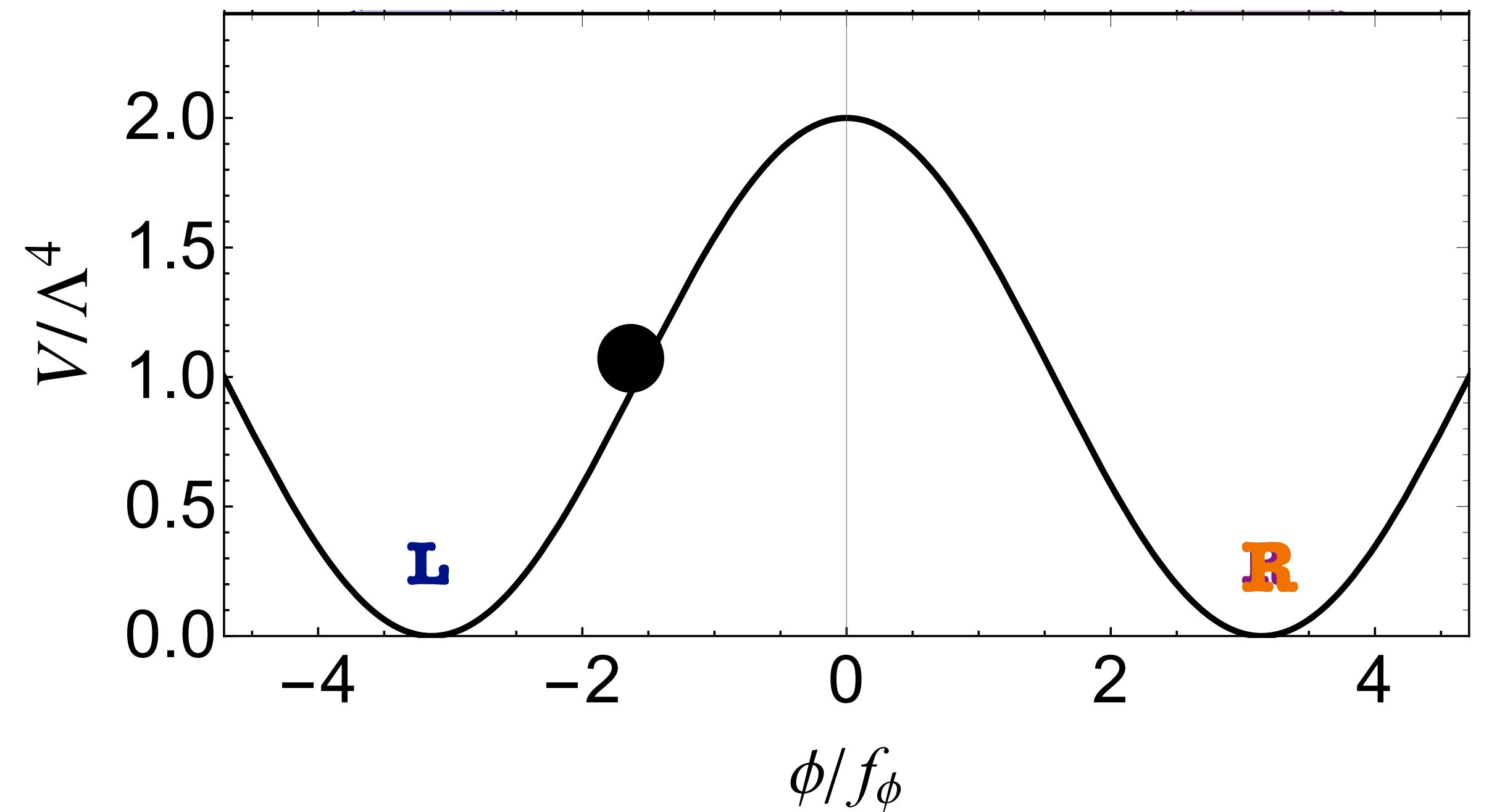
2. ALP domain walls *without a string*

ALP domain wall does not need a string.

Suppose that PQ symmetry never restore. During the inflation ALP undergoes random walk due to quantum diffusion given $m_\phi \ll H_{\text{inf}}$.

$$\dot{\phi}_{\text{classical}} \simeq -\frac{m_\phi^2}{H_{\text{inf}}} \phi \rightarrow 0$$

(at 1 Hubble time)

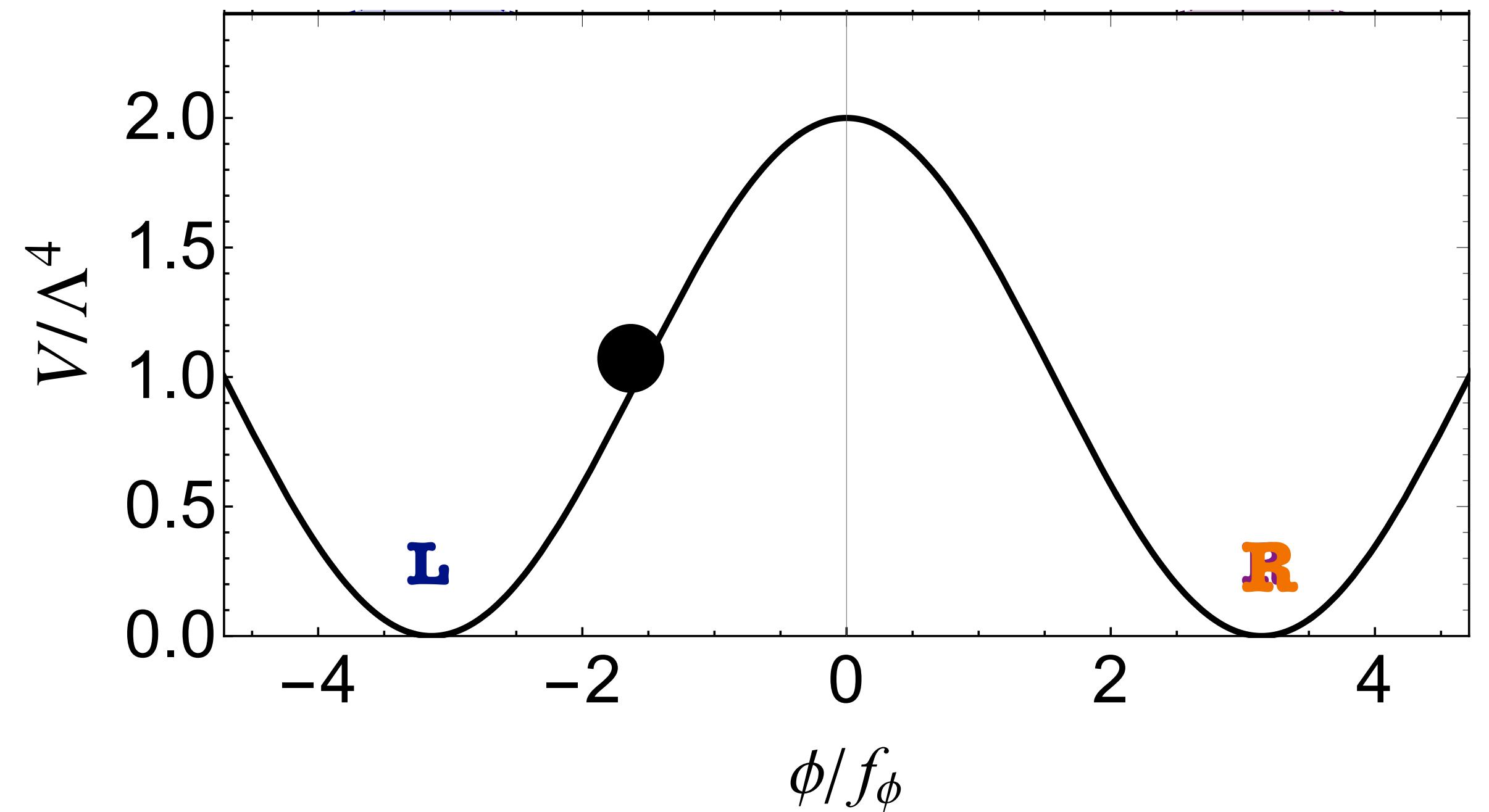


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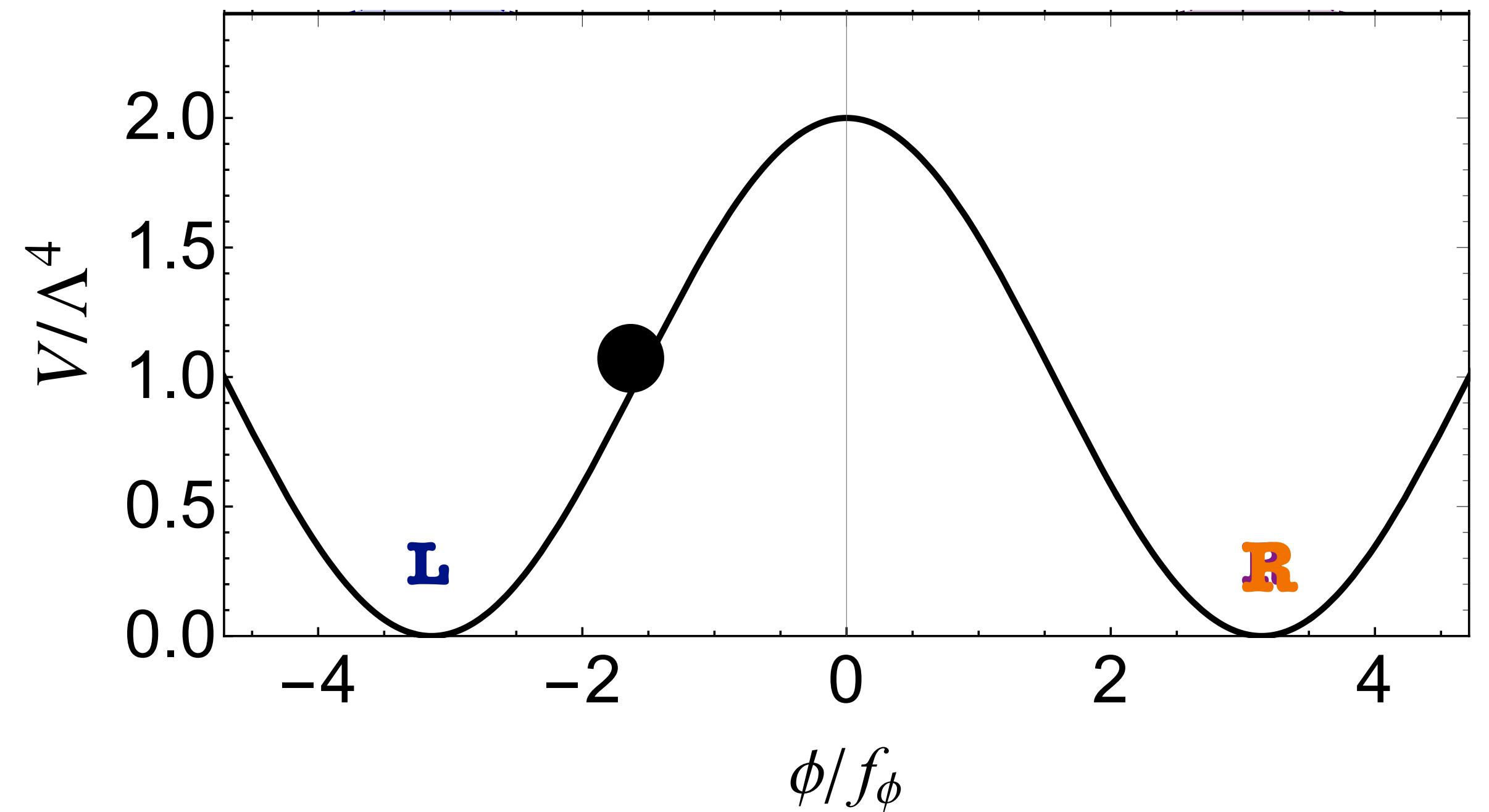


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Quantum jump (Random walk) $\frac{\delta\phi}{f_\phi} \sim \frac{H_{\text{inf}}}{2\pi f_\phi}$ (at 1 Hubble time)

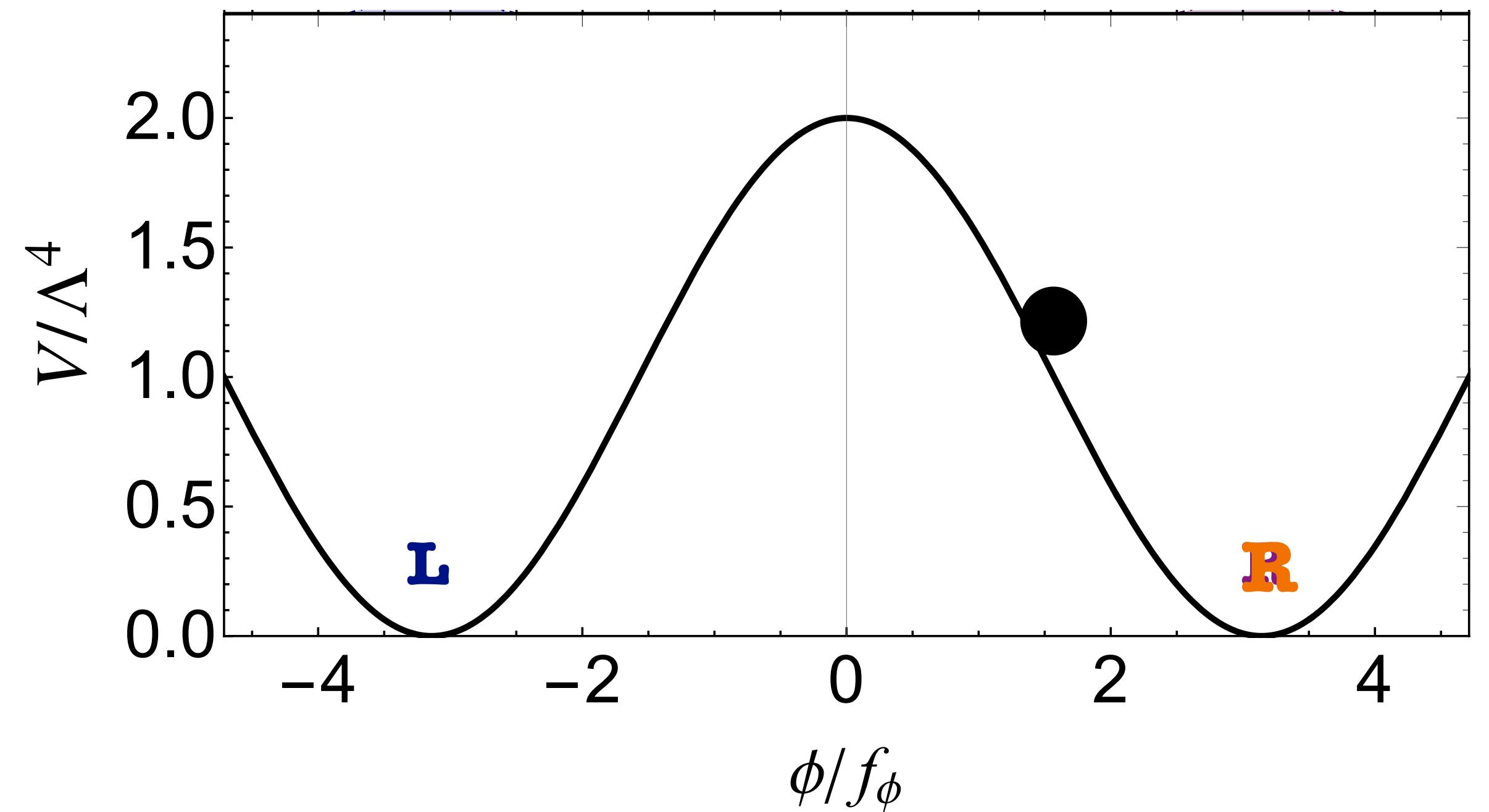


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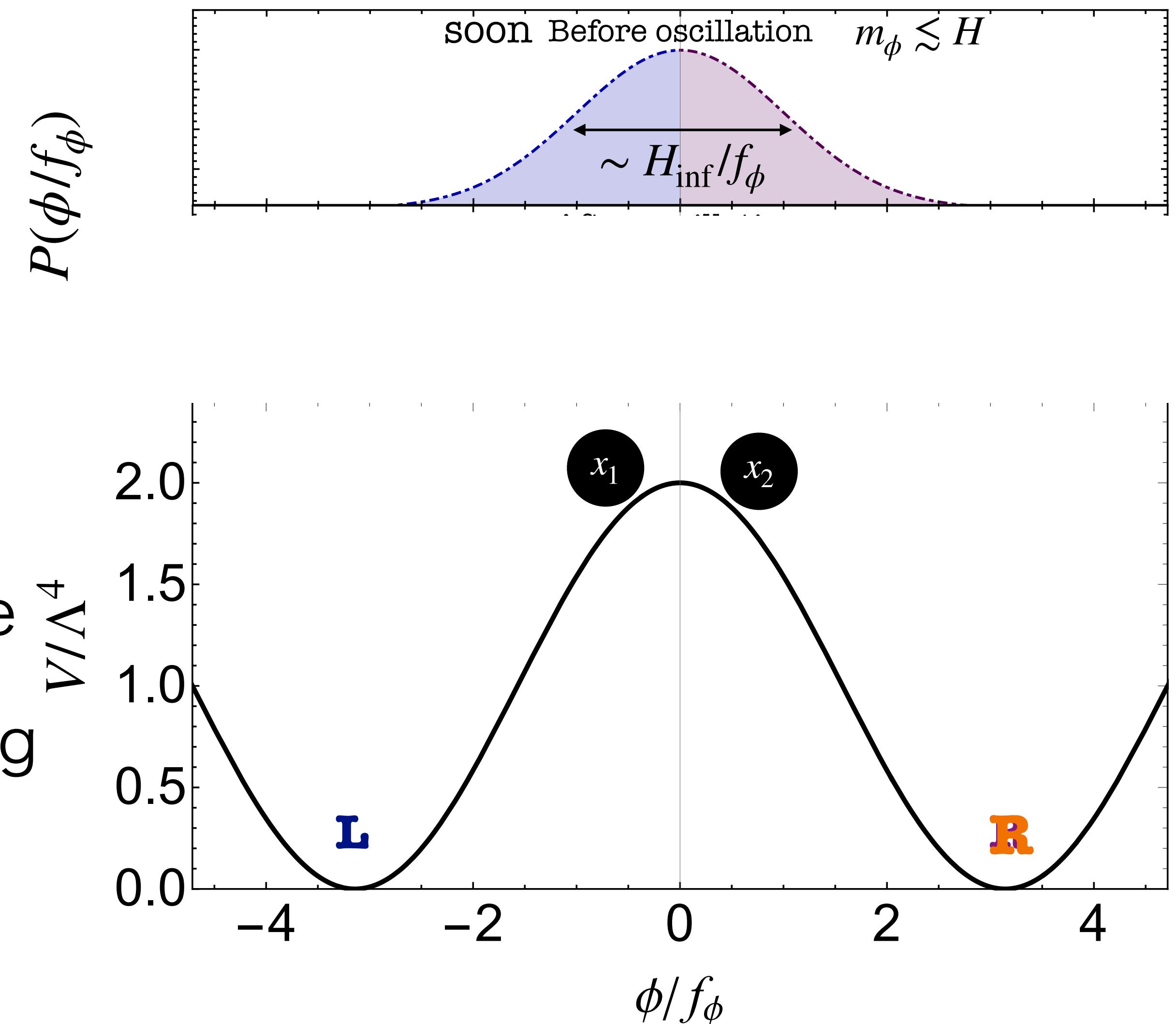
c.f. Resembles the domain wall from a Z_2 breaking

Let us consider that PQ symmetry never restore.

- .It is natural that ϕ has a non-trivial initial distribution, e.g. during inflation $\Delta\phi \sim H_{\text{inf}}/(2\pi)$.

- .When $m_\phi \sim H$, ALP starts to oscillate about two vacua, L and R depending on the position.

- .Domain walls!



ALP domain wall does not need a string.

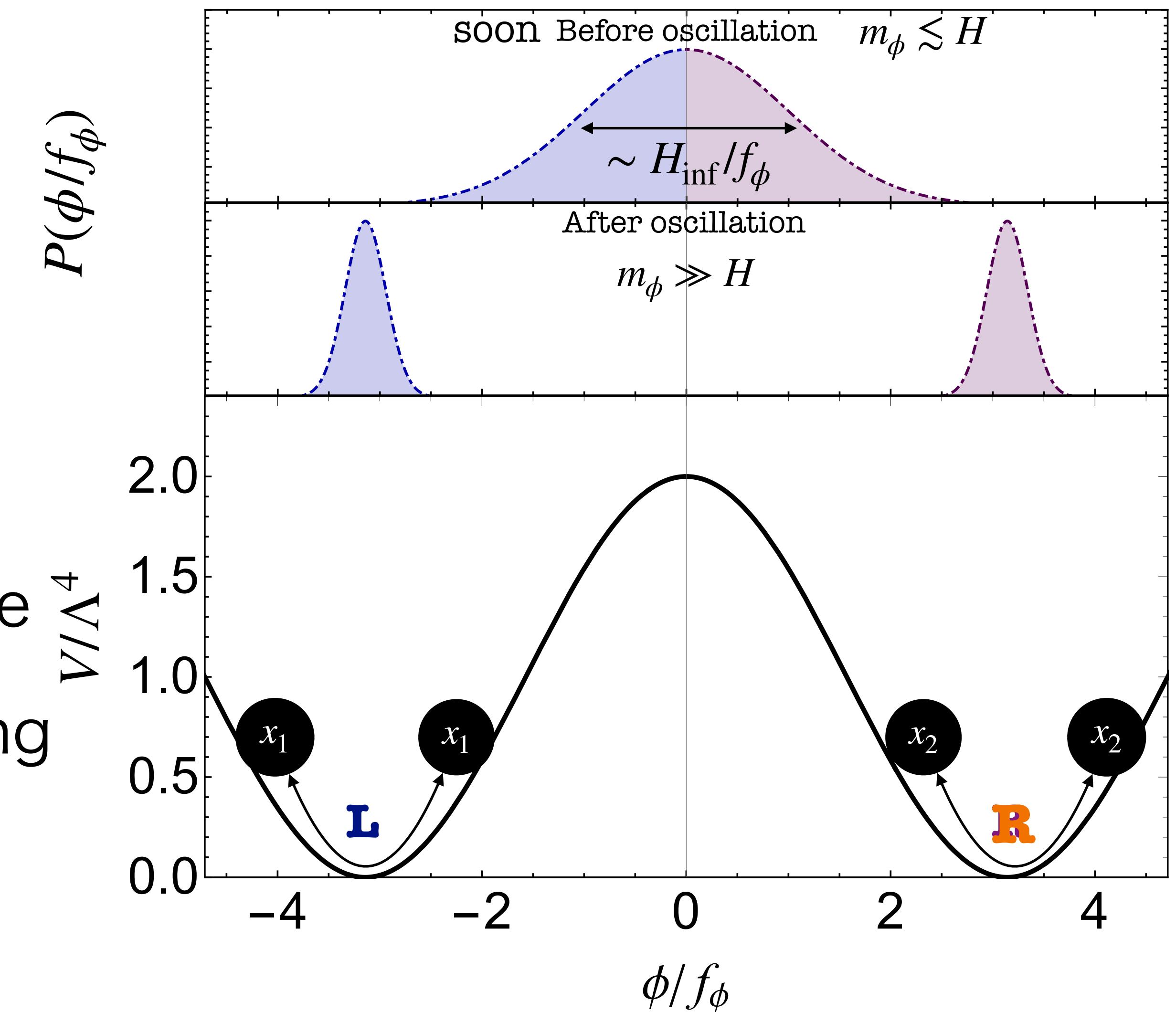
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Percolation theory and domain wall network

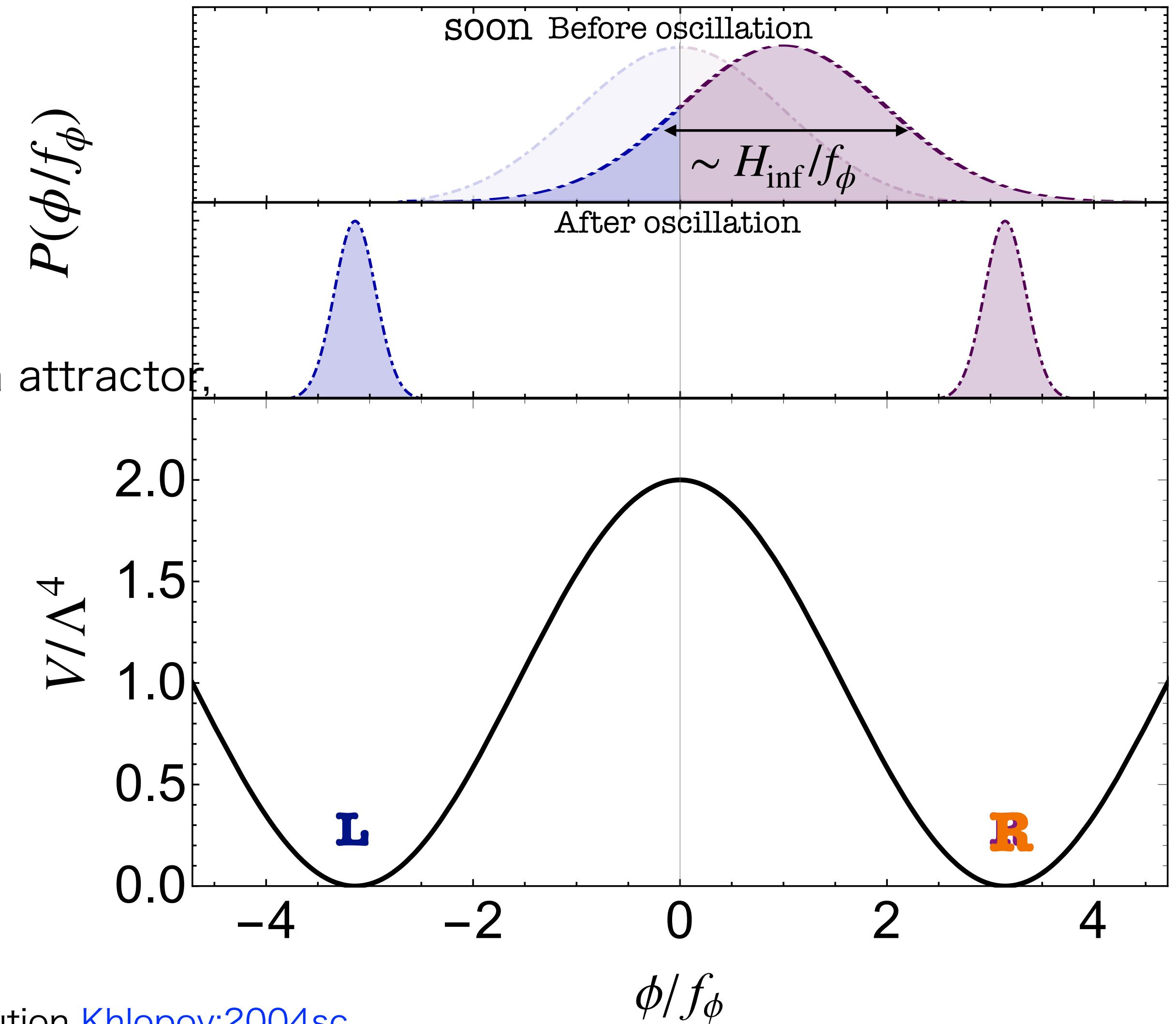
Soon after the onset of oscillation many domain walls are formed

as long as $0.31 < \int_{-2\pi}^0 d\theta P(\theta) < 0.69$.

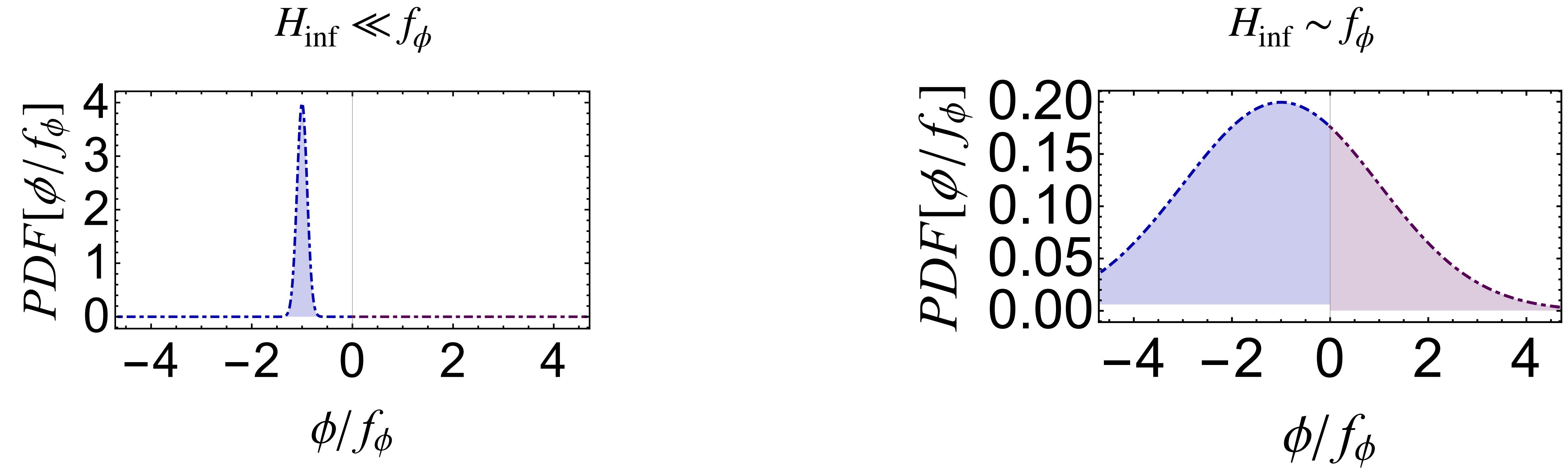
Vachaspati:1984dz, Vilenkin:1984ib

The distribution much after the onset of oscillation is an attractor, known as the scaling solution.

$O(1)$ domain walls always survive in a Hubble horizon at any time.



See also the PBH production scenario without satisfying the scaling solution [Khlopov:2004sc](#).



ALP domain wall without a string can
be naturally formed if $f_\phi \gtrsim H_{\text{inf}}$!

Is $f_\phi \sim H_{\text{inf}}$ for DW without a string natural?

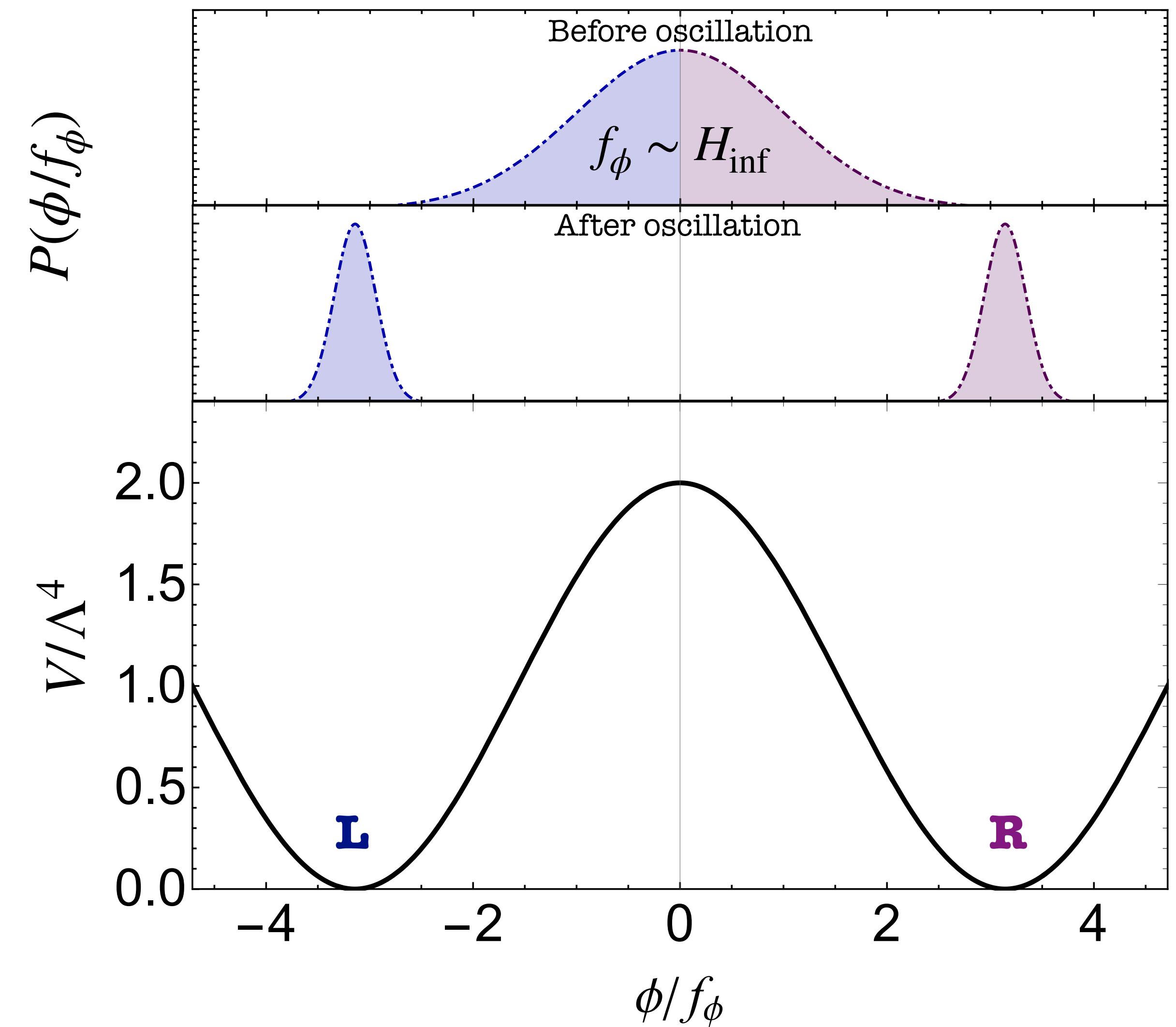
Given the light ALP, our predictions only rely on the condition $f_\phi \sim H_{\text{inf}}$

$$\mathcal{L} \supset \sqrt{-g}R \left(\frac{\xi}{2} |S|^2 + \frac{M_{\text{pl}}^2}{2} \right)$$

$$V_{\text{eff}} \approx (-6\xi H_{\text{inf}}^2 - m_S^2) |S|^2 + \lambda |S|^4$$

if $\xi H_{\text{inf}} \gtrsim m_S$

$$\xrightarrow{} f_{\phi,\text{inf}} \simeq 2\sqrt{\frac{3\xi}{\lambda}} H_{\text{inf}}.$$



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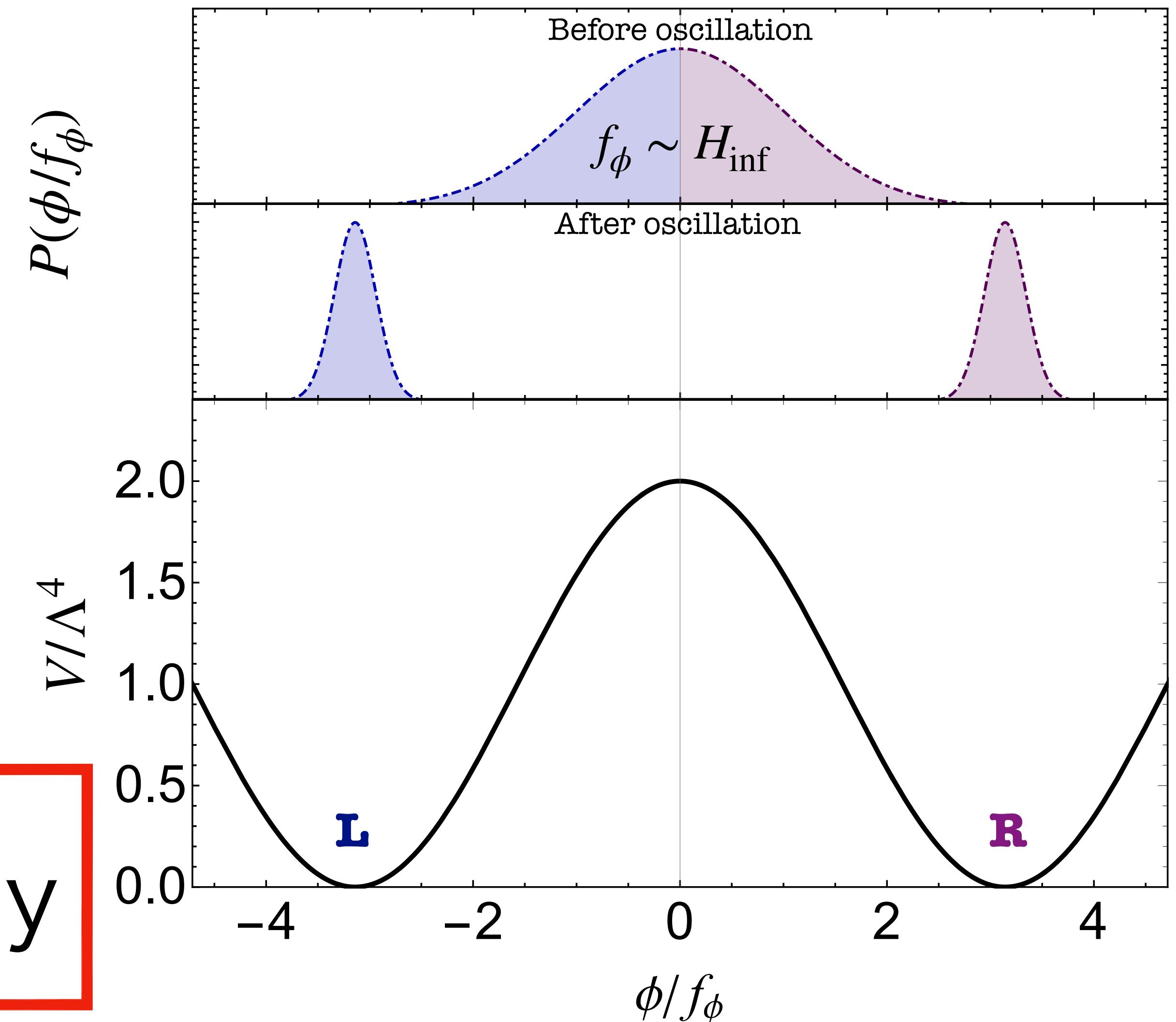
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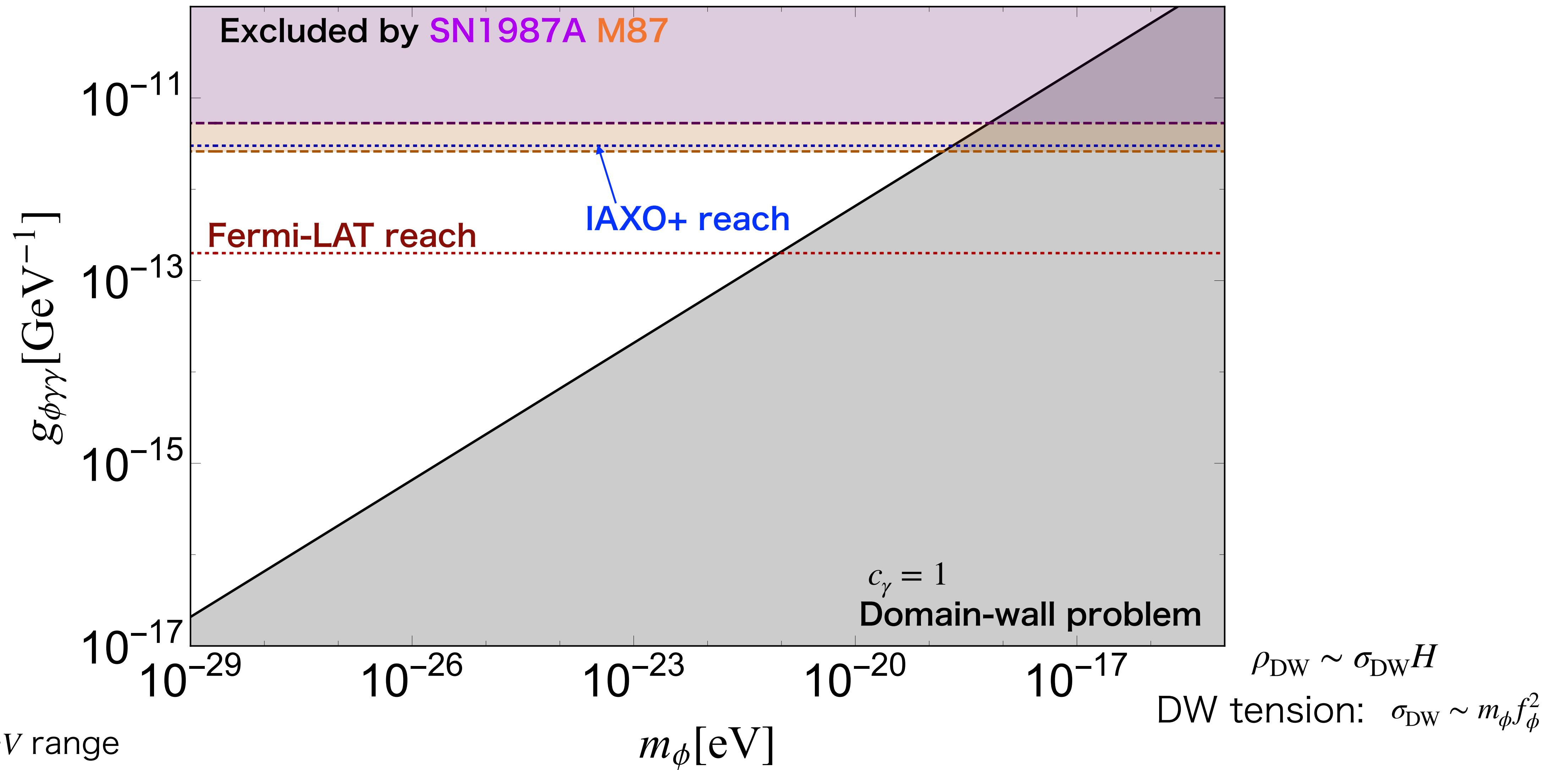
if $\xi H_{\text{inf}} \gtrsim m_S$

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DWs are formed naturally



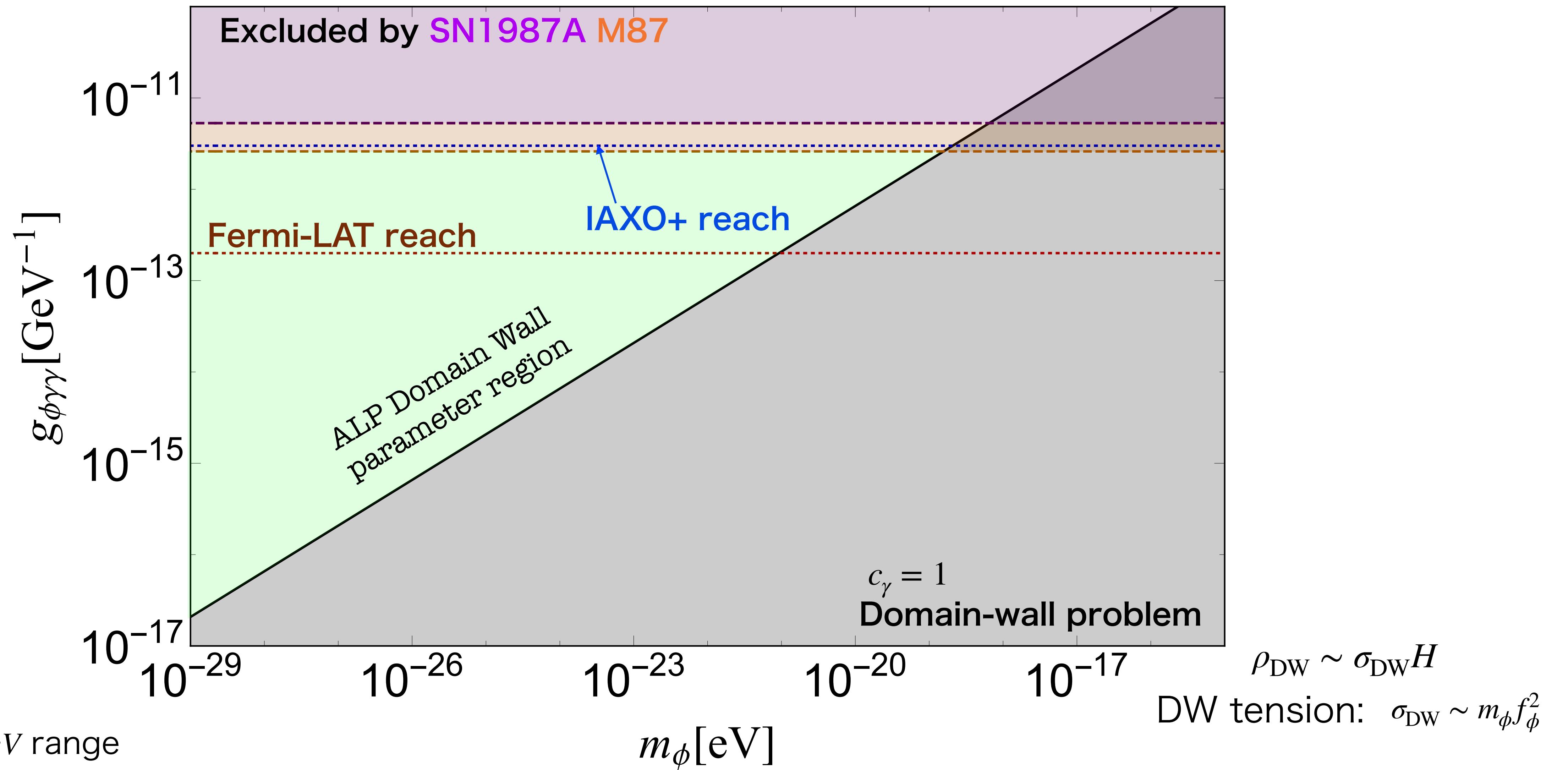
Parameter region of ALP domain wall in the scaling solution



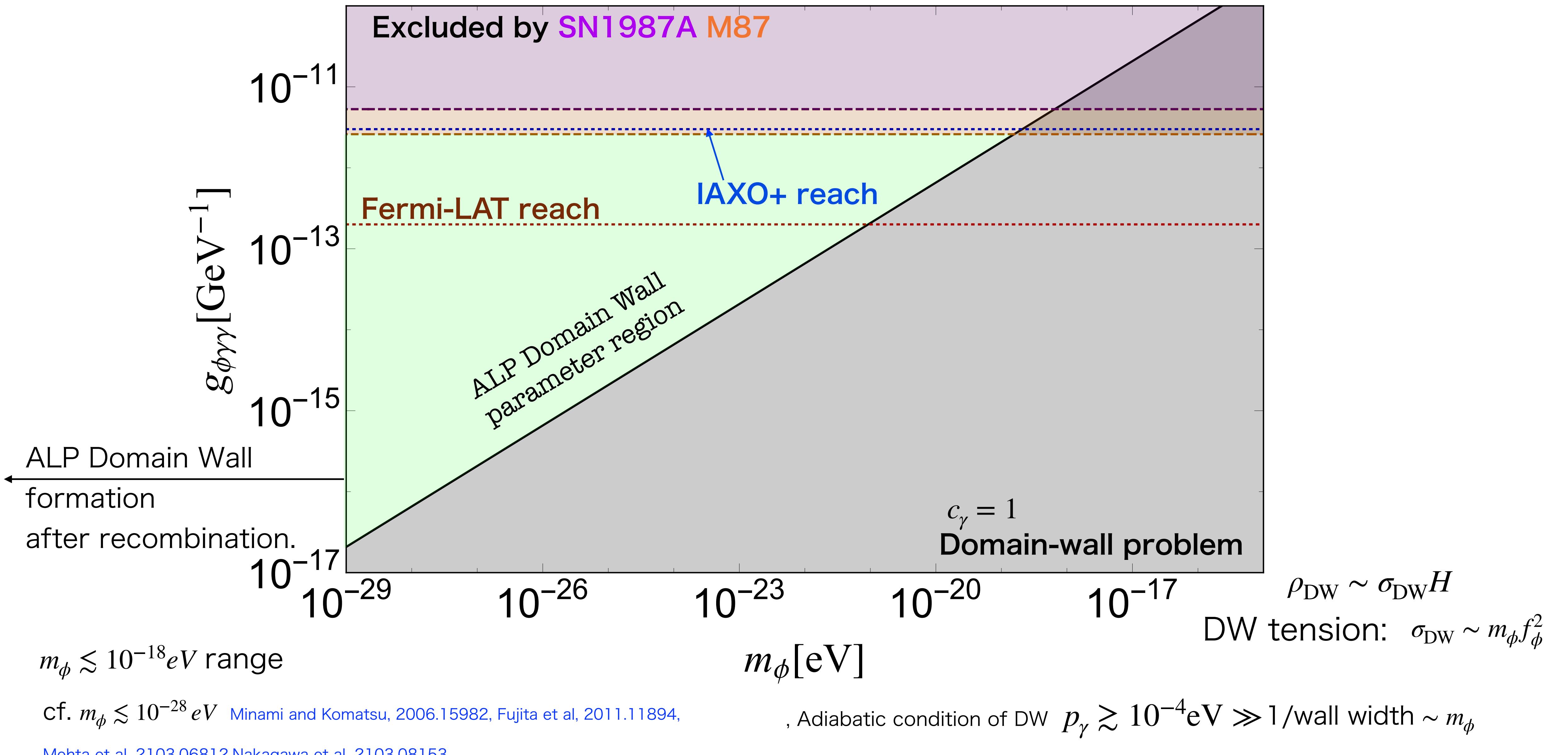
cf. $m_\phi \lesssim 10^{-28}$ eV Minami and Komatsu, 2006.15982, Fujita et al, 2011.11894,

, Adiabatic condition of DW $p_\gamma \gtrsim 10^{-4}$ eV $\gg 1/\text{wall width} \sim m_\phi$

Parameter region of ALP domain wall in the scaling solution

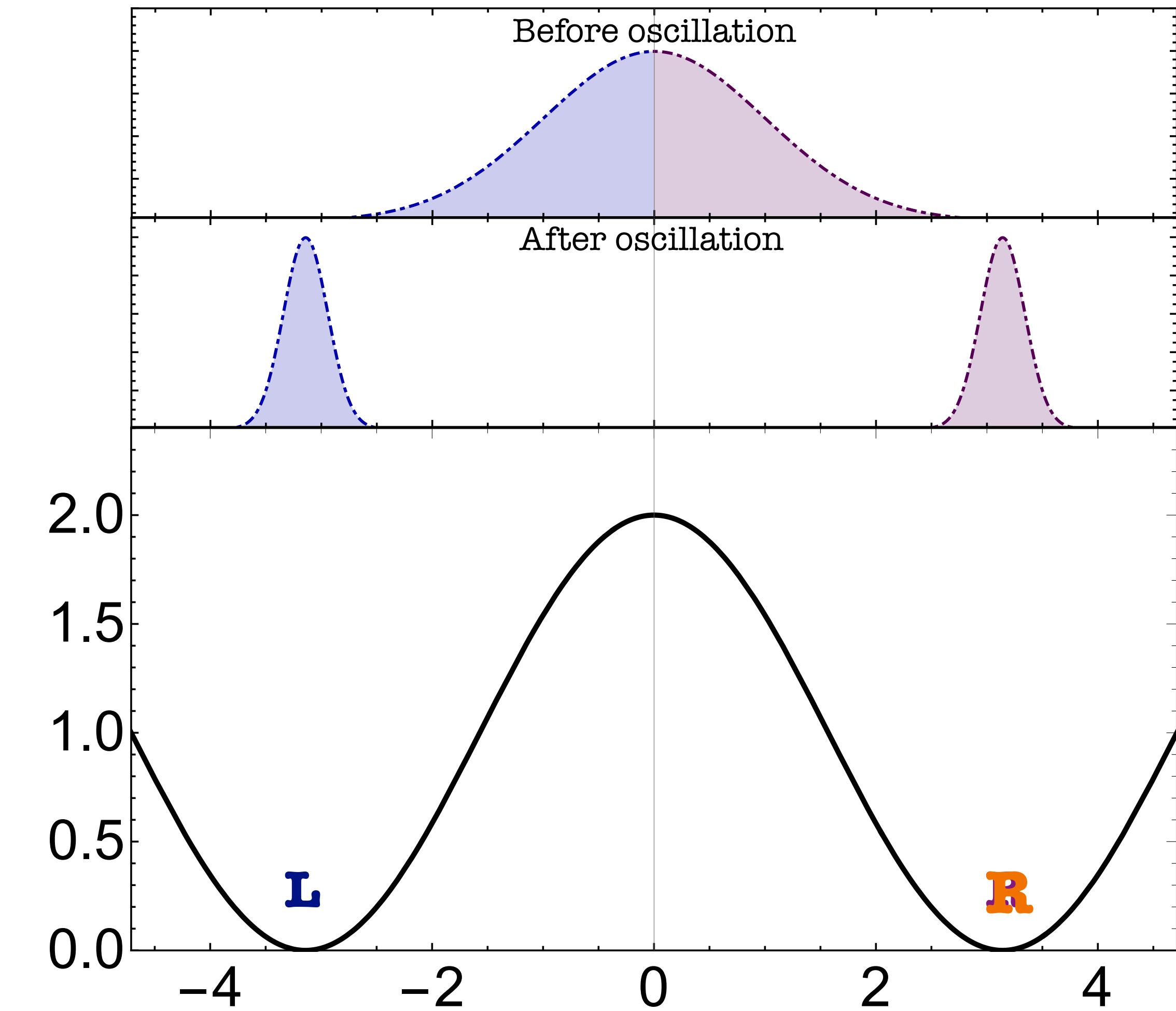
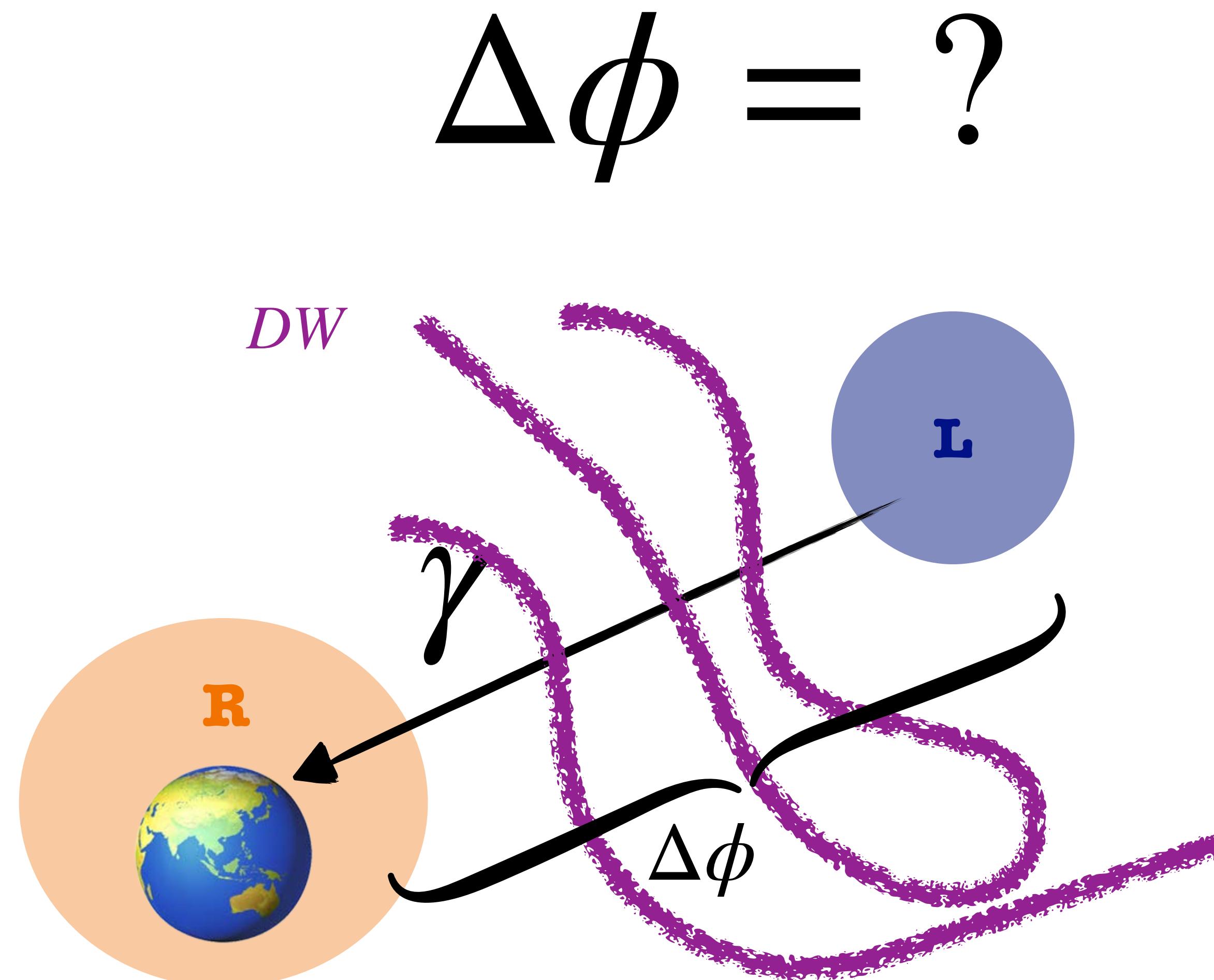


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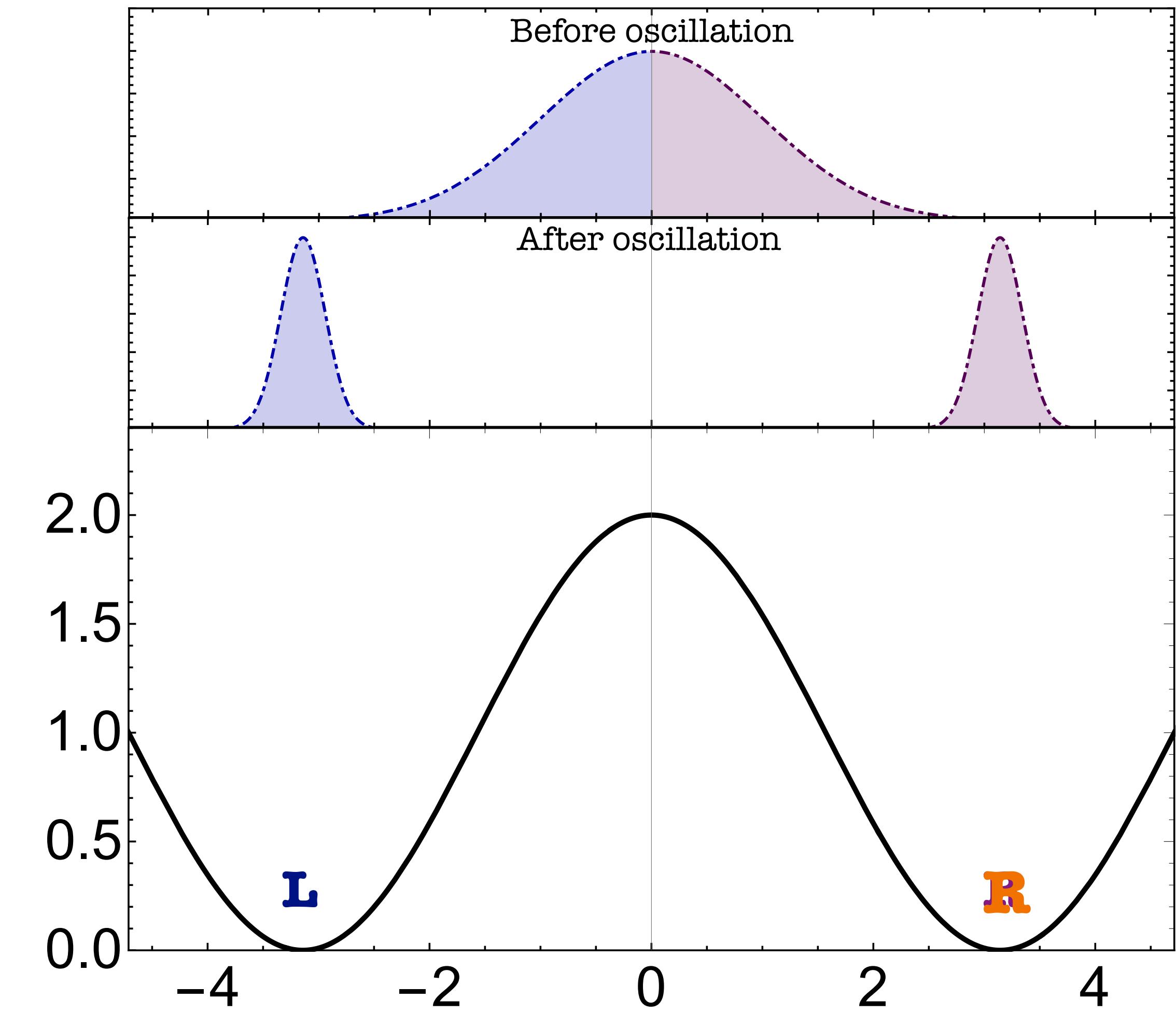
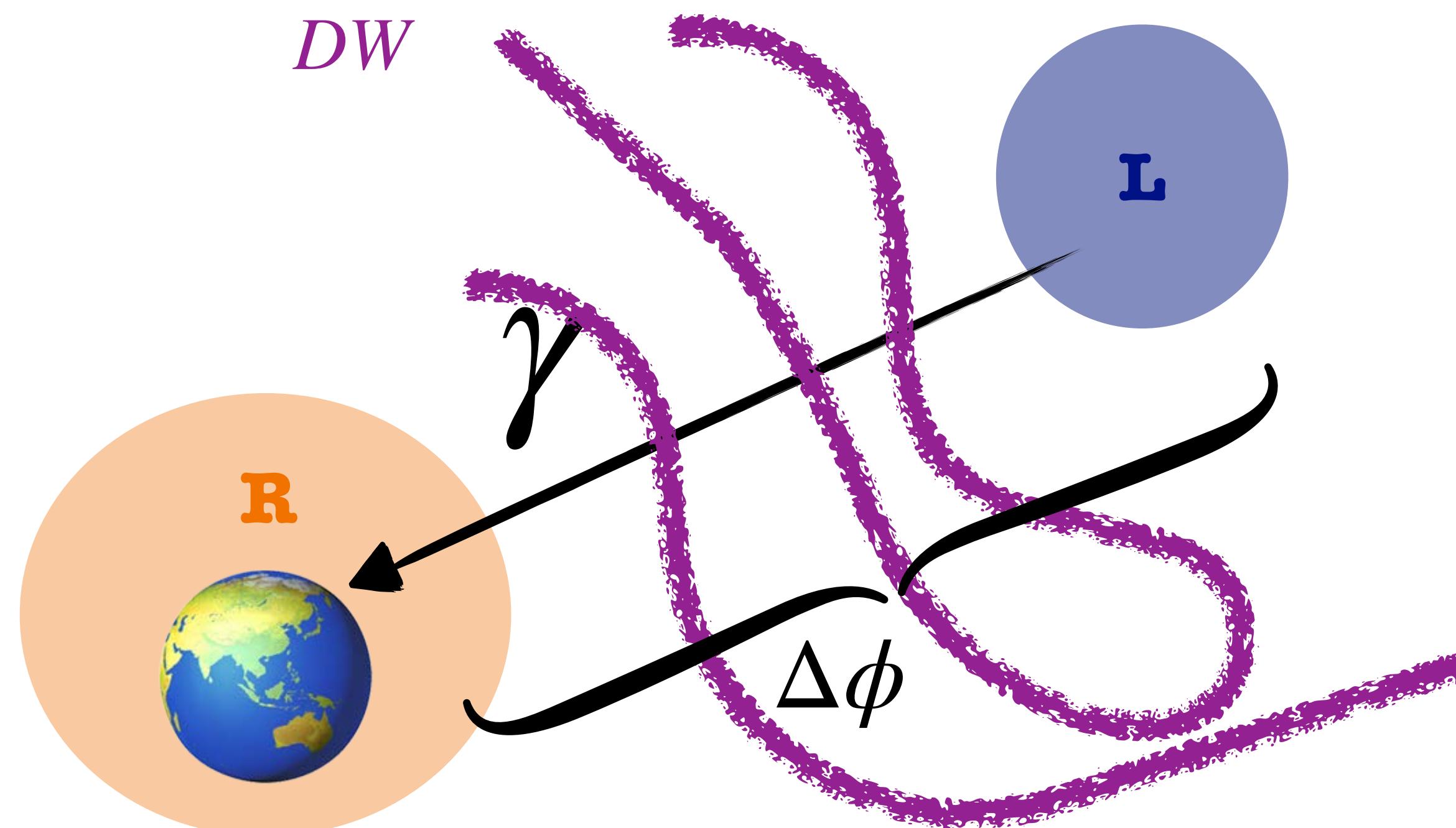
3. *Kilobyte cosmic birefringence (KBCB)*

Path-independent field excursion.

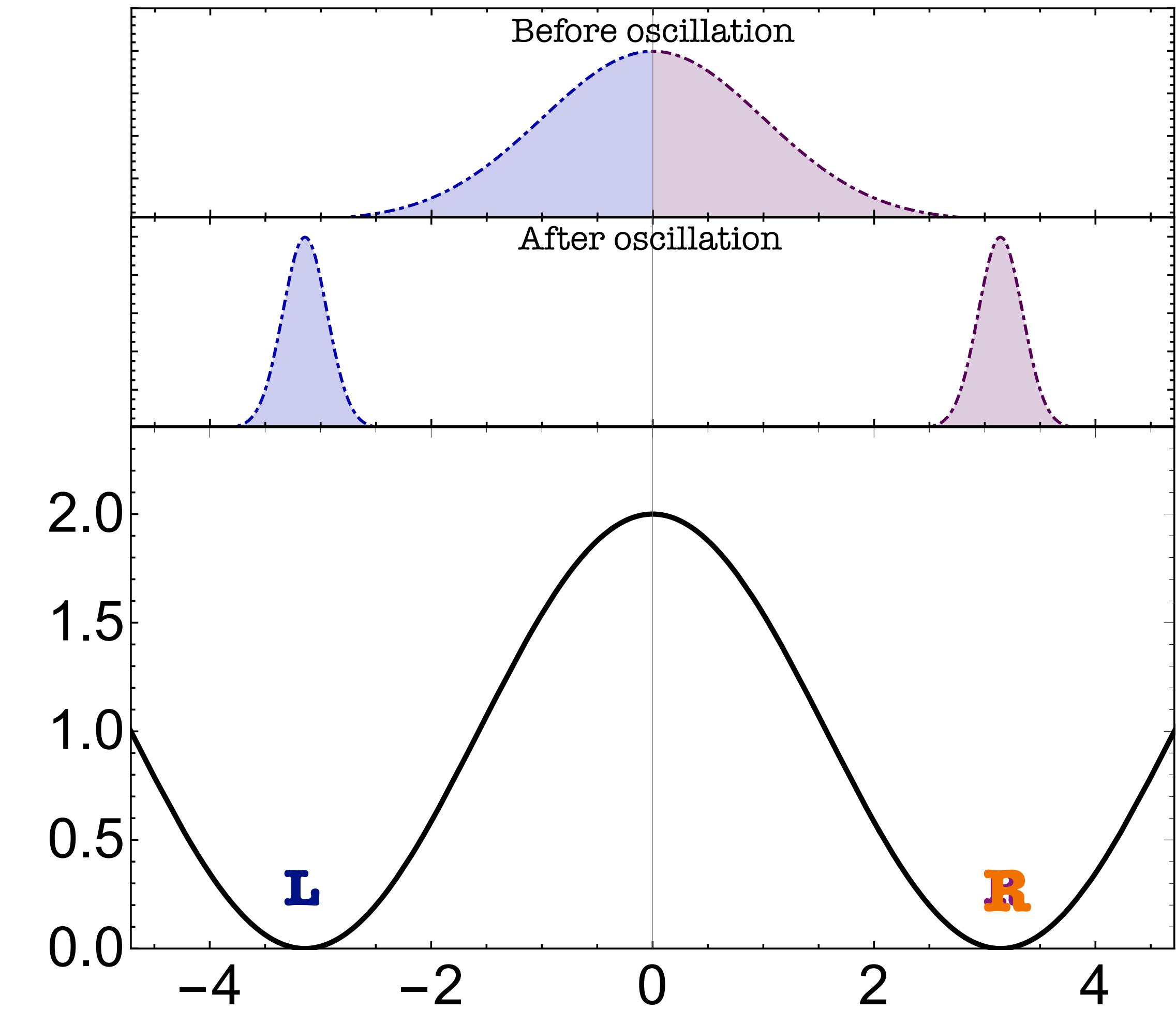
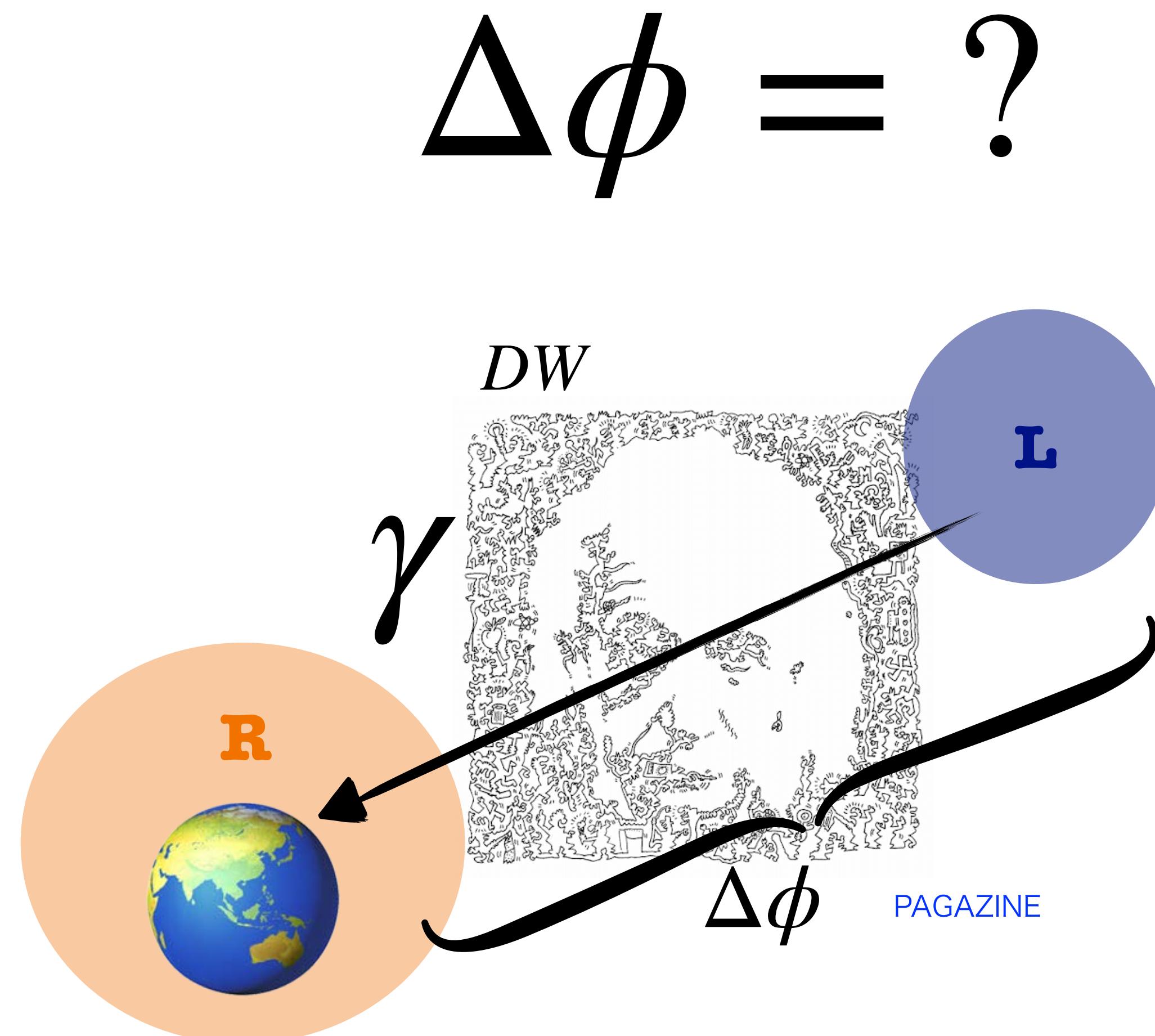


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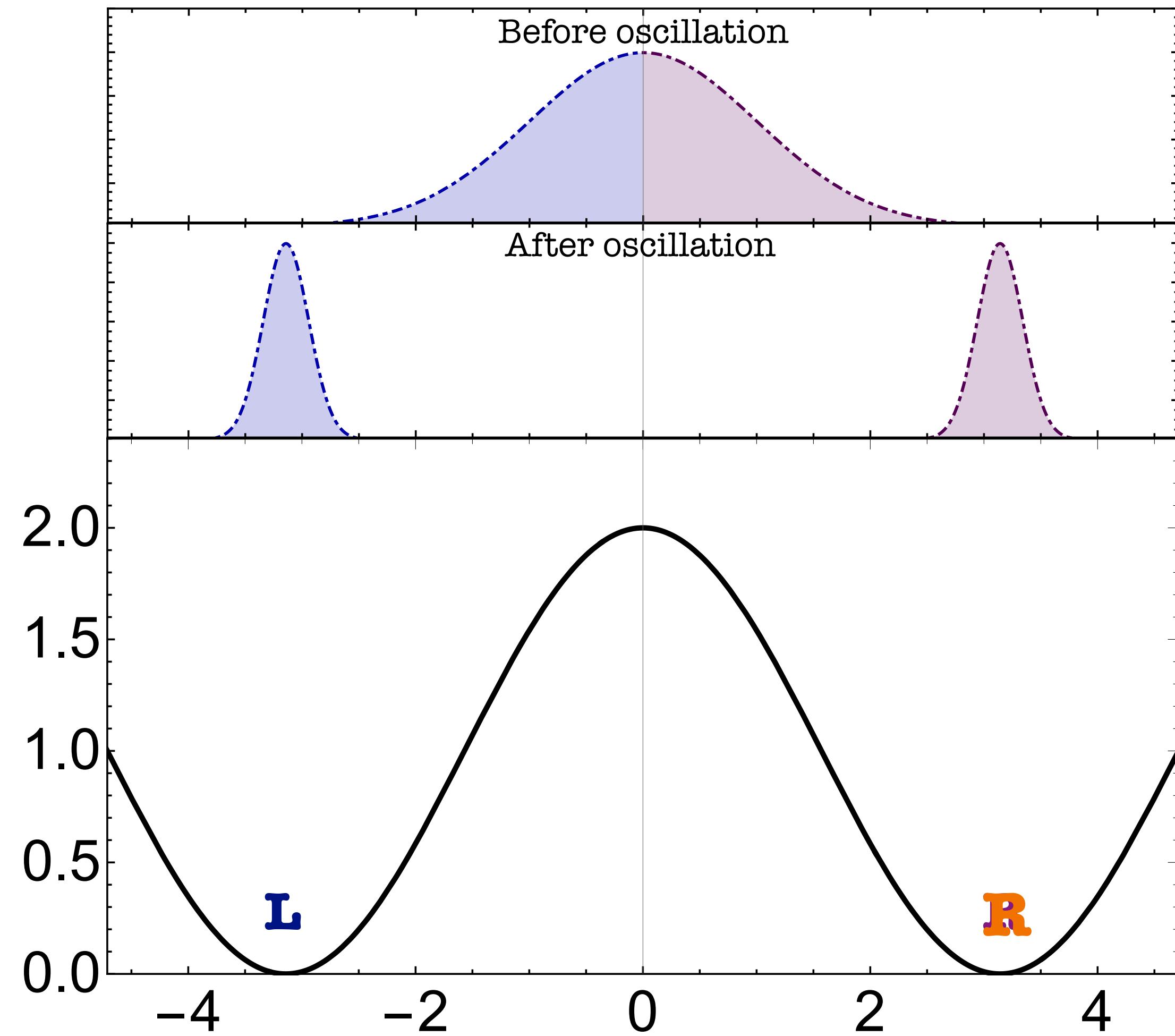
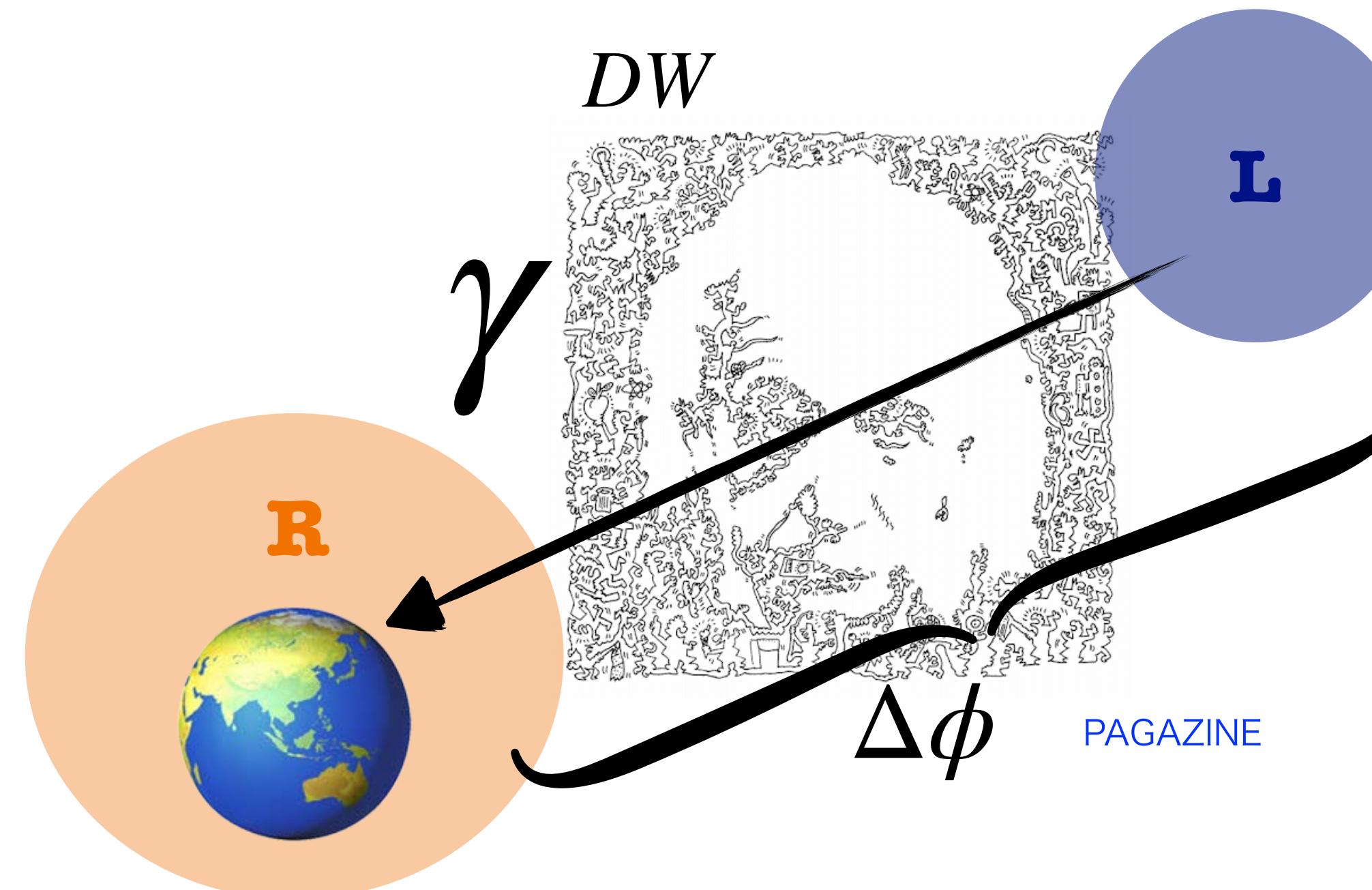
$$\Delta\phi = 2\pi f_\phi$$



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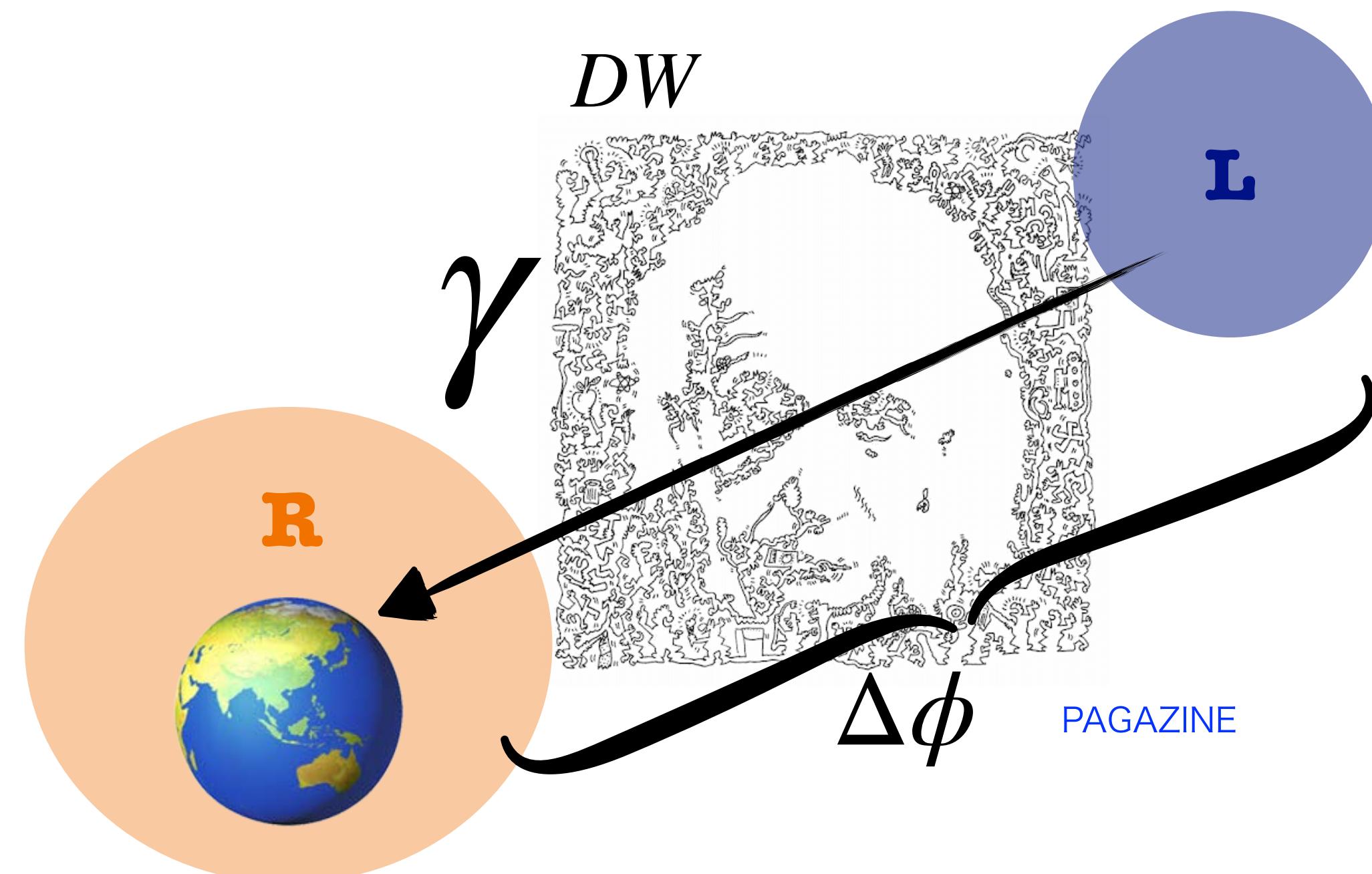


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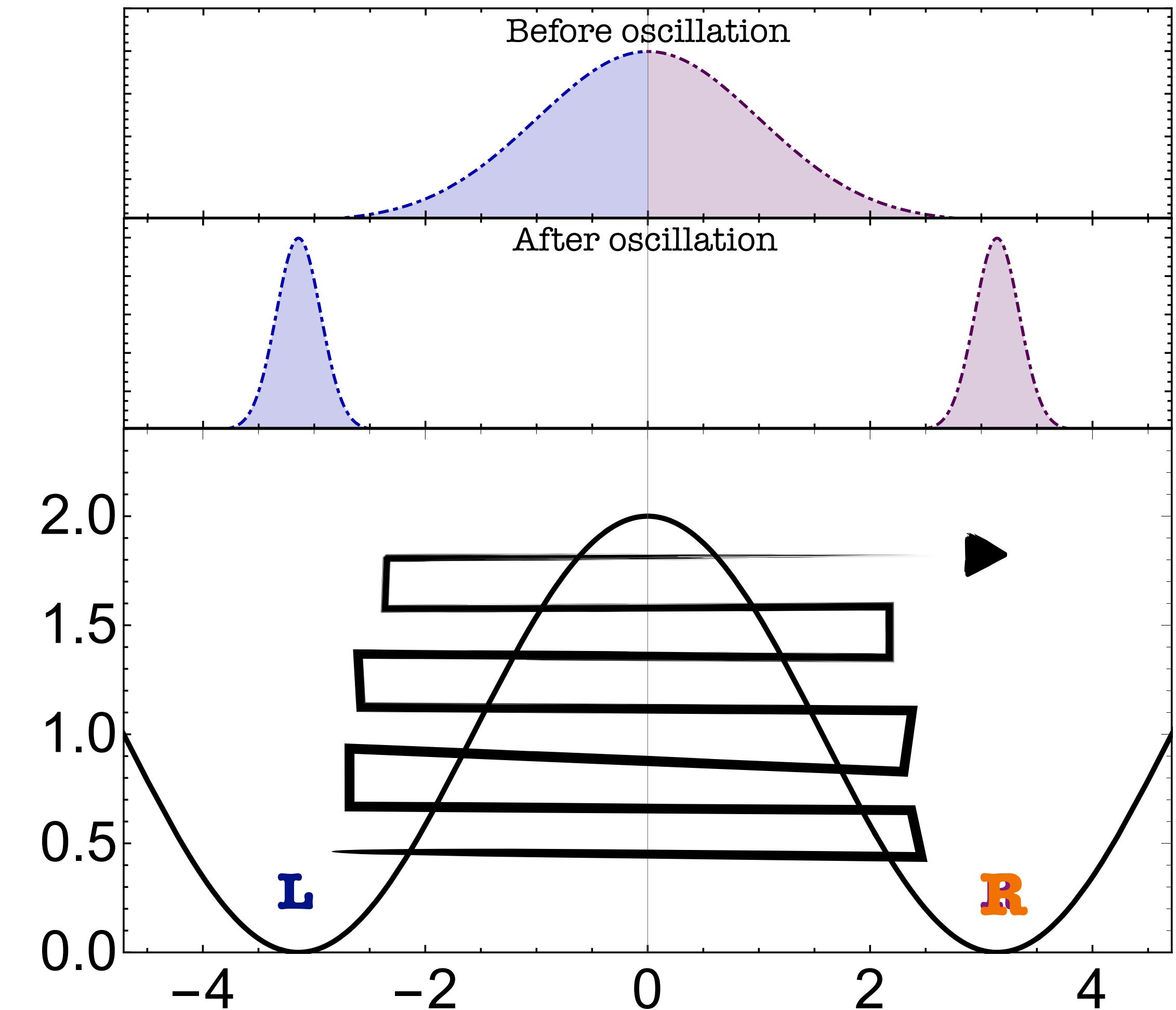
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Field excursion only depends on the
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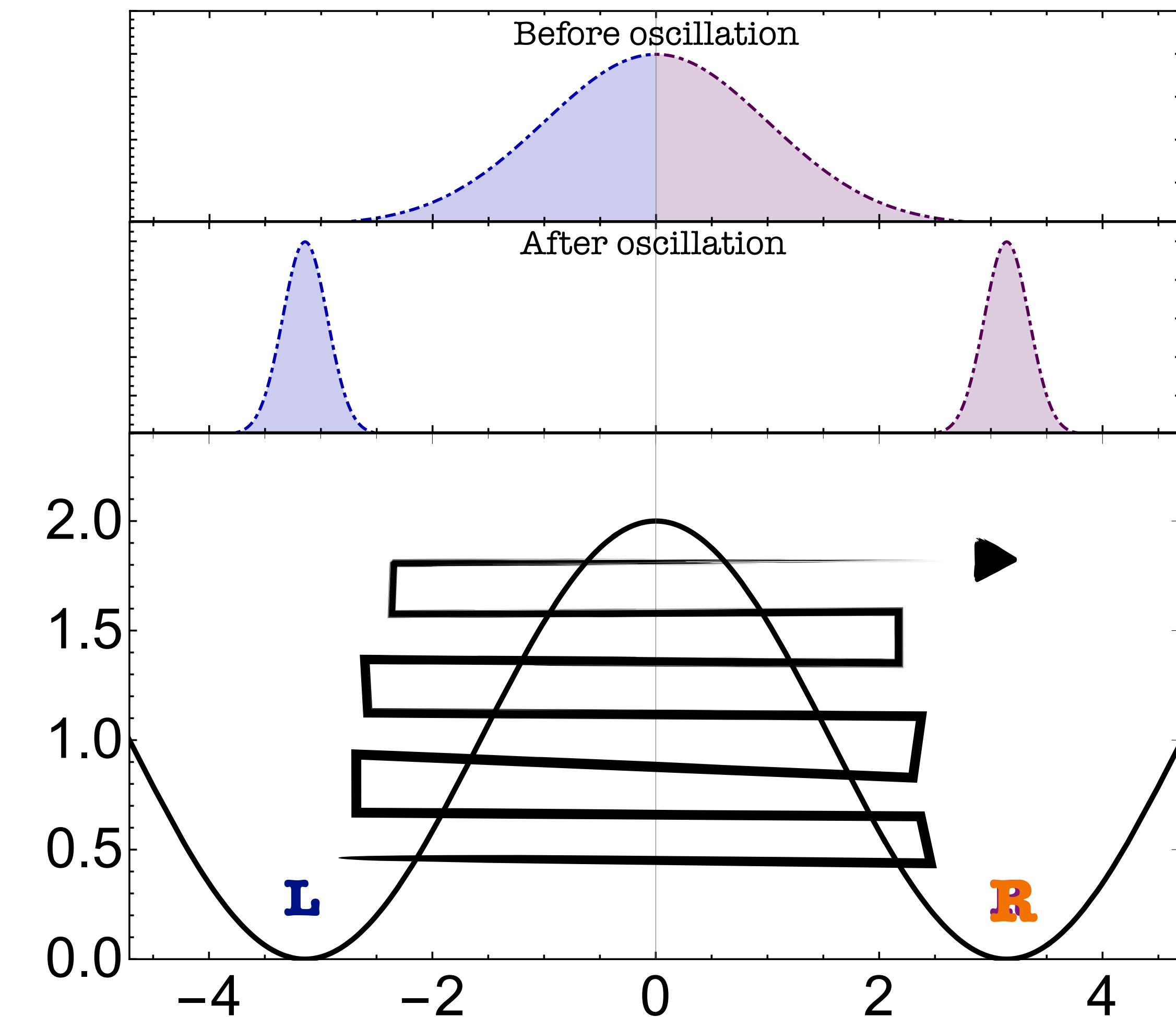
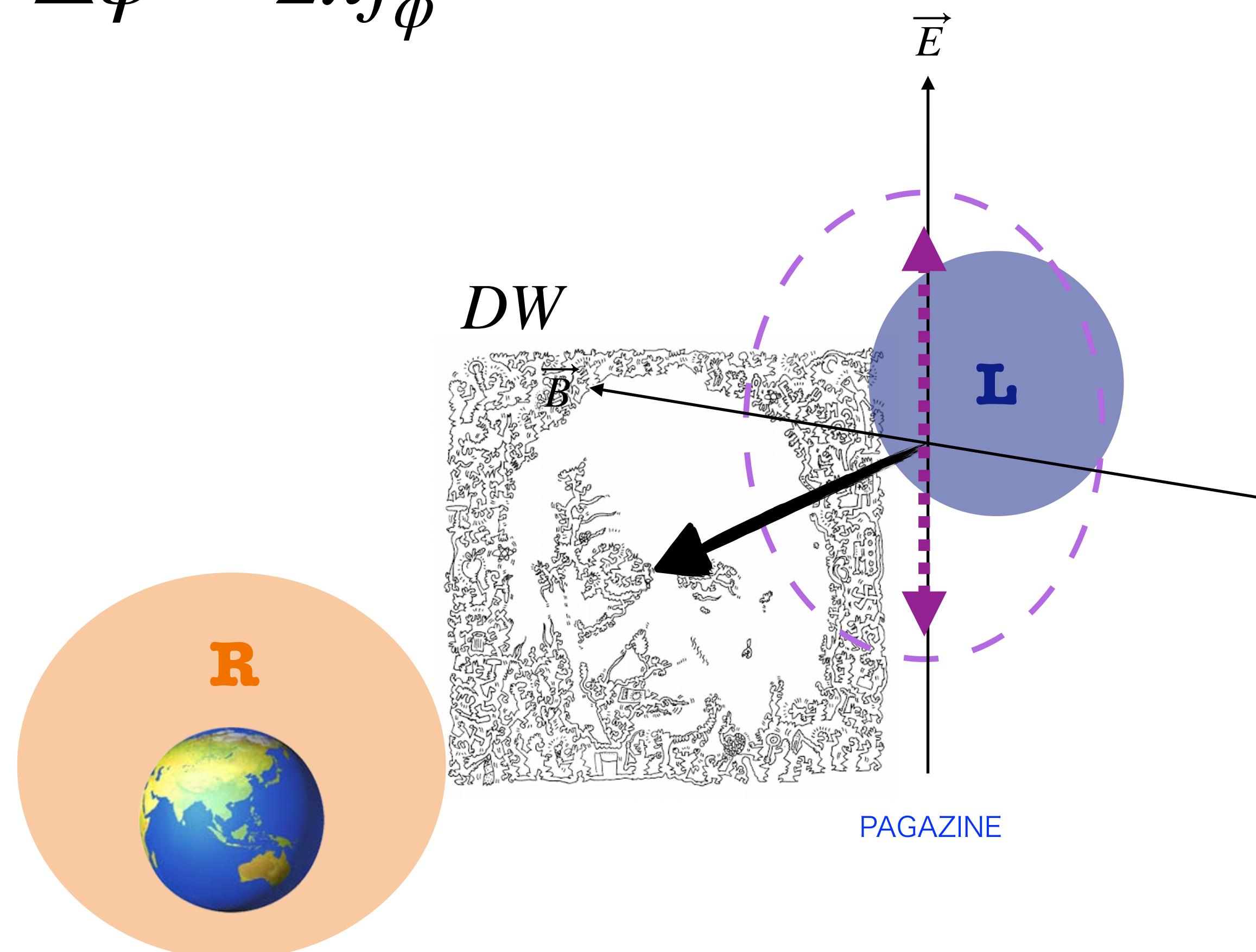
DWs have direction!
[A property special for DW **without string**]



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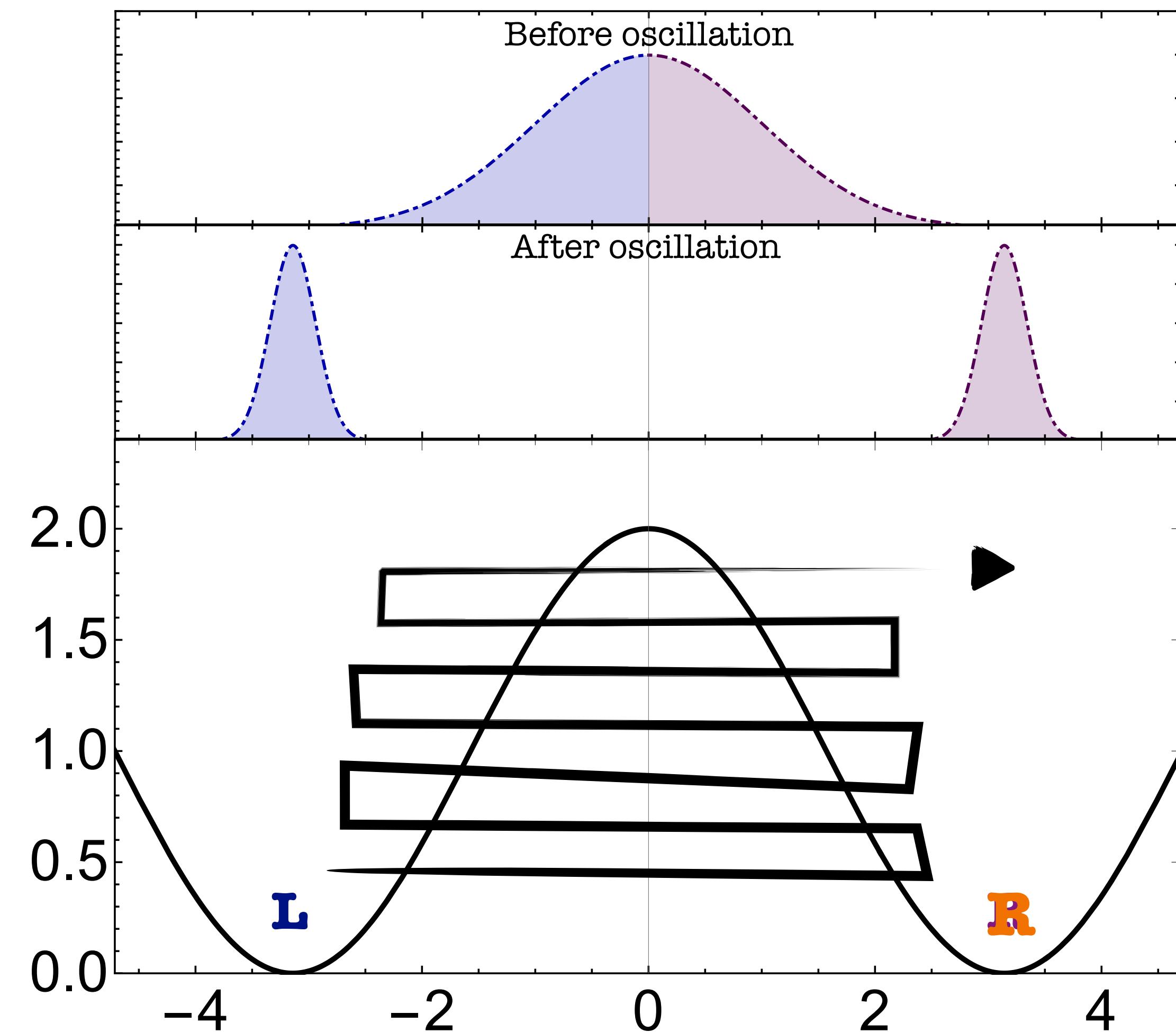
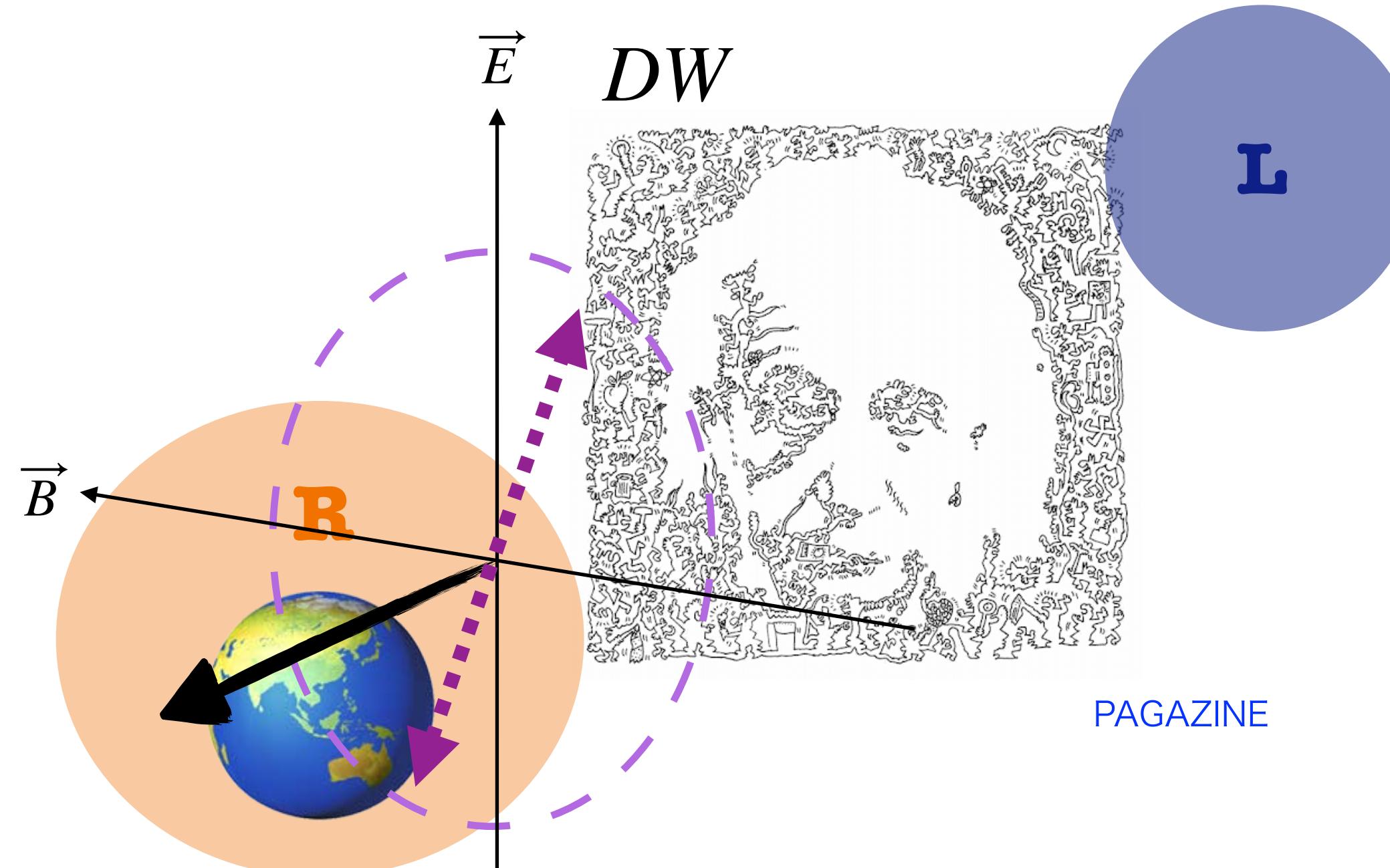


Path-independent birefringence

The net change of polarization angle only depends on the vacua from which photon are emit and detect.

$$\Delta\phi = 2\pi f_\phi \quad \Phi = 0.42 \text{ deg} \times c_\gamma \left(\frac{\Delta\phi}{2\pi f_\phi} \right),$$

$$\Delta\Phi[\Omega] = 0.42 \text{deg} c_\gamma$$

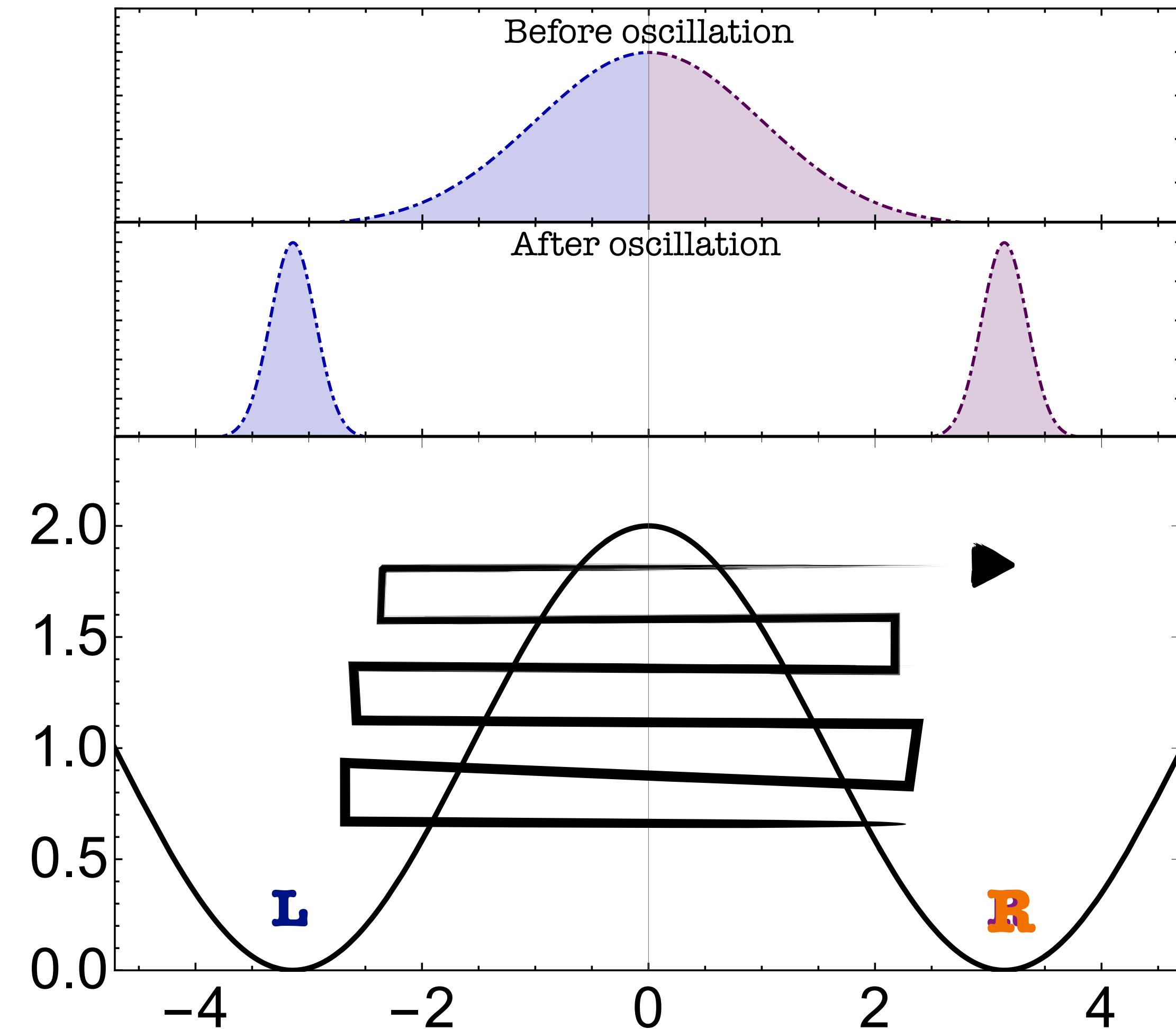
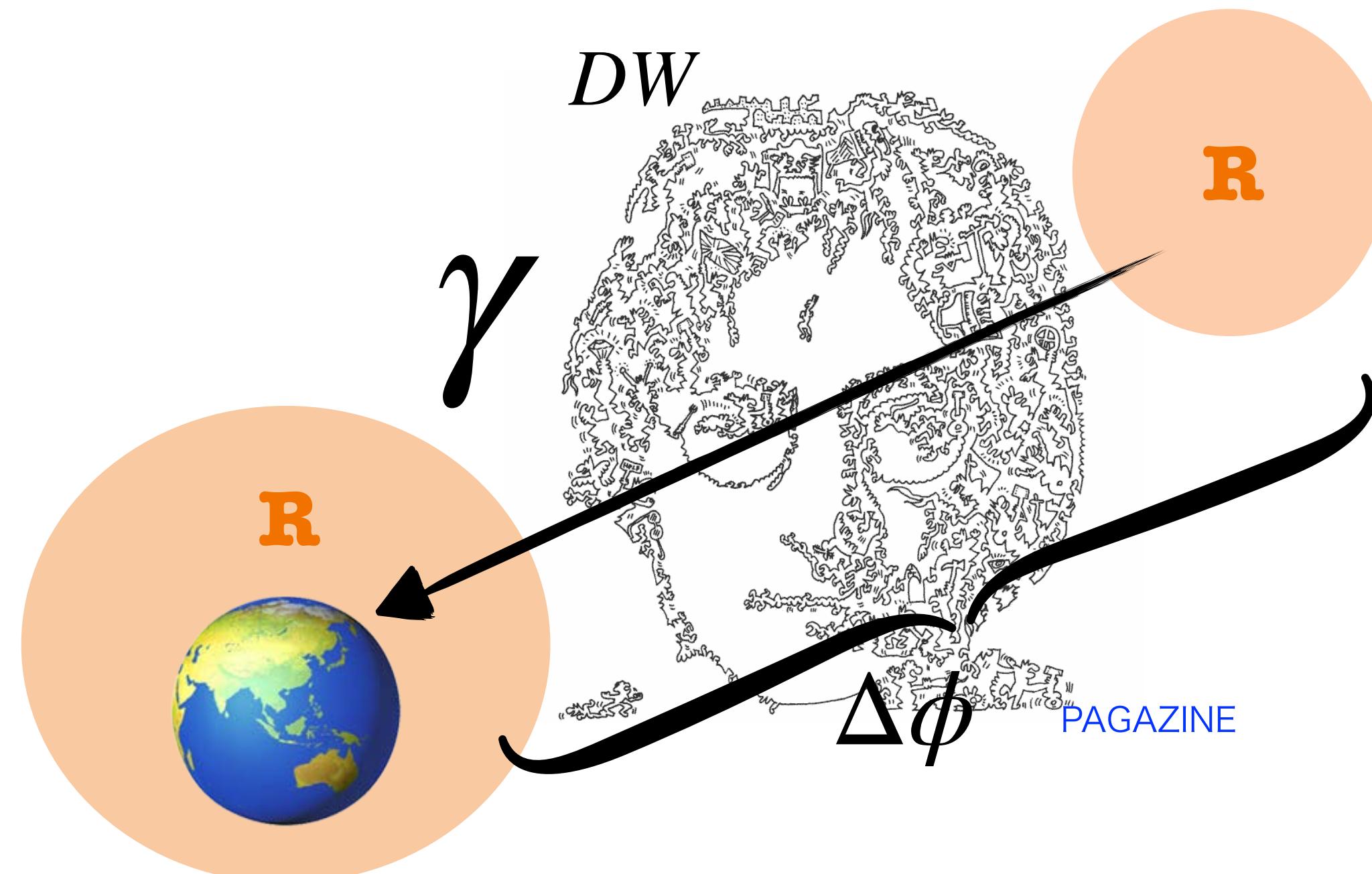


Path-independent birefringence

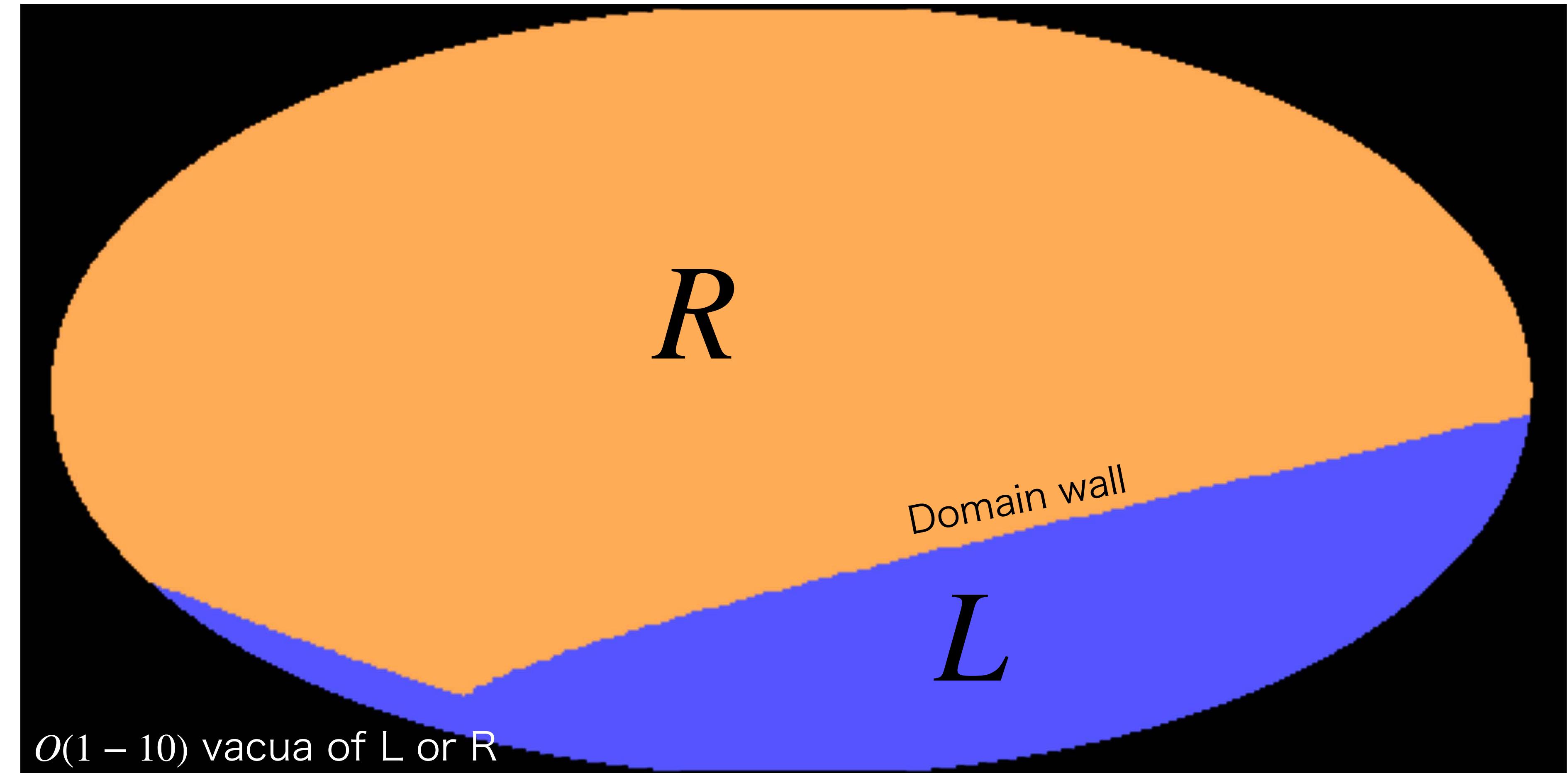
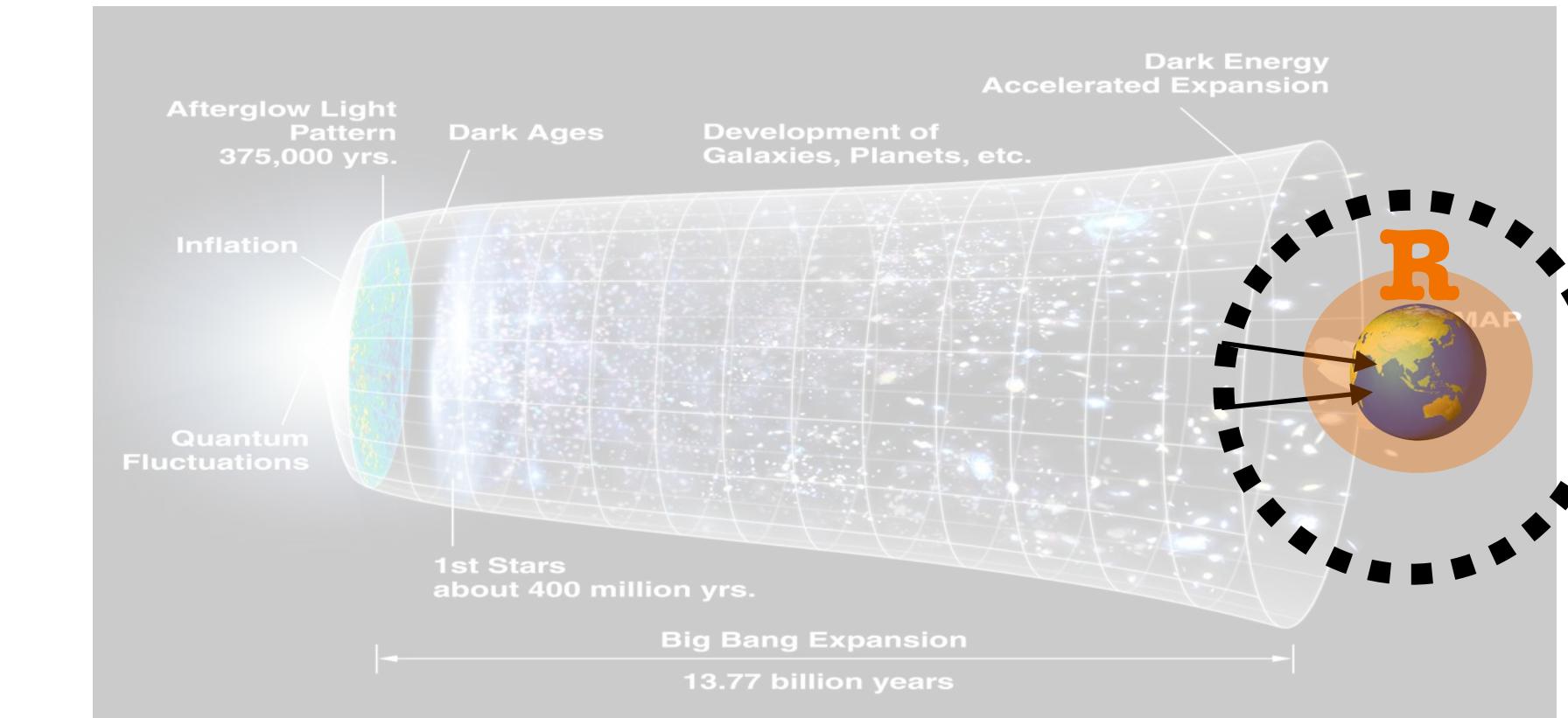
The net change of polarization angle only depends on the vacua from which photon are emit and detect.

$$\Delta\phi = 0 \quad \Phi = 0.42 \text{ deg} \times c_\gamma \left(\frac{\Delta\phi}{2\pi f_\phi} \right),$$

$$\Delta\Phi[\Omega] = 0$$

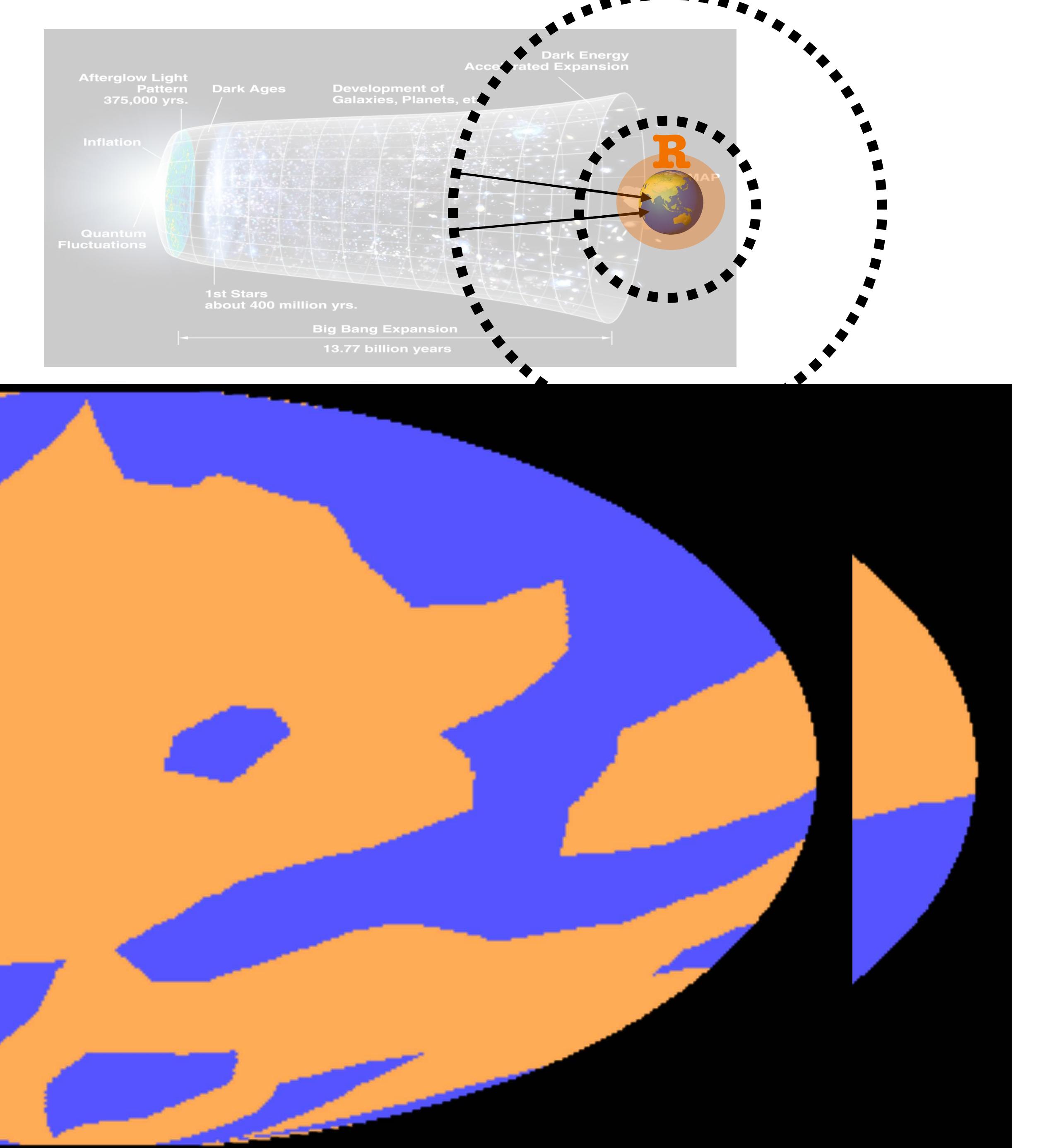


Vacua with scaling solution



Based on a simplified estimation assuming $O(1)$ vacua per a Hubble patch at random.

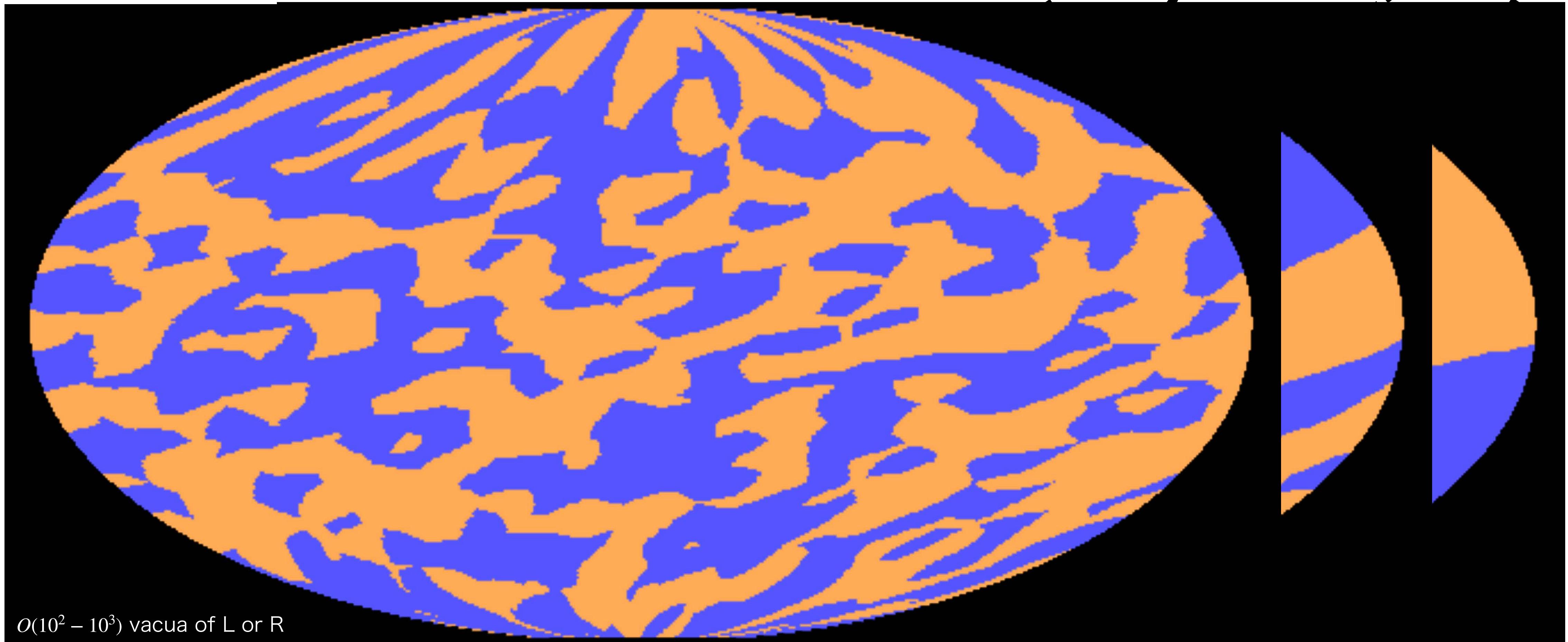
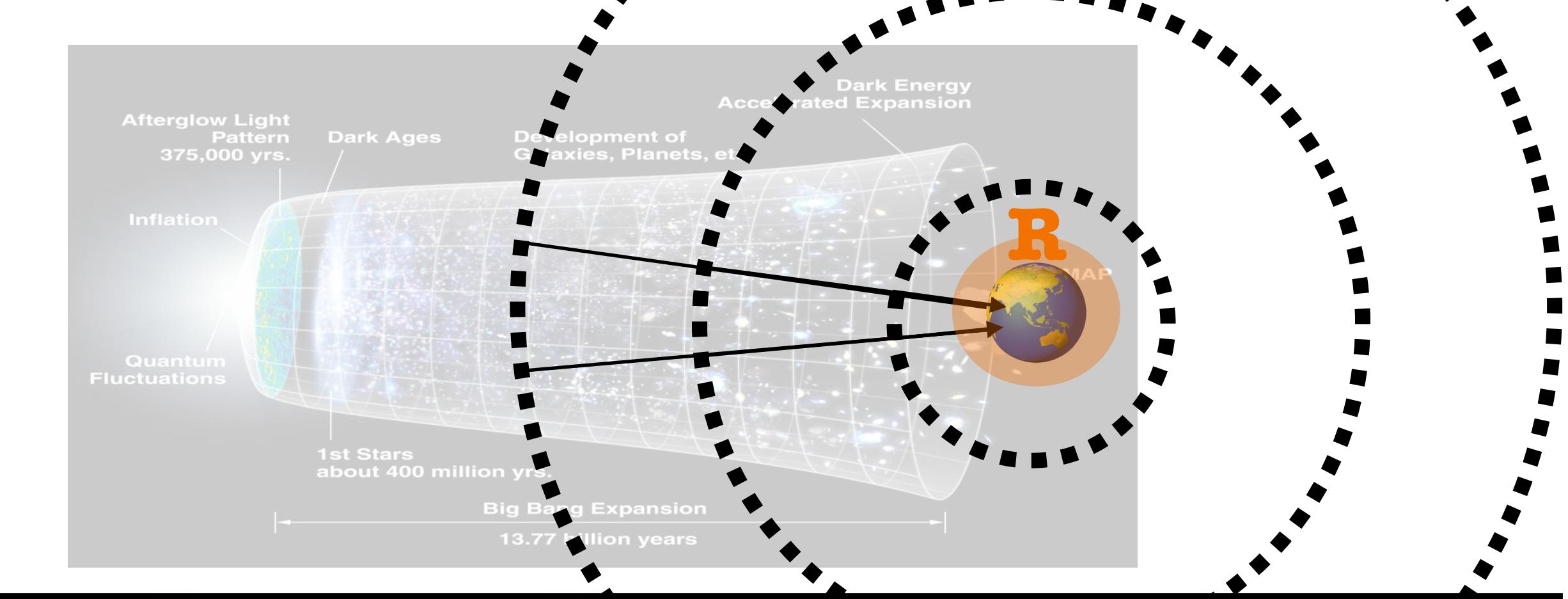
Vacua with scaling solution



$O(10 - 10^2)$ vacua of L or R

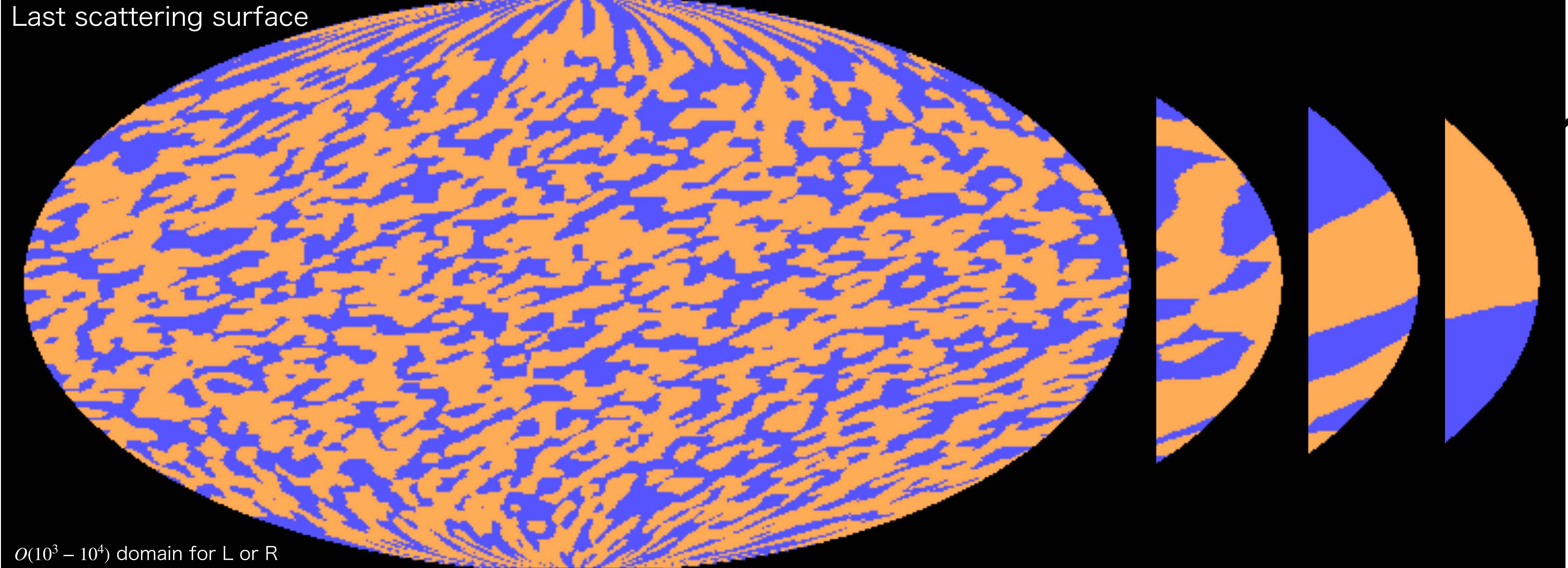
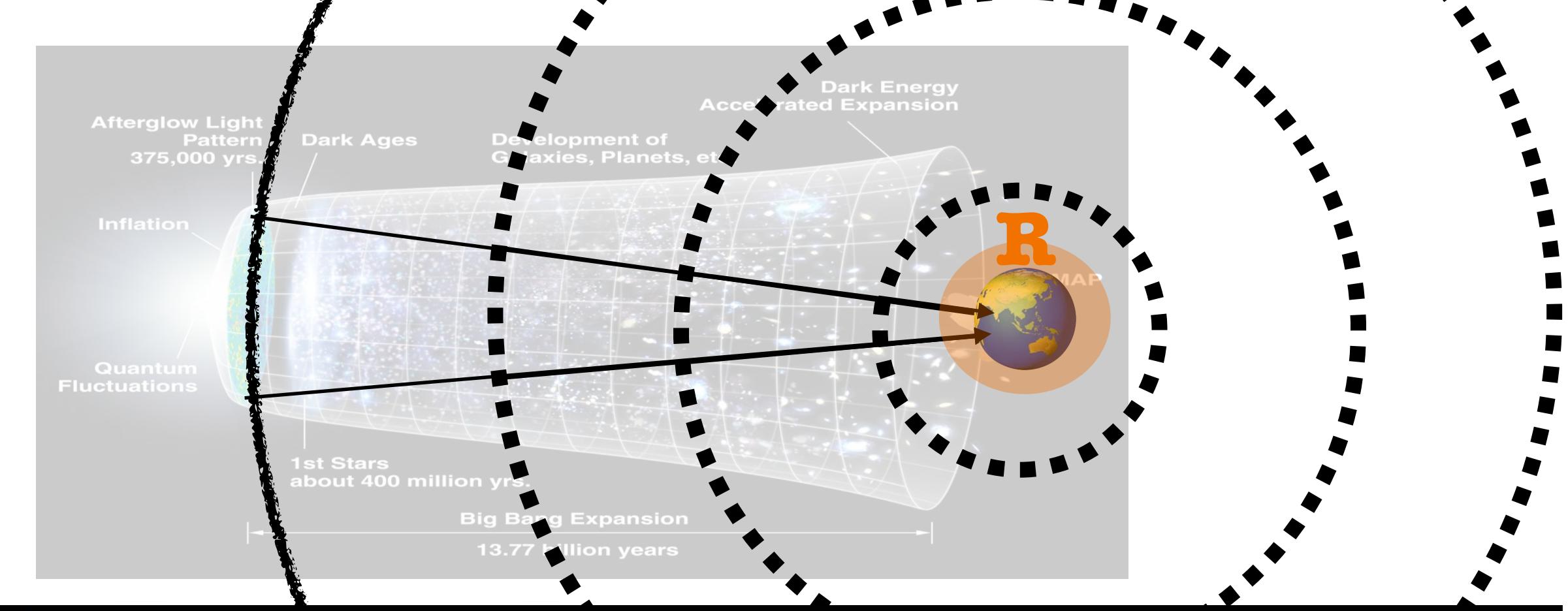
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Vacua with scaling solution

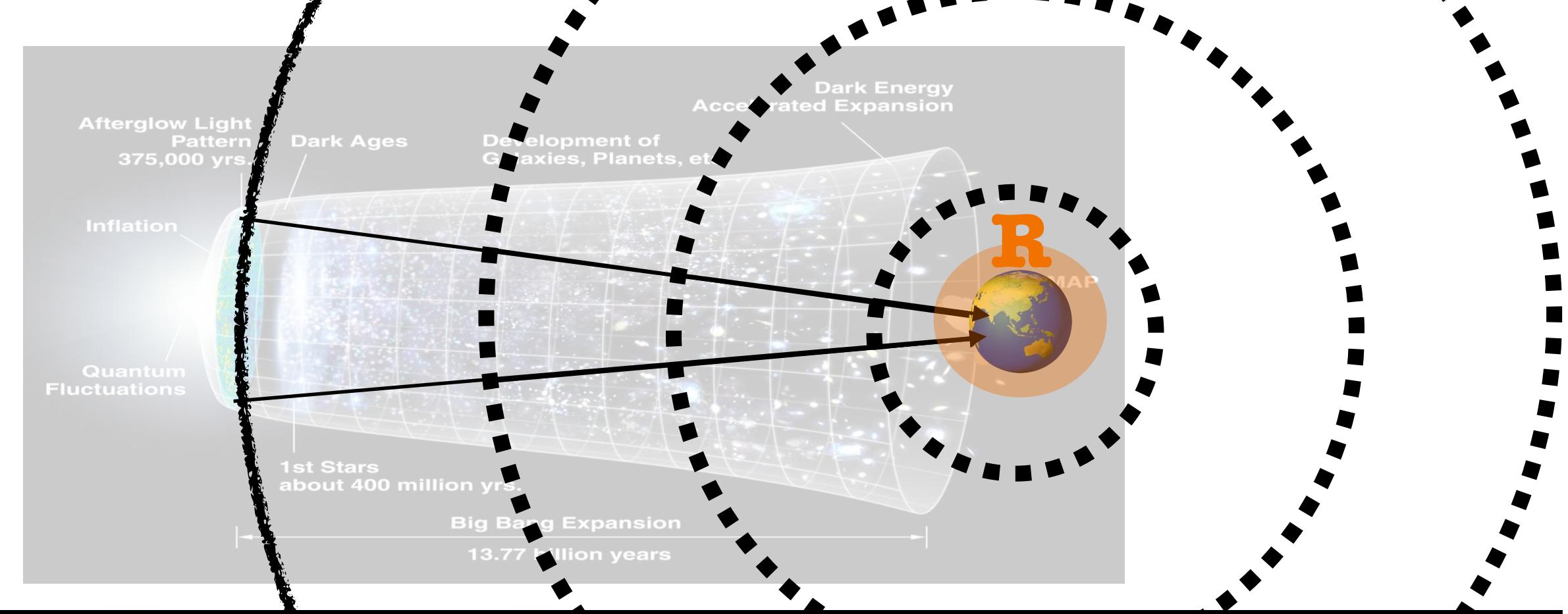


Vacua with scaling solution

CMB photons are from vacua with

kilobyte patterns of L or R:

**kilobyte cosmic birefringence
(KBCB).**



Last scattering surface

ALP DWs without strings+scaling solution → KBCB

$O(10^3 - 10^4)$ domain for L or R

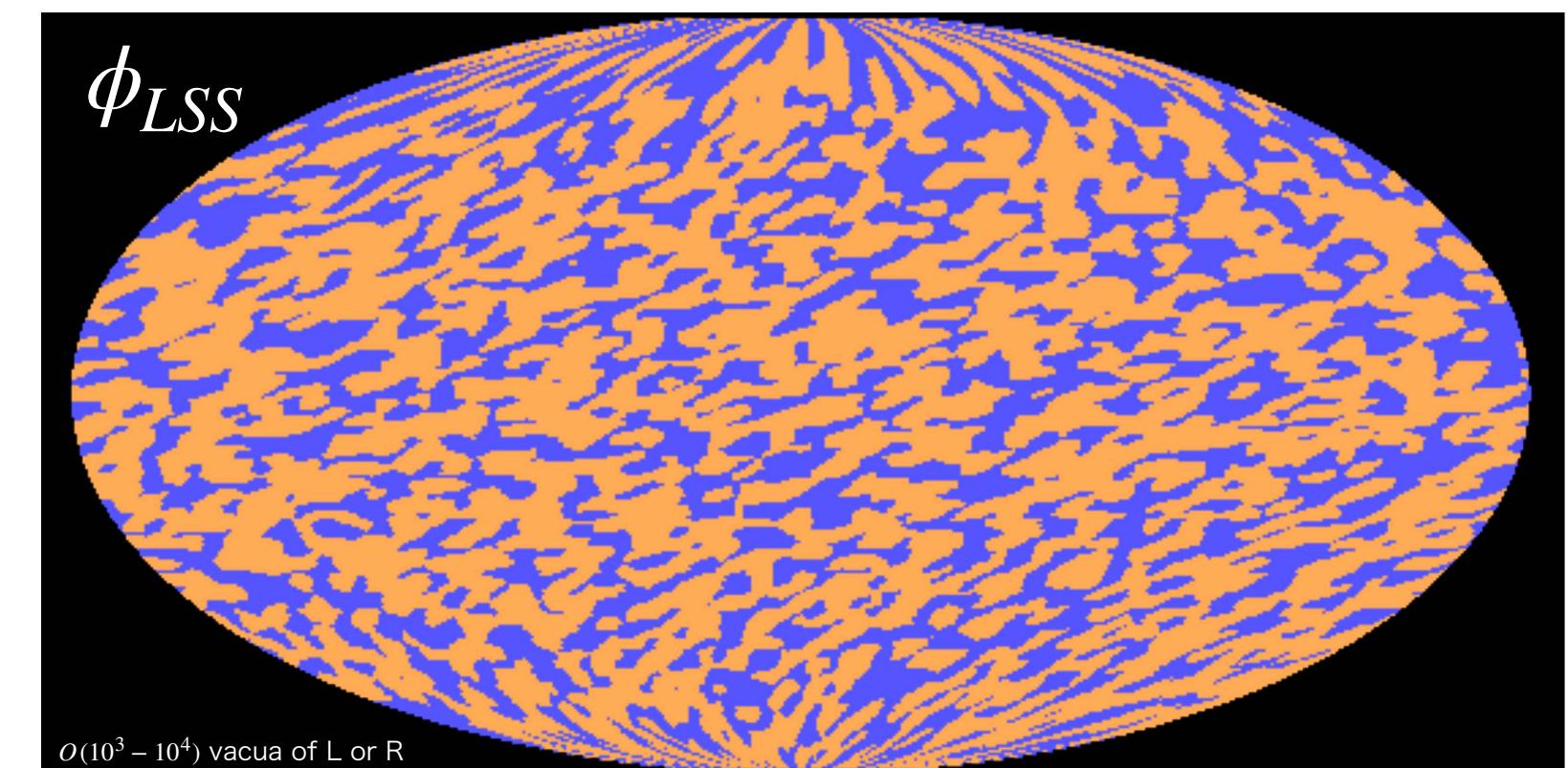
Based on a simplified estimation assuming $O(1)$ vacua per a Hubble patch at random.

Spectrum of KBCB

Isotropic KBCB

$$\Phi(\Omega) = \int_{\text{LSS}[\Omega]}^{\text{Earth}} c_\gamma \frac{d\phi}{2f_\phi} = \frac{c_\gamma \alpha}{2\pi f_\phi} (\phi_{\text{Earth}} - \phi_{\text{LSS}}[\Omega])$$
$$\phi_{\text{LSS}} = -\pi f_\phi \text{ or } \pi f_\phi, \phi_{\text{Earth}} = \pi f_\phi$$

$$\beta = \frac{1}{4\pi} \int d\Omega \Phi[\Omega] = \alpha c_\gamma / 2$$
$$= 0.21 c_\gamma \text{deg}$$



$$\beta_{\text{obs}} = 0.35 \pm 0.14 \text{ deg},$$

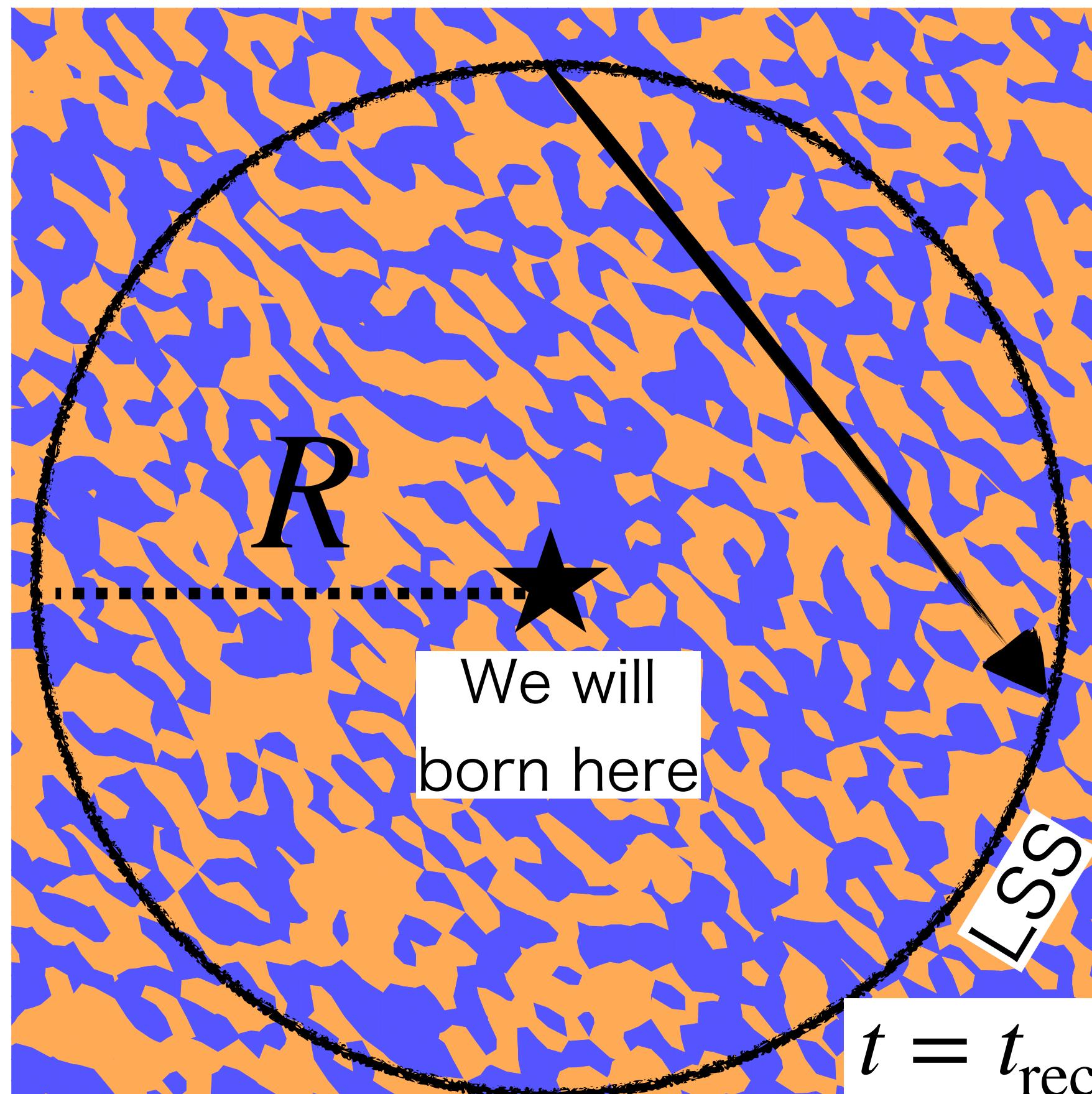
The attractor (scaling solution) prediction is consistent with measured one!

A modeling for anisotropic KBCB

Angular power spectrum: $\bar{C}_\ell^\Phi = 2\pi \int d\cos\theta \langle \Delta\Phi(0,0)\Delta\Phi(\theta,0) \rangle P_\ell(\cos\theta)$

$$\Delta\Phi \equiv \Phi(\Omega) - \beta$$

$$\langle \Delta\Phi(0,0)\Delta\Phi(\theta,0) \rangle \simeq \beta^2(2P_{\text{match}} - 1)$$



$$L \xrightarrow{\Delta x = N\delta x} L$$

$$P_{\text{DW}} = \kappa_{\text{DW}} H_{\text{rec}}, \quad \kappa_{\text{DW}} = O(1)$$

(i.e. $O(1)$ DW within one Hubble)

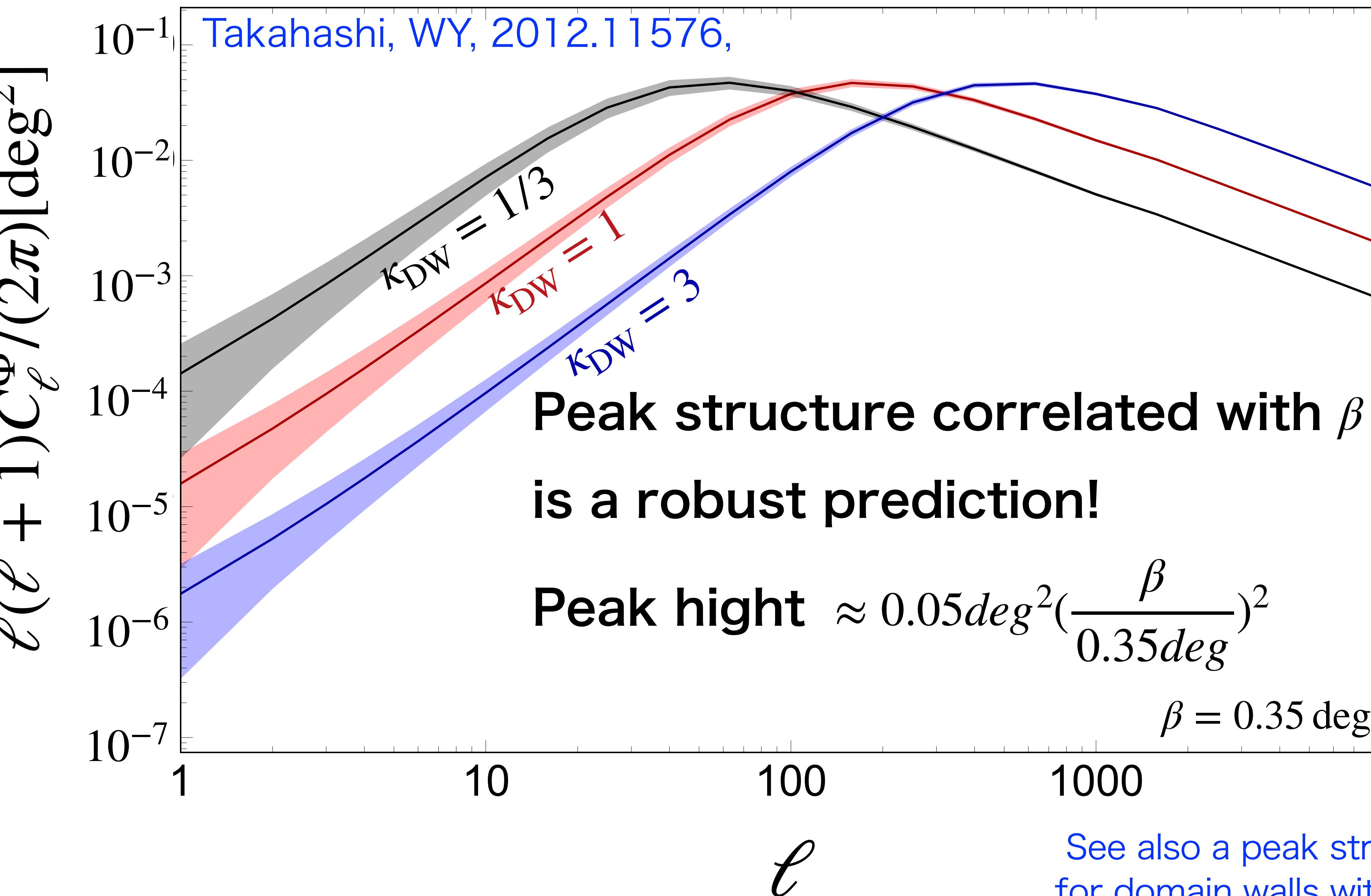
$$P_{\text{match}}[\Delta x] = \sum_{N/2 \geq m=0} \frac{N!}{2m!(N-2m)!} (P_{\text{DW}}\delta x)^{2m} (1 - P_{\text{DW}}\delta x)^{N-2m} \rightarrow \frac{1}{2}(1 + e^{-2P_{\text{DW}}\Delta x}),$$

Our DW modeling:

$$\langle \Delta\Phi(0,0)\Delta\Phi(\theta,0) \rangle \simeq$$

$$\beta^2 e^{-2P_{\text{DW}}R\sqrt{2(1-\cos\theta)}} \sim \beta^2 e^{-176\kappa_{\text{DW}}\sqrt{1-\cos\theta}}$$

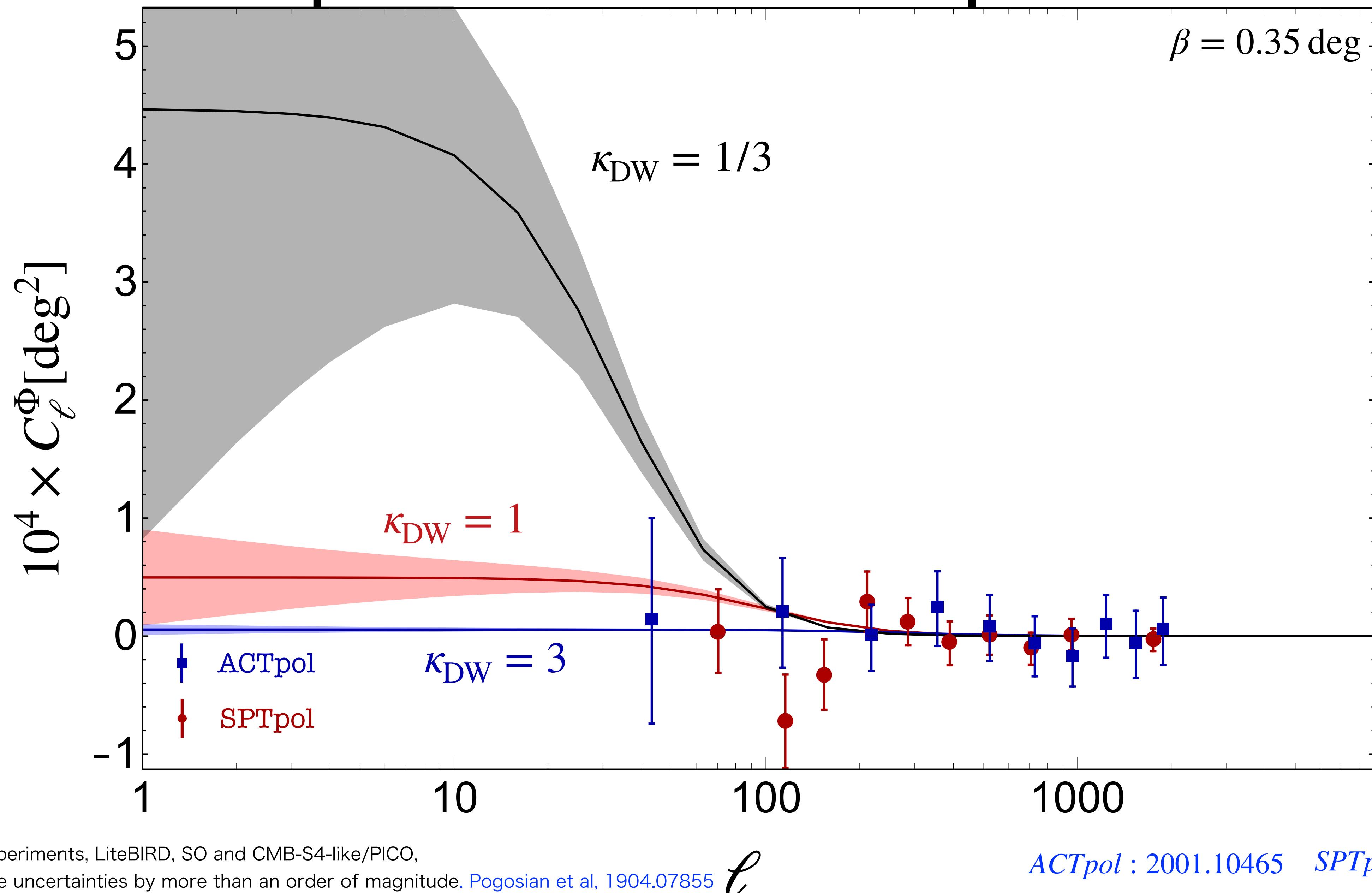
Anisotropic KBCB



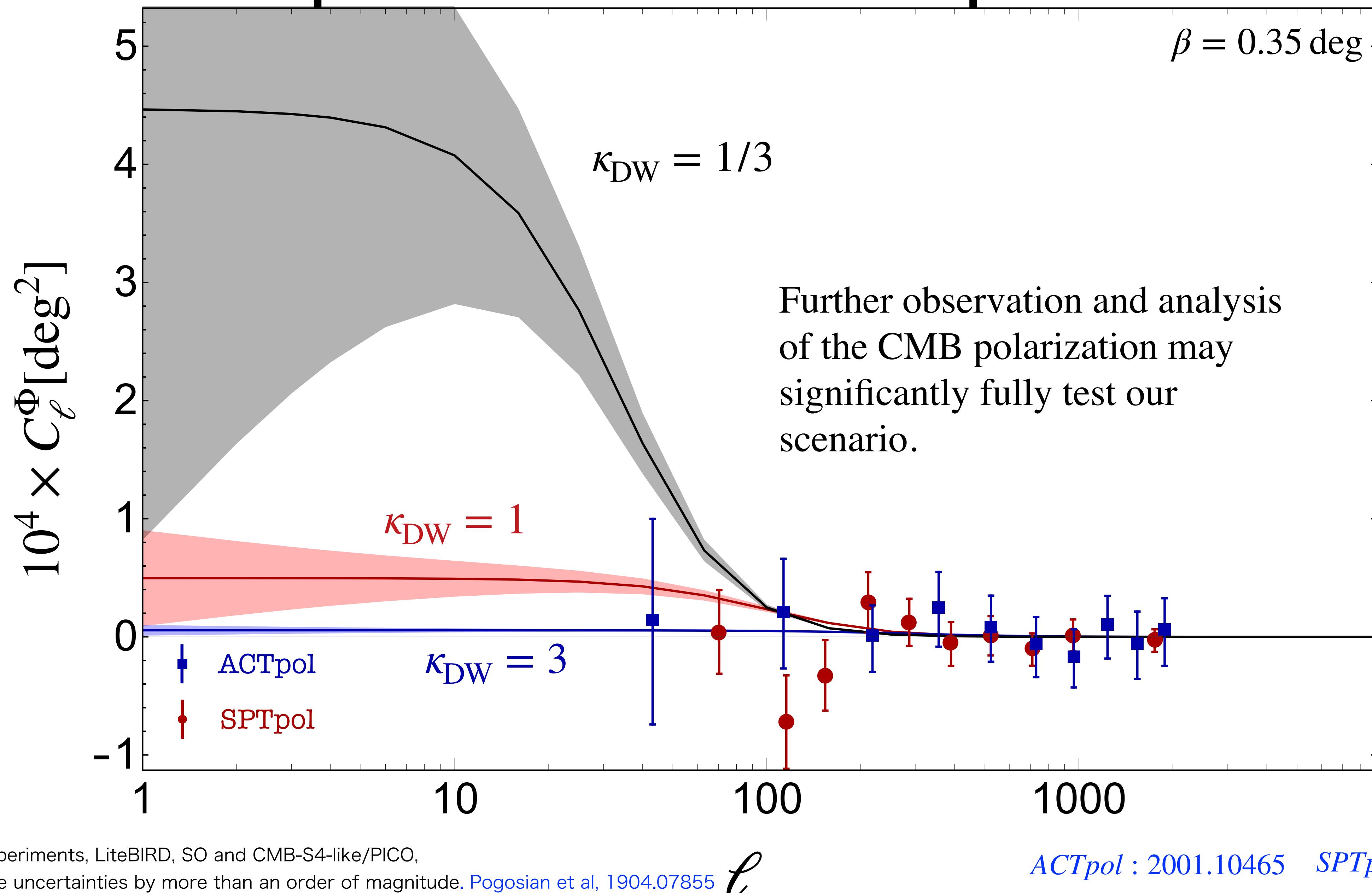
Cosmic variance:

$$\Delta C_\ell^\Phi \approx \sqrt{\frac{2}{2\ell + 1}} \bar{C}_\ell^\Phi$$

Anisotropic KBCB and experimental data



Anisotropic KBCB and experimental data



ACTpol : 2001.10465 SPTpol : 2006.08061

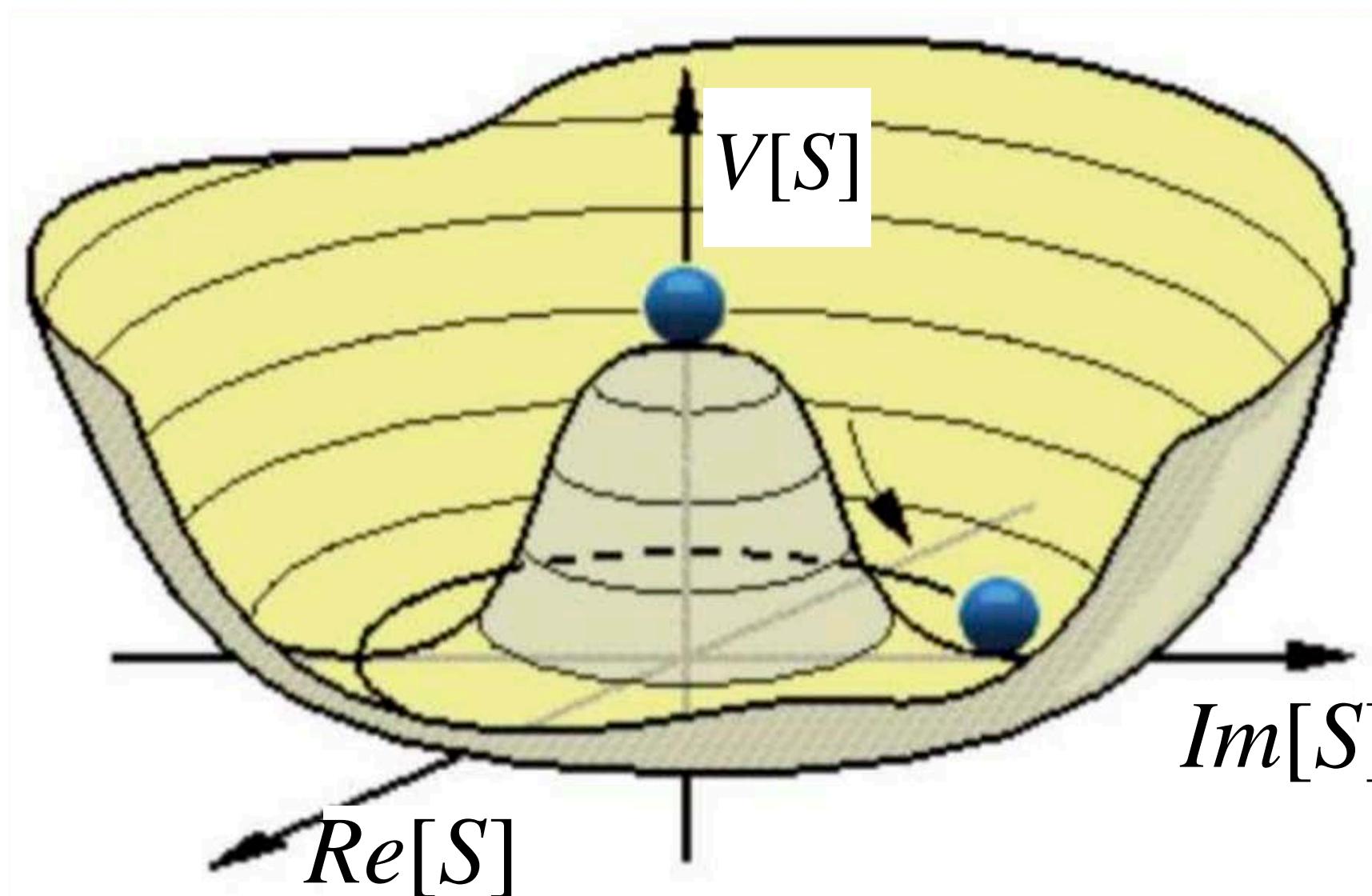
Conclusions

- Isotropic cosmic birefringence (CB) implies slow-roll ultra-light ALP or ALP domain wall without a string.
- ALP domain wall without a string can be naturally formed due to inflation fluctuation. (It can also be formed by the mixing with QCD axion. [Takahashi WY 2012.11576](#))
- The attractor scaling solution of the domain wall predicts a kilobyte (KB) CB.
- The attractor predictions of the isotropic and anisotropic KBCB are correlated and are recently consistent with the observations!
- Further observation and analysis of the CMB polarization may reveal the information of order KB encoded on the LSS.

backup

ALP: Nambu Goldstone boson of a global Peccei-Quinn (PQ) symmetry $U(1)$ that is anomalous to photons.

If a continuous global $U(1)$ symmetry is *spontaneously* broken, there is a massless NGB.

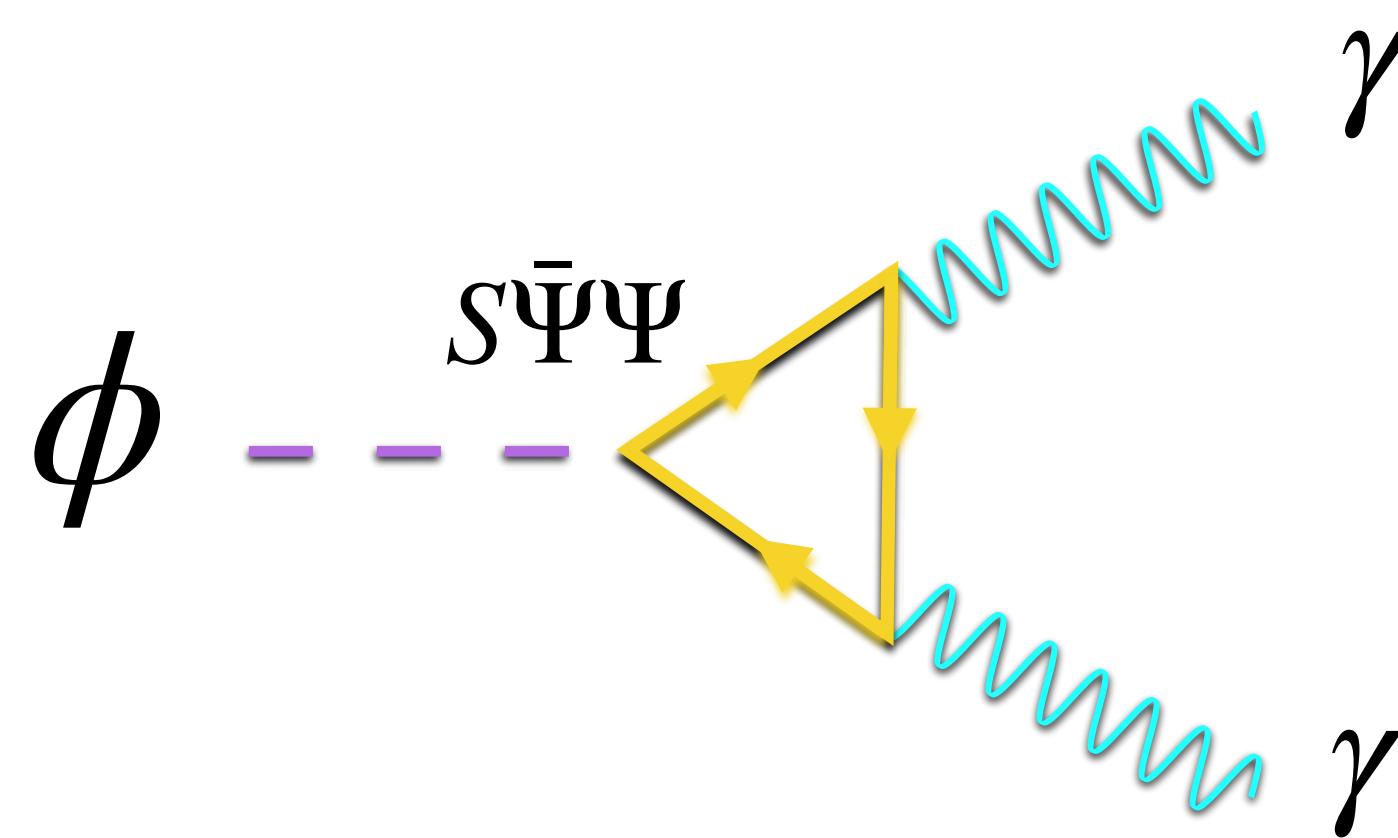


<https://physicsforme.com/2012/01/31/a-historical-profile-of-the-higgs-boson/>

$$S \sim (\nu + h)\exp(i\frac{\phi}{\sqrt{2}\nu})$$

$$U(1) \quad \phi \rightarrow \phi + \alpha$$

$$V[\phi] = V[\phi + \alpha]$$



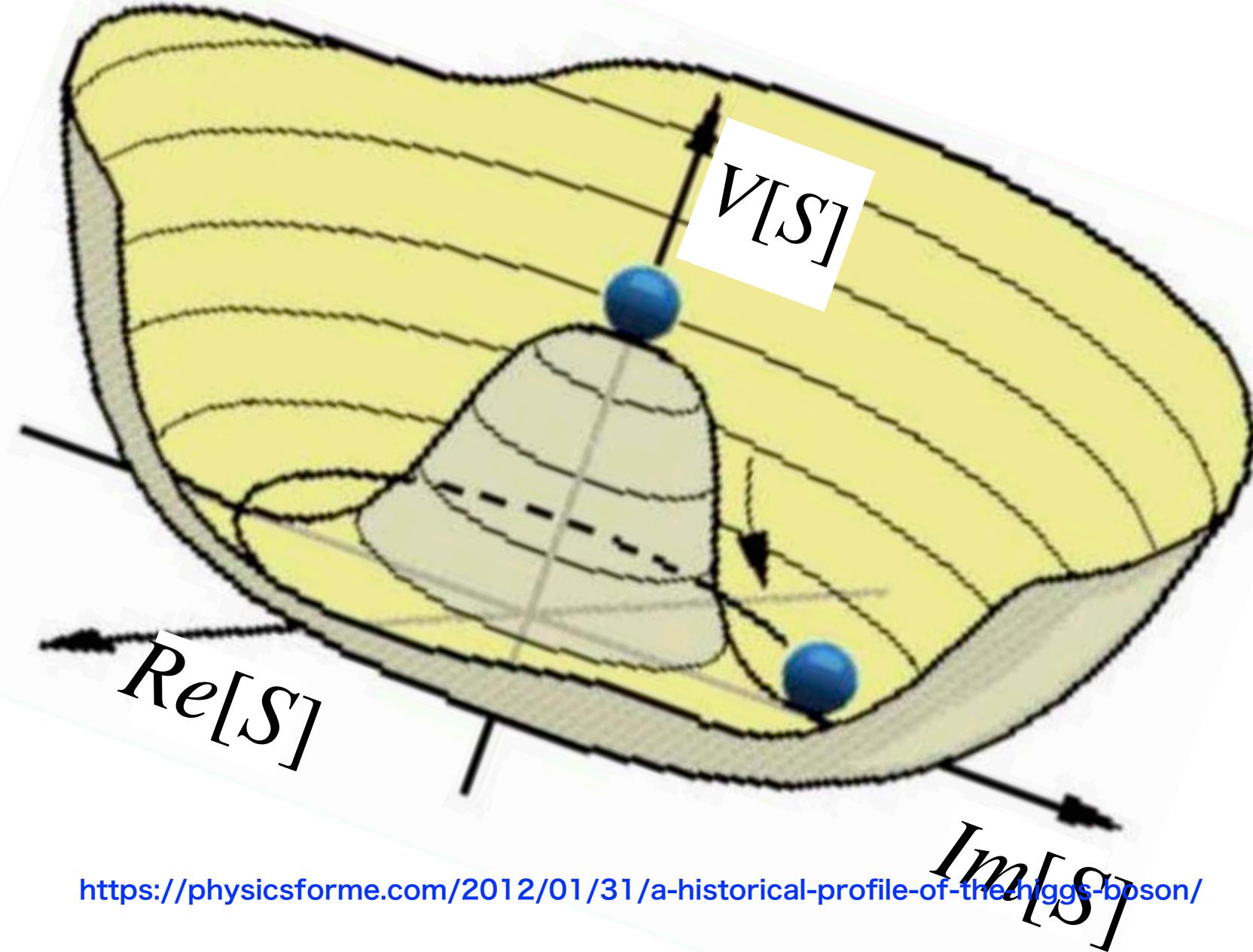
$$\mathcal{L} = -c_\gamma \frac{\alpha}{4\pi} \frac{\phi}{f_\phi} F_{\mu\nu} \tilde{F}^{\mu\nu}$$

$$c_\gamma = q_\Psi^2$$

-> naturally ϕ gets masses due to (small) instantons
(or quantum gravities).

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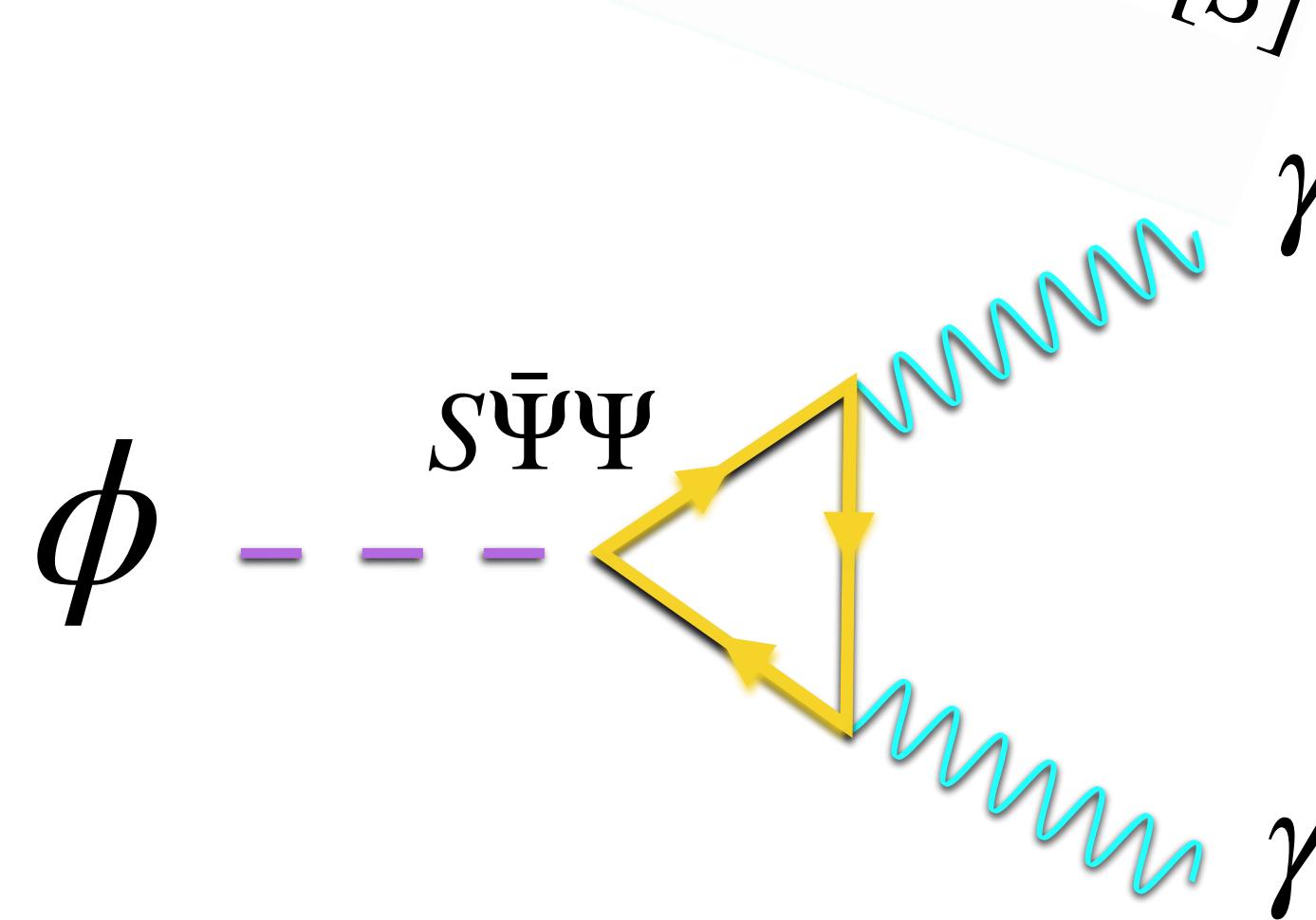


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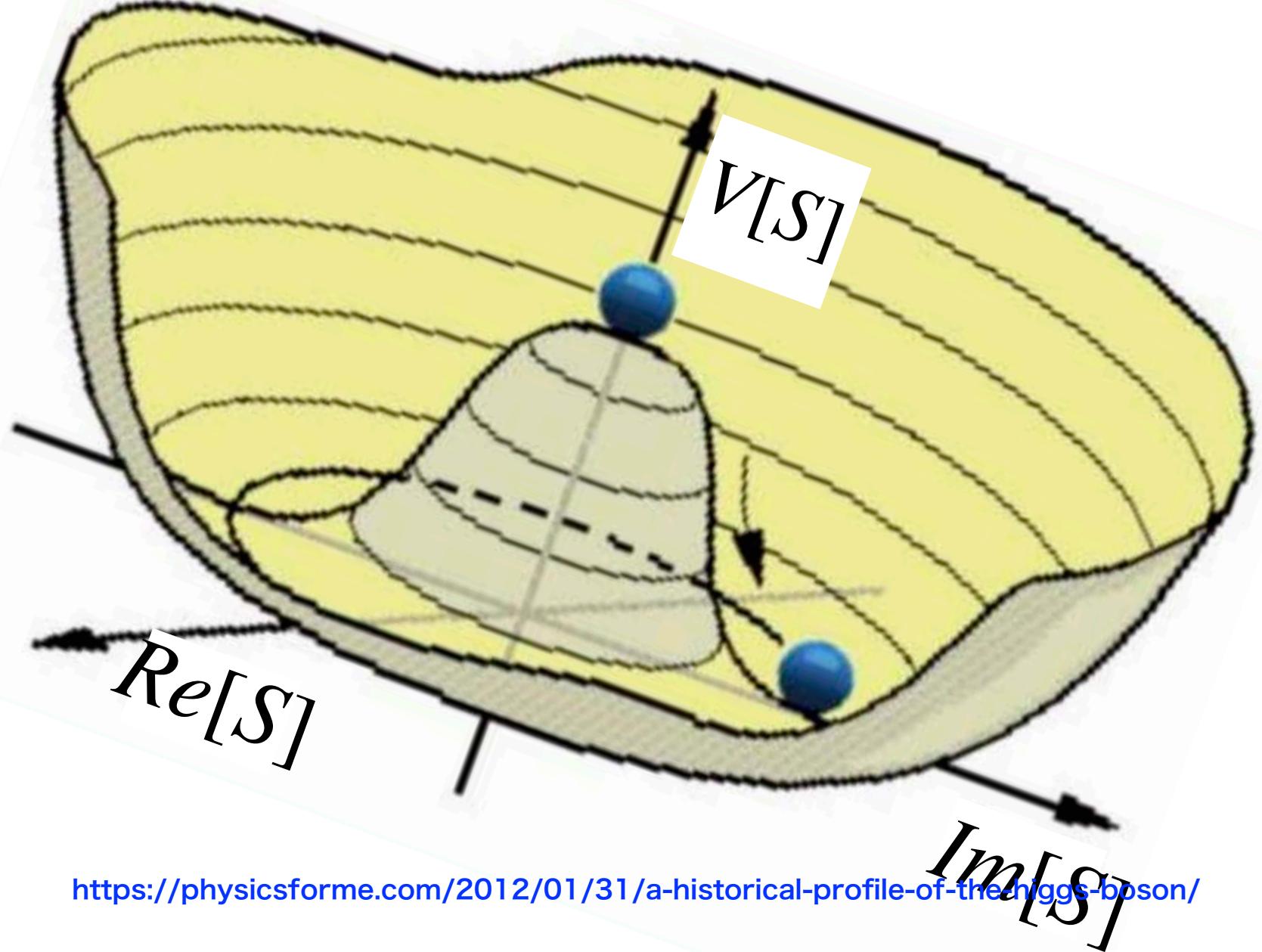
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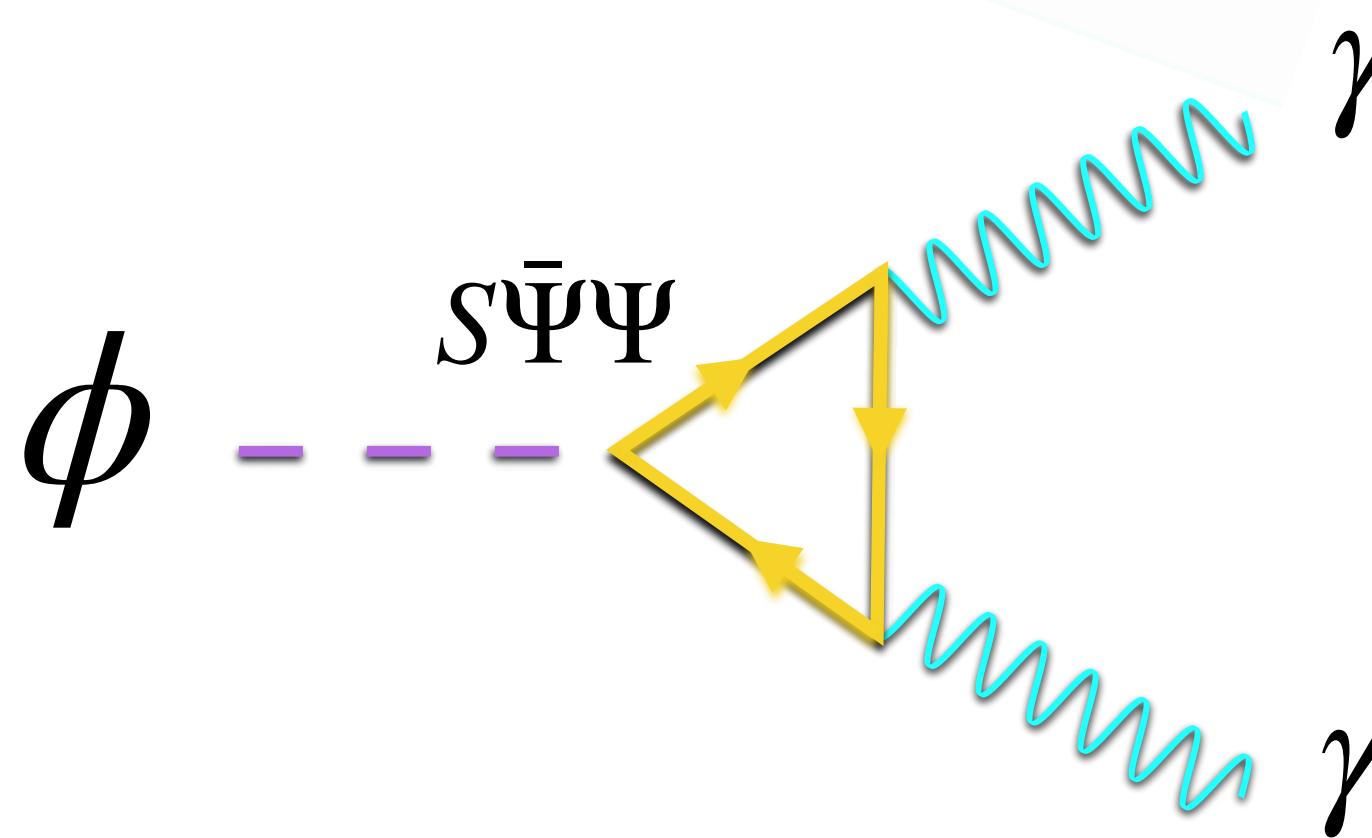
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$$V[\phi] = V[\phi + \alpha] + \delta V[\phi, \alpha]$$

$$\simeq \Lambda^4(1 - \cos[\phi/f_\phi]) \approx m_\phi^2 \phi^2 / 2$$

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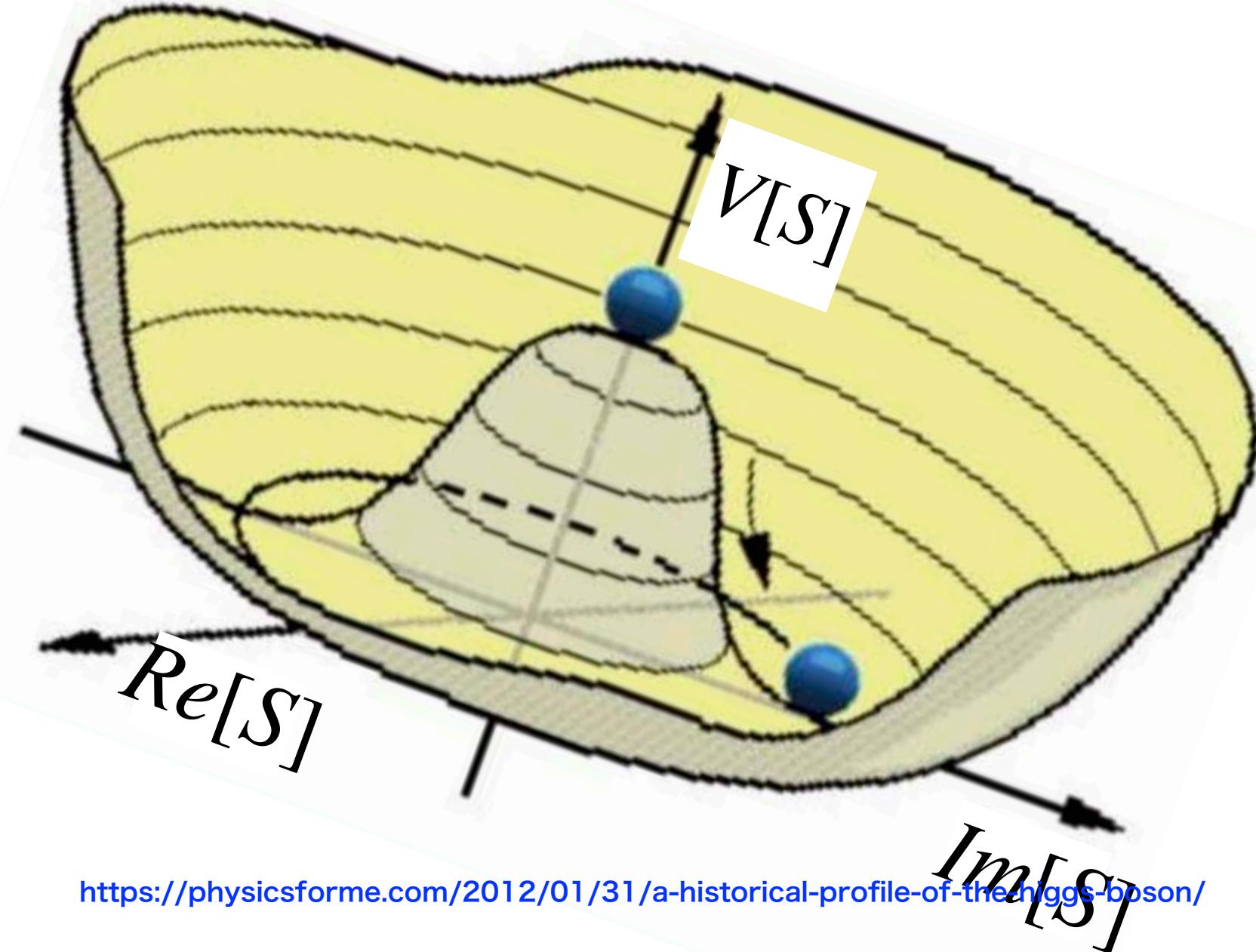
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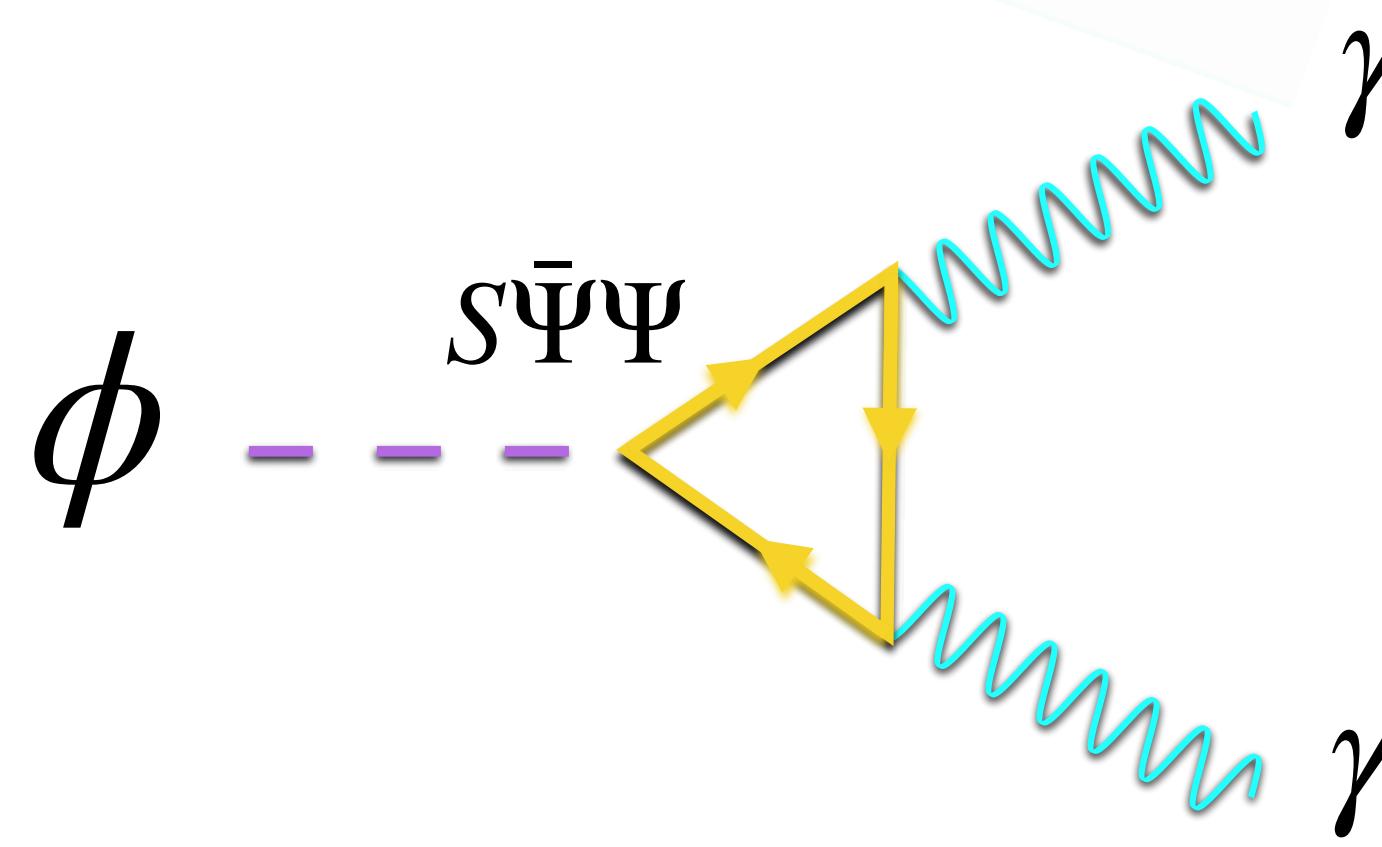
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ALPs are predicted in axiverse of string or M theory.

Isotropic Cosmic Birefringence by ALP models

- Isotropic CB by $\dot{\phi} \neq 0$: Slow-rolling ALP

Minami and Komatsu, 2006.15982,

Fujita et al, 2011.11894, (CB and H_0 tension)

Mehta et al, 2103.06812, (Many ALPs)

Nakagawa et al, 2103.08153, (Very light ALP)

- Isotropic CB by $|\partial_{\vec{x}}\phi| \neq 0$: Domain walls

Takahashi, WY, 2012.11576, (CB by Domain wall)

This talk

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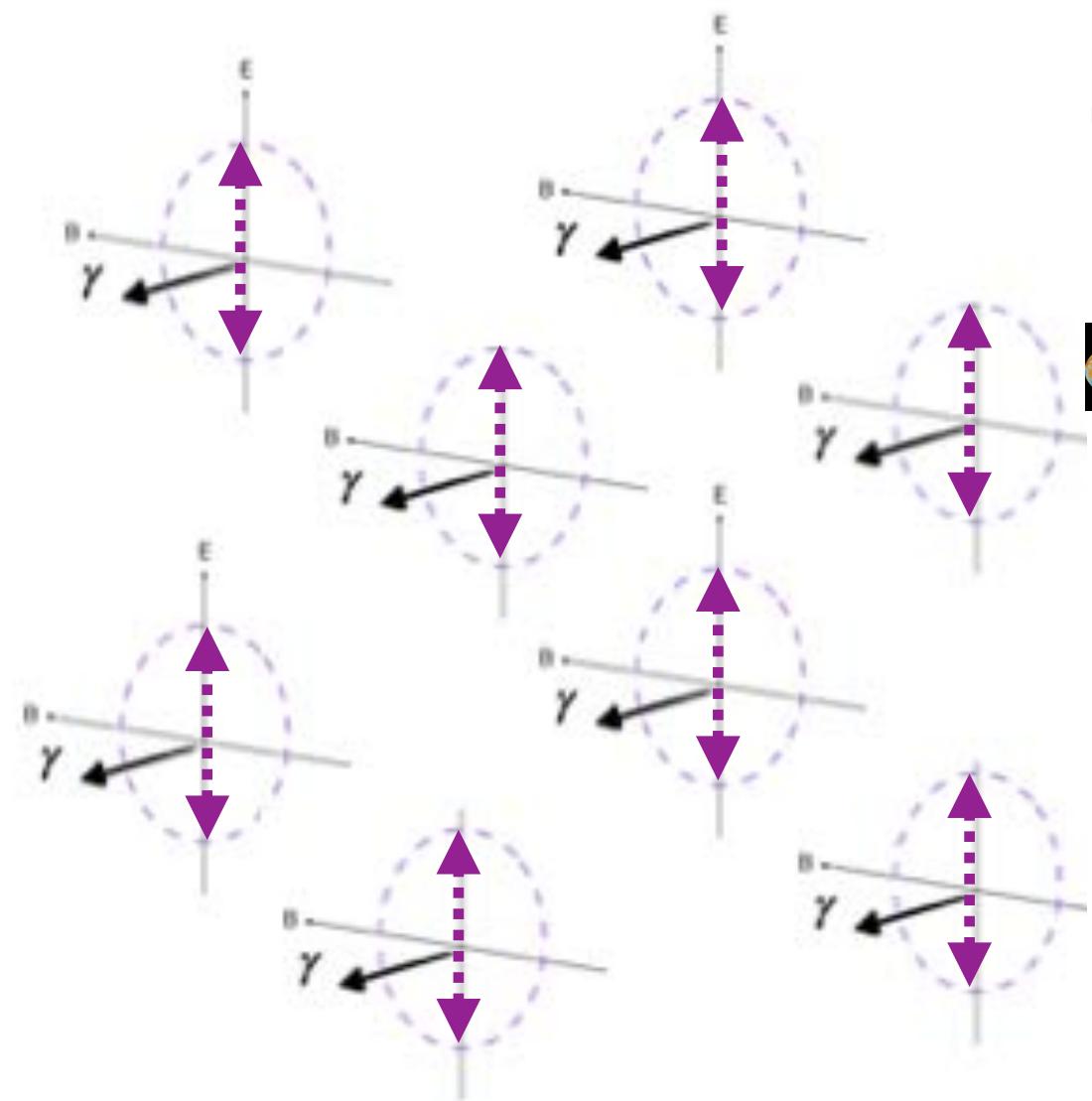
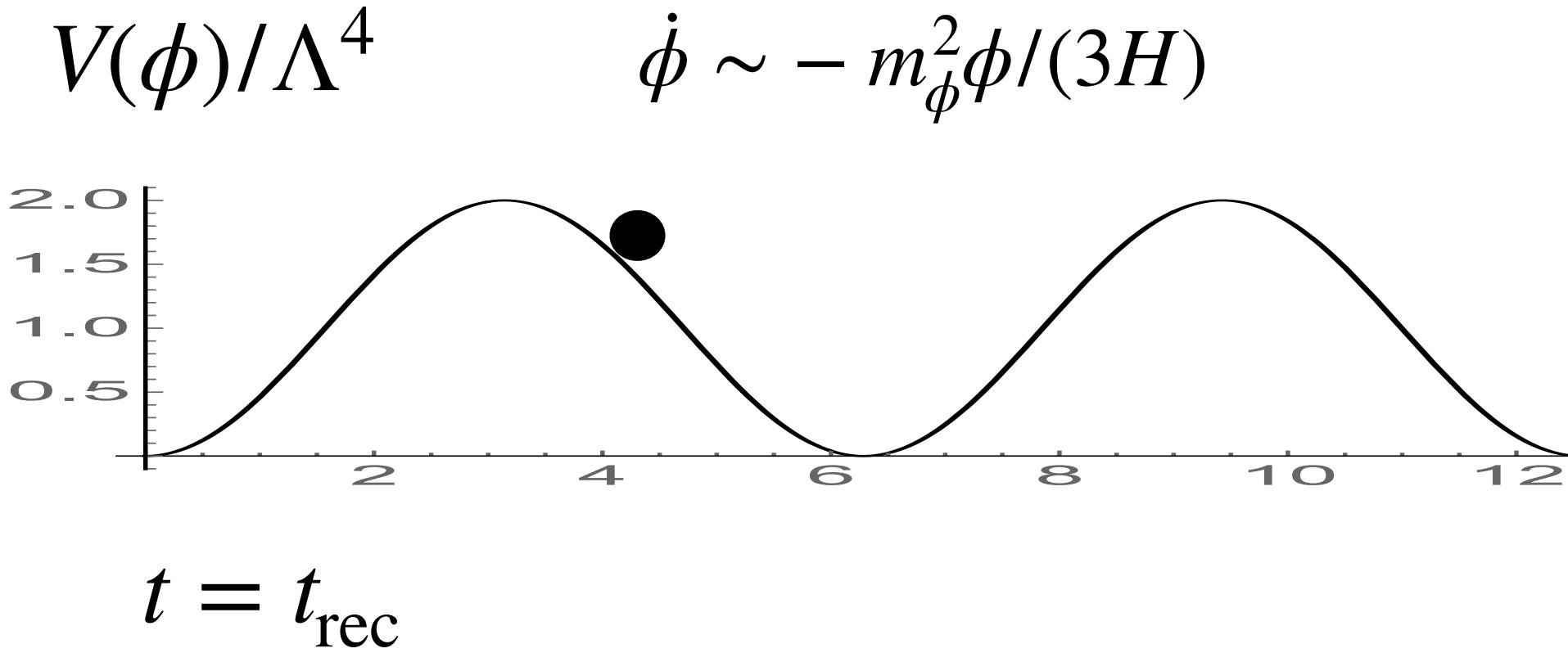
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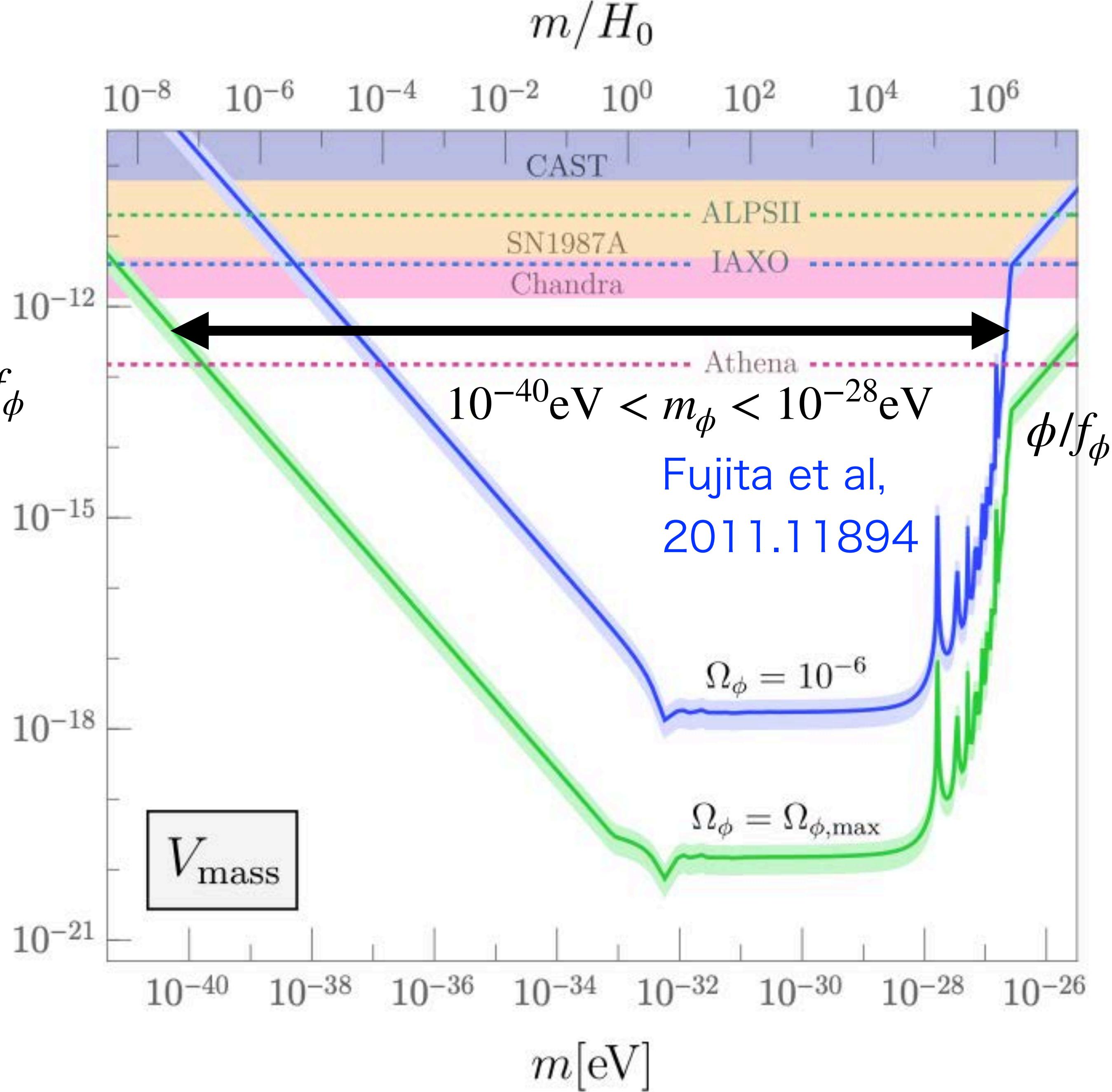
This talk

○ Slow-rolling ALP



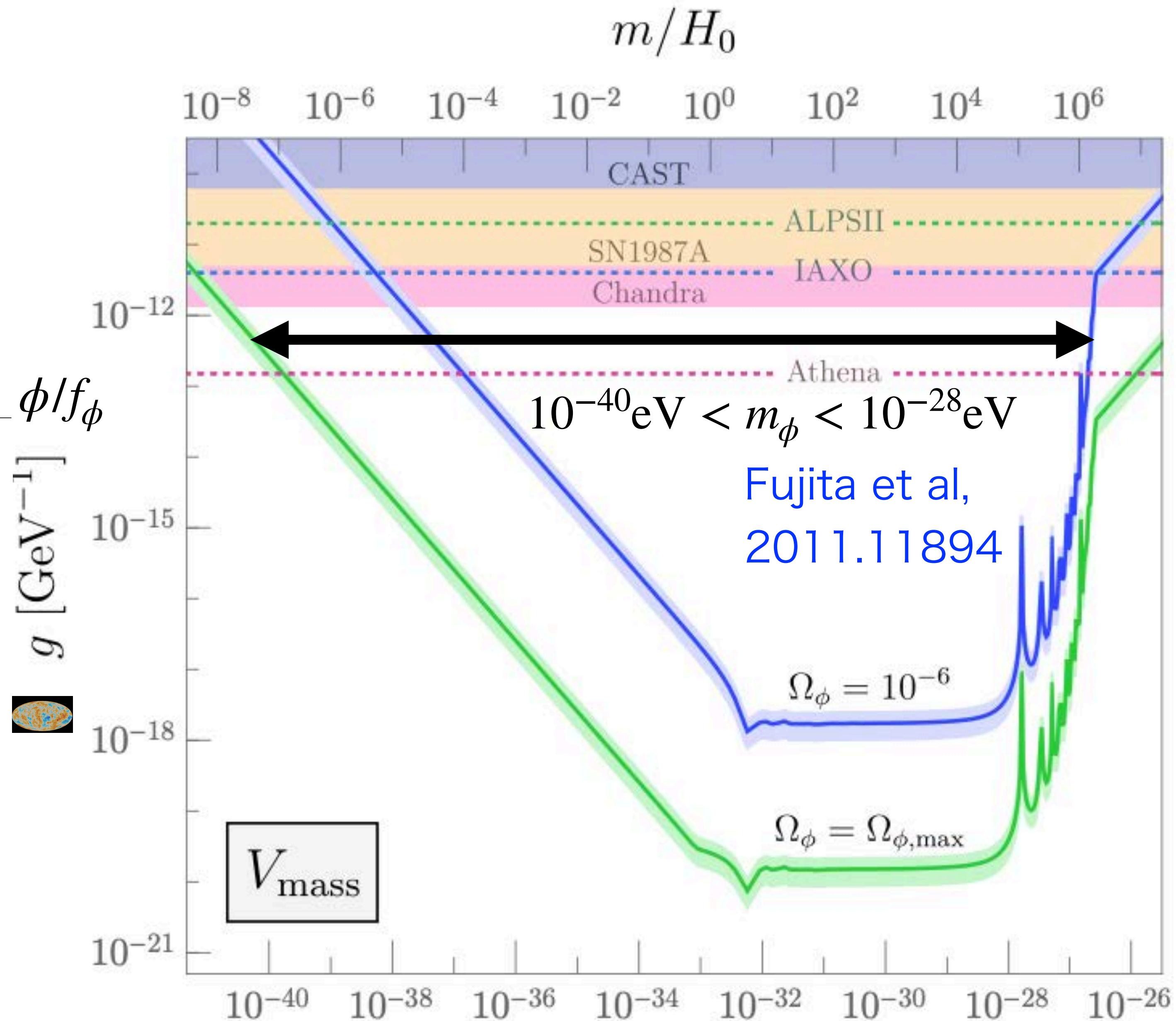
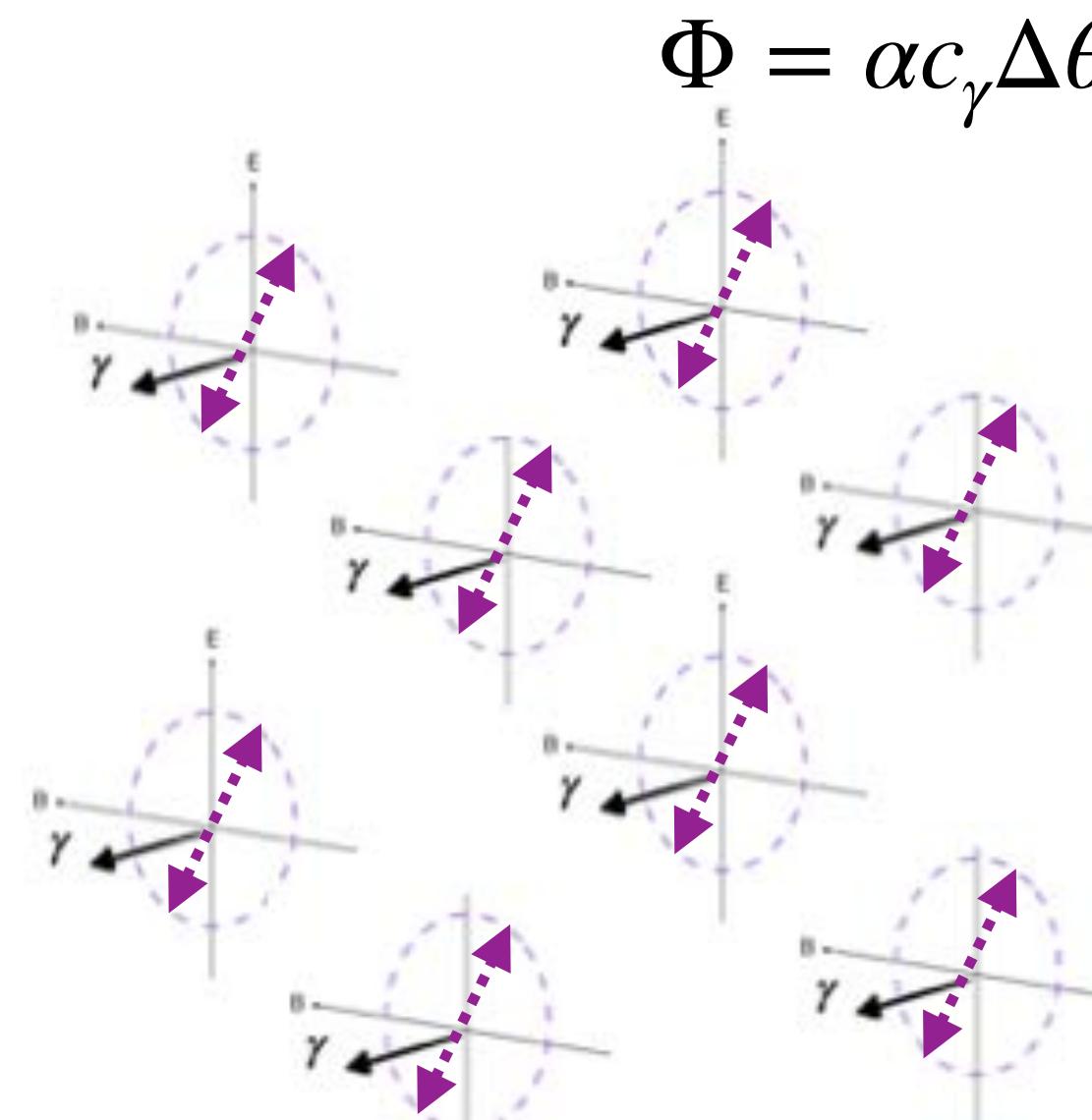
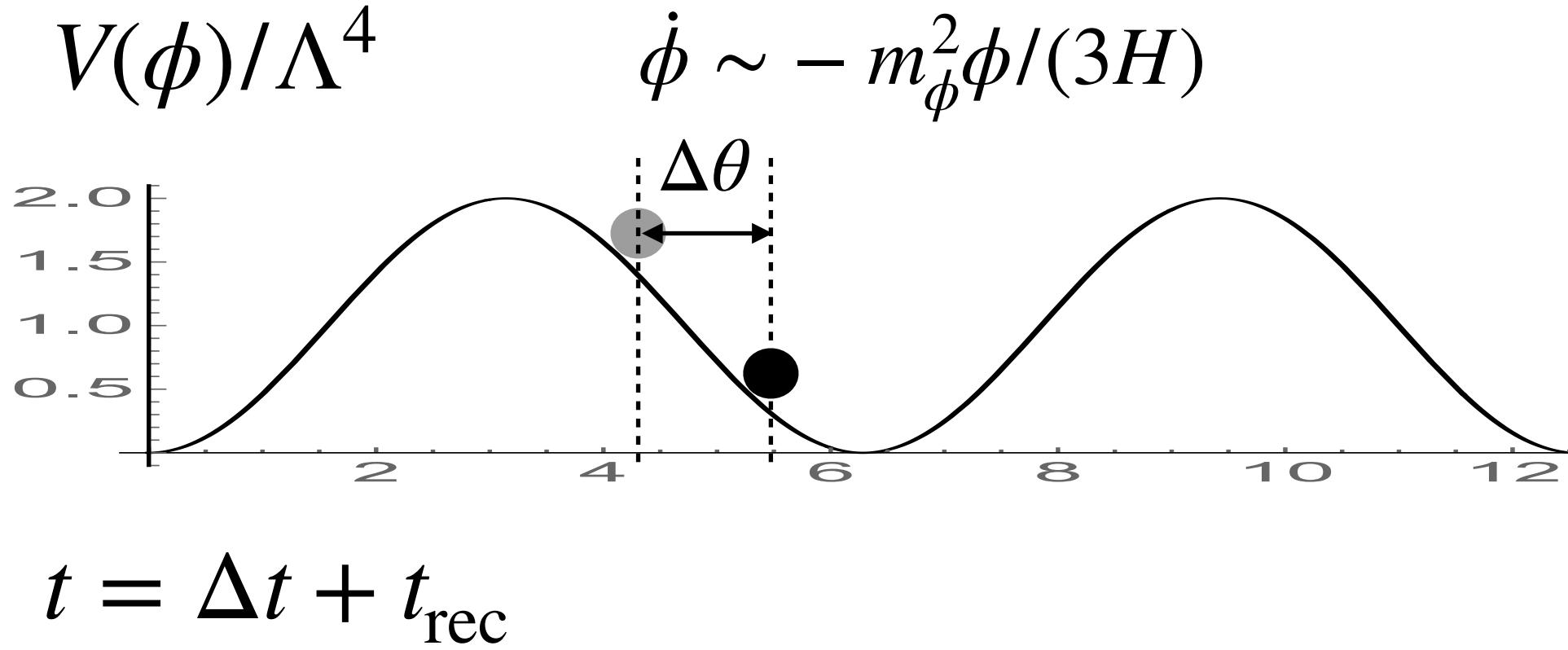
ϕ/f_ϕ

$g [\text{GeV}^{-1}]$



Hidden monopole DM coupled to ALP, ALP can be lighter Nakagawa et al, 2103.08153.

○ Slow-rolling ALP



Inflationary fluctuation can also induce anisotropic CB.

Hidden monopole DM coupled to ALP, ALP can be lighter Nakagawa et al, 2103.08153.

Review: Cosmic Birefringence from Strings

Agrawal et al, 1912.02823;

- PQ symmetry breaking after inflation induces strings (with domain walls).
- Anisotropic cosmic birefringence but **negligible isotropic cosmic birefringence.**

$$\beta = \frac{1}{4\pi} \int d\Omega \Phi[\Omega] \simeq 0$$

